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General approach for the determination of the magneto-angular dependence of the critical current of YBCO coated conductors

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Abstract

The physical understanding and numerical modelling of superconducting devices which exploit the high performance of second generation high temperature superconducting tapes (2G-HTS), is commonly hindered by the lack of accurate functions which allow the consideration of the in-field dependence of the critical current. This is true regardless of the manufacturer of the superconducting tape. In this paper, we present a general approach for determining a unified function $I_c(B, \theta)$, ultimately capable of describing the magneto-angular dependence of the in-field critical current of commercial 2G-HTS tapes in the Lorentz configuration. Five widely different superconducting tapes, provided by three different manufacturers, have been tested in a liquid nitrogen bath and external magnetic fields of up to 400 mT. The critical current was recorded at 90 different orientations of the magnetic field ranging from $\theta = 0^\circ$, i.e., with B aligned with the crystallographic ab-planes of the YBCO layer, towards $\pm 90^\circ$, i.e., with B perpendicular to the wider surfaces of the 2G-HTS tape. The whole set of experimental data has been analysed using a novel multi-objective model capable of predicting a sole function $I_c(B, \theta)$. This allows an accurate validation of the experimental data regardless of the fabrication differences and widths of the superconducting tapes. It is shown that, in spite of the wide set of differences between the fabrication and composition of the considered tapes, at liquid nitrogen temperature the magneto-angular dependence of the in-field critical current of YBCO-based 2G-HTS tapes, can be described by a universal function $I_c(f(B), \theta)$, with a power law field dependence dominated by the Kim's factor B/B_0 , and an angular dependence moderated by the electron mass anisotropy ratio of the YBCO layer.

Keywords: superconductors, YBCO coated conductors, critical currents, angular dependence, finite-element analysis, AC losses

(Some figures may appear in colour only in the online journal)

1. Introduction

It is expected that the progressive development of superconducting applications such as superconducting fault current limiters [1], power transmission lines [2], and HTS rotary

machines [3, 4], together with a steady progress in the deposition techniques and fabrication of YBCO coated conductors or 2G-HTS tapes will lead to more competitive prices and improved efficiencies in comparison to resistive conductors such as copper. However, in order to design or optimize a superconducting machine composed of 2G-HTS tapes, ideally it is necessary to know in advance what is the value of the critical current density of the used tape when it is affected by an external magnetic field, also called the in-field critical current density $J_c(B, \theta)$ [5].



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The critical current density of YBCO coated conductors displays a complex anisotropic behaviour for in-plane and out-of-plane applied magnetic field, even when the field is only applied in perpendicular direction with the flow of the electric current, and the complex interaction between shielding and transport currents is confined to two dimensions. The essential physics behind the collected vast phenomenology has been well known for decades [6, 7] and it may be analysed in terms of interactions between the flux lines themselves (lattice elasticity and line cutting) and interactions with the underlying crystal structure (flux pinning). However, if \mathbf{J} is locally perpendicular to \mathbf{B} , it is easy to demonstrate that the flux lines are always parallel to each other [8] and therefore, the anisotropy of the in-field critical current density $J_c(B, \theta)$ may have its main origin in the crystal structure and fabrication of the YBCO layer. It is this dependence on the fabrication process what hinders the assertion of the existence of a general function that might describe the in-field dependence of the critical current density of commercial 2G-HTS tapes, regardless of their manufacturer.

We have experimentally measured the $J_c(B, \theta)$ function of different batches of superconducting tapes fabricated by three different companies, namely SuperPower Inc. (SP) [9], American Superconductor (AMSC) [10], and Shanghai Superconductor Technology Co., Ltd. (SHSC) [11], under the same experimental conditions, in order to explore the possibility of unifying their physical behaviour in a general $J_c(B, \theta)$ function. The critical current density profiles of the tested tapes are measured under the action of a homogeneous external magnetic field of intensities ranging from 50 to 400 mT, in all cases. The experiment has been performed such that the angular dependence on the magnetic field can be studied in increments of 2° from the in-plane field approach, i.e., with the field parallel to the wider surface of the SC tape and with $\mathbf{J} \perp \mathbf{B}$. It covers the peak width of the critical current density which spans towards the out-of-plane field directions ($\theta = \pm 90^\circ$), with the maximum centred when the magnetic field is applied parallel to the wider surface of the SC tape. Thus, later it is shown that regardless of the manufacturer and width of superconducting tape, a simplified function of the in-field critical current density $J_c(B, \theta)$ can be constructed, by extending the scope of the Kim's model $J_c(B)$ for the out-of-plane approach, and assessing the magneto-angular dependence of the fitting parameters therein assumed [12].

This paper is organized as follows. In section 2, the experimental setup and the most relevant information for the classification of the superconducting tapes considered across this study, are presented. Then, in section 3 the underlying approximations and the numerical procedure that has been implemented for the identification of a general function for the in-field magneto-angular dependence of the critical current for second generation HTS tapes, are discussed in detail. It will be shown that our numerical results allow to prove the existence of a sole equation for the definition of the $I_c(B, \theta)$ function in the Lorentz configuration, by considering the experimental results obtained for up to five different samples these provided by three different manufacturers. Finally,

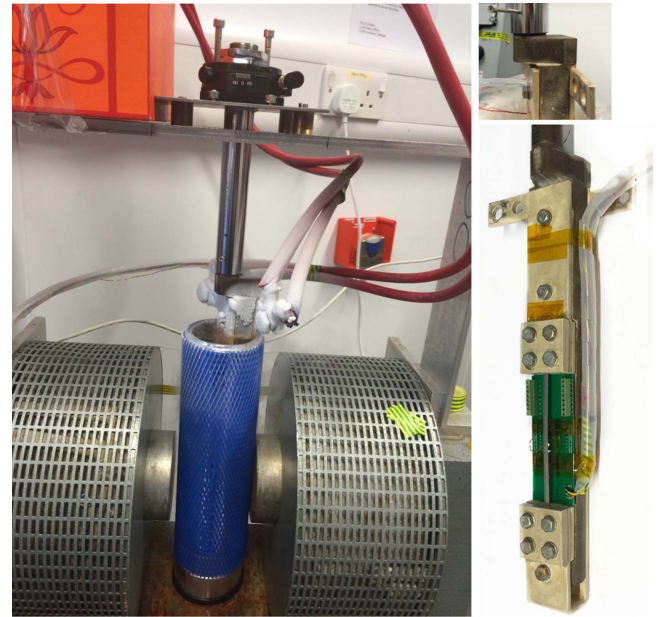


Figure 1. On the left, a picture of the experimental rig is presented. The sample holder and the neck offset for coaxial configuration is displayed in the right pane.

section 4 is devoted to summarize the main conclusions of this work.

2. Experimental setup and measured samples

A 600 mT electromagnet of ~ 204 mm pole face diameter was employed for the angle-resolved critical current density measurements. The magnetic field was measured with a HZ-11C hall-probe aligned with the pole face centre of the electromagnet. The longitudinal axis of the YBCO coated conductor, which was mounted over a tufnol support board, is coaxially aligned with the rotation axis of a high precision rotation stage as shown in figure 1. The current return path has been aligned parallel with the length of the sample at a distance of 10 cm, such that the maximum magnetic field produced by the current return path over the surface of the sample (~ 1 mT at 533 A), and its influence on the measurement of the critical current for applied magnetic fields ranging from 50 to 400 mT can be neglected. In addition, the shape of the tufnol board and the rod connecting with the rotation stage, have both been carefully designed with a neck offset in order to ensure a coaxial relationship between the test sample and the rotation stage in all field orientations.

Low temperature solder (melting point 470 K) was used to attach the voltage taps on the nameplate side of the YBCO coated conductor. However, depending on the characteristics of the stabilizer layer. The solder-flux used for adequate soldering of each of the voltage taps corresponded to the manufacturers' suggestions. For example for copper or brass laminated tapes, zinc chloride flux (Baker's Soldering Fluid No.3) was applied to the sample surface where solder dots were to be made. For stainless steel laminated tapes, highly

corrosive solder flux (Superflux, Castonlin Eutectic) was used to provide a better electrical connection.

The critical current of studied HTS tapes was measured while the samples were immersed in liquid nitrogen bath, with voltage criterion $E_0 = 1 \times 10^{-4} \text{ V m}^{-1}$ applied. All measured samples are 160 mm length, and the end terminals were clamped by copper plates and copper bases with four M5 cap head screws. The contact length was 15 mm for HTS tapes 4–6 mm width, and 25 mm for HTS tapes 10–12 mm width, respectively. High purity indium was also applied to the interlayer of coppers for cold welding, and the contact resistance at room temperature was determined to be 0.8 m Ω for 4–6 mm width tapes, and 0.2 m Ω for 10–12 mm width tapes, respectively. Finally, an Agilent 6680A was used as a DC current source, and the differential of voltage between the taps was measured with a Keithley 2182A nano-voltmeter. All the instruments were connected via an IEEE-488 GPIB bus with in-house built LabVIEW controllers.

Five different YBCO coated conductors from three different manufacturers have been considered. Two different types of SP tapes have been tested, namely, 4 mm width SCS4050 tapes with top and bottom Cu stabilizer layers of ~ 0.02 mm thickness, and the 12 mm width stabilizer free SF12100 tapes [9]. In both cases, the YBCO layers are fabricated by metal organic chemical vapour deposition (MOCVD) over a buffer of heteroepitaxial layers deposited by sputtering, on a Hastelloy C-276 substrate of 0.1 mm thickness for the SF12100 tape, and 0.05 mm thickness for the SCS4050 tape, respectively. The YBCO layers ($\sim 1 \mu\text{m}$ thick) are then coated by a thin Ag layer of about $\sim 2 \mu\text{m}$ thick to provide electrical contact. For the AMSC samples [10], we have chosen the 4.4 mm width single YBCO layer tape or AMSC8700 tape with brass stabilizing layers of 0.15 mm thickness and also, the 12 mm width double layer YBCO tape or AMSC8612 tape with stainless-steel stabilizing layers of 0.075 mm thickness. In both AMSC tapes, the YBCO layers are deposited by MOCVD over a similar stack of heteroepitaxial layers (buffer) grown on a 0.075 mm thickness NiW alloy substrate. However, it is worth emphasizing that the AMSC8612 is a double layered HTS tape, i.e., the tape is composed by two stacks of YBCO/Buffer/NiW layers placed back-to-back in a single laminated package with the YBCO films coated by a $3 \mu\text{m}$ thick layer of Ag. Finally, the last of our five samples corresponds to the 5.8 mm width, 0.220 mm thickness, 2G-HTS tape provided by ShangHai SuperConductor (SHSC), also called ST-06-L tape [11], with similar substrate and buffer layer characteristics to the SP tapes, although with the YBCO layer deposited over a MgO template (buffer) by pulsed laser deposition (PVD) rather than MOCVD. A brief comparison of the technical features of the five 2G-HTS tapes aforementioned, is presented in table 1 for the ease of the reader.

3. Generalizing the in-field $I_c(B, \theta)$ function

For the selection of different 2G-HTS tapes shown in table 1, we have measured the profile of critical current I_c as a

Table 1. 2G-HTS tapes technical parameters^a.

2G-HTS tape	No. YBCO layers	h (mm)	w (mm)	I_c Max. (A)	n
SCS4050 [9]	1	0.055	4	114	30.5
SF12100 [9]	1	0.105	12	388	30.1
AMSC8700 [10]	1	0.150	4.4	98.2	36
AMSC8612 [10]	2	0.330	12.2	533	52.2
ST-06-L [11]	1	0.220	5.8	167	42.14

^a h refers to the overall thickness of the 2G-HTS tape, and w to its total width, respectively. The 12.2 mm width of the AMSC8612 sample includes the solder fillet layers at each side of the tape (~ 1.1 mm), i.e. with an effective YBCO layer of ~ 10 mm width.

function of the applied magnetic field, B , and its orientation, θ , in the maximum Lorentz force configuration, i.e., with the magnetic field applied perpendicular to the direction of the transport current. Therefore, the field angle θ is defined as 0° when the external magnetic field is parallel to the ab -plane of the YBCO tapes, as illustrated in figure 2. Therein, similar qualitative features of the in-field $I_c(B, \theta)$ function can be observed for the different 2G-HTS tapes that have been studied. In more detail, the maximum critical current at self-field, $I_c(0, \theta)$, i.e., without the influence of an external magnetic field has been measured for all samples and then, the magneto-angular study has been conducted for external magnetic fields of intensities $B = 50$ mT, 100 mT, 200 mT, 300 mT, and 400 mT, respectively. For the sake of comparison the results obtained at $\theta = 0$ ($B \parallel ab\text{-plane}$, $B \perp I$) and $\theta = \pm 90$ ($B \parallel c\text{-axis}$, $B \perp I$) are shown in table 2.

In the case of the SP samples, SCS4050 and SF12100, a more acute drop of the critical current is observed when the applied magnetic field is tilted towards $\pm 90^\circ$ from the ab -plane orientation of the HTS tape ($\theta = 0^\circ$), with a reduction of I_c of up to 67% at 400 mT for SCS4050, and 41% for SF12100, respectively. A similar drop pattern on the I_c is observed for the SHSC sample, ST-06-L, with a maximum reduction of the critical current of about 58% at 400 mT, and nearly the same percentage standard deviation when it is compared with the SCS4050 sample ($\Delta\sigma_{st} = 18.36(\text{ST-06-L}) - 18.04(\text{SCS4050}) = 0.32$). On the other hand, the AMSC samples show a more isotropic behaviour on the angular dependence of the I_c , with a maximum drop of 31% at 400 mT for AMSC8700 ($\sigma_{st} = 10.88$), and only a 19% for the double layered HTS tape or AMSC8612 ($\sigma_{st} = 6.16$) sample. Nevertheless, although the magneto-angular dependence of I_c on the AMSC samples is smaller than the observed one for the SP and SHSC samples, for comparable widths and structure, i.e., for the SCS4050 versus AMSC8700, a significant improvement of about 53% on the relative reduction of the I_c drop at moderately high fields (400 mT) is achieved. The SP samples at self-field conditions and for in-plane field ($\theta = 0$) attain greater critical current values. This is contrary to what happens when the external magnetic field is applied at $\theta = \pm 90^\circ$ and for intensities greater than 200 mT (see

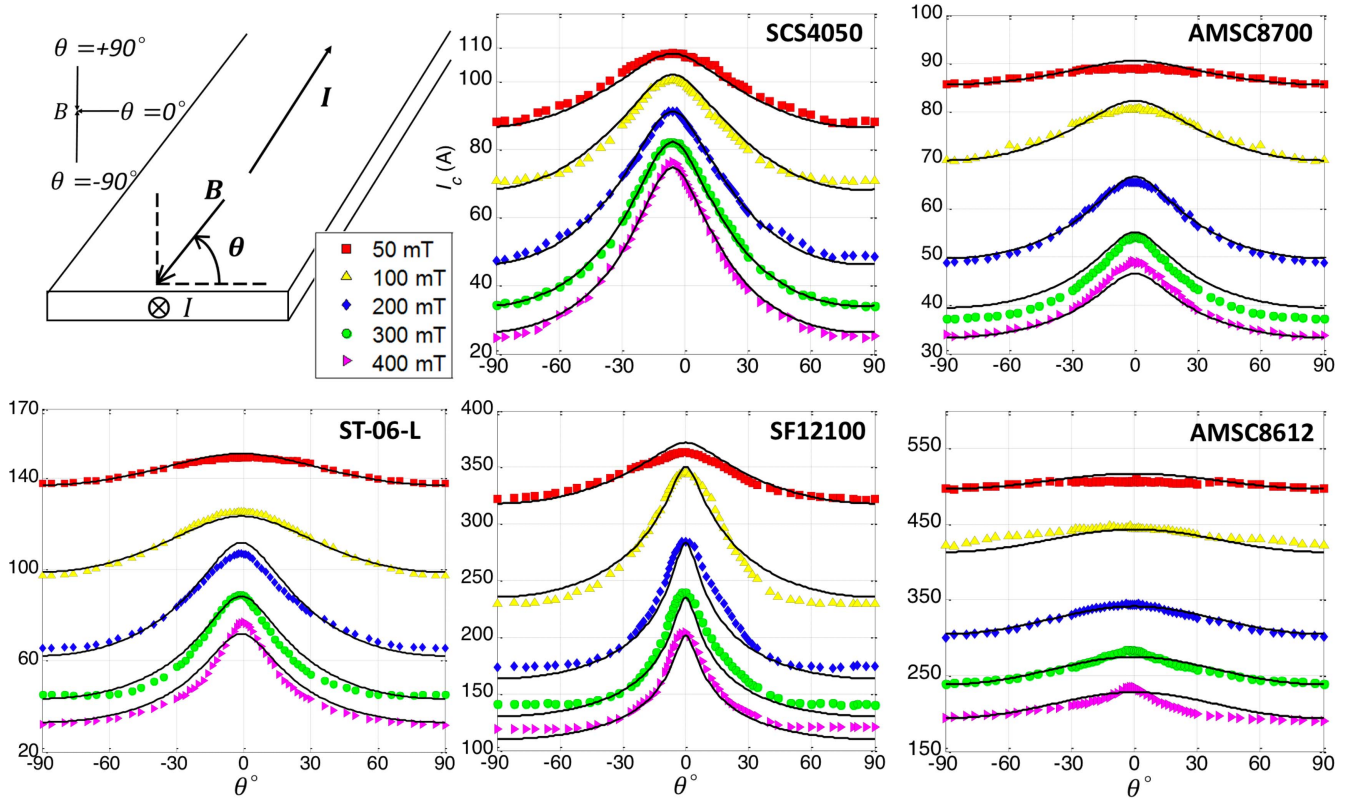


Figure 2. In-field magneto-angular dependence of the critical current I_c for the 2G-HTS tapes summarized in table 1. Solid symbols correspond to the experimental data acquired for an external magnetic field of 50 mT (red-squares), 100 mT (yellow-triangles), 200 mT (blue-diamonds), 300 mT (green-circles), and 400 mT (purple-triangles), respectively. Solid lines, correspond to the results obtained from our extended version of the Kim's model. As greater the applied magnetic field is, the lower the critical current. The orientation of the field angle and the direction of the transport current for all cases is illustrated in the top-left pane of the figure.

table 2). It is worth mentioning that for the 12 mm double layered YBCO tape (AMSC8612) a straightforward comparison with the SF12100 sample cannot be achieved. This is because each one of the two layers of YBCO that compose the AMSC8012 tape is inherently affected by the magnetic field created by its reciprocal layer. Thus, although the total I_c measured for this tape is the greatest, it is expected that assuming equal sharing of current, the I_c per layer has to be smaller than the one observed for the SF12100.

In order to generalize the previous results and allow an accurate prediction of the critical current in the maximum Lorentz force configuration, I_c , independently of the intensity of the applied magnetic flux density, $B \equiv |\mathbf{B}|$, and the angle θ , we have assumed that the critical current has to be moderated by the ratio between the effective mass of the charge carriers along the c -axis and the ab -plane of the YBCO layer, i.e., the electron mass anisotropy ratio $\gamma = m_c^*/m_{ab}^*$, as it was suggested by Blatter *et al*, in [13]. This anisotropy is caused by imperfect alignment of the ab -plane of each YBCO grain and the small fraction of grains with their ab -planes exactly parallel to the tape surface, which contributes to a large intergrain critical current in a magnetic field parallel to the tape, as it has been experimentally observed (see figure 2, $\theta = 0$). Thereby, we have extended the conventional Kim's model [12] taking into account Blatter's angular anisotropy factor, ε_θ , as

follows:

$$I_c(B, \theta) = I_{c0} \left(1 + \frac{\varepsilon_\theta B}{B_0(B)} \right)^{-\beta}, \quad (1)$$

with

$$\varepsilon_\theta = \sqrt{\gamma^{-1} \sin^2(\theta) + \cos^2(\theta)}. \quad (2)$$

In equation (1), $I_{c0} = I_c(0, \theta)$, i.e., the self-field critical current, and the empirical parameters introduced by Kim, B_0 and β , take into account the thermally activated flux-creep processes into specific samples. In fact, as the mechanism of flux creep is a thermally activated motion of bundles of flux lines, aided by the Lorentz force $\mathbf{J} \times \mathbf{B}$, over free energy barriers coming from the pinning effect of inhomogeneities, dislocations, strains, or other physical defects [16], in a first instance we have assumed that the parameter B_0 can be a function of B for the different samples considered in this study. Thus, by assuming the minimum number of empirical parameters that have been formulated within the Kim [12] and Anderson [16] flux creep theory, we have fixed the value of I_{c0} in equation (1) accordingly with our experimental observations (see table 1 or 2), and the parameters γ , $B_0(B)$, and β have been determined for the lowest mean absolute percentage deviation (MAPD) and analogously, for the lowest root-mean-square deviation (RMSD) of the experimental data,

with the minimum order function for $B_0(B)$. The latter fact is important because multiple guesses of the parameters γ and $B_0(B)$ could lead to similar MAPD and RMSD outcomes on specific tapes. Nevertheless, what is possible is to find a suitable expression for the different SC tapes along the minimization of the MAPD and RMSD values, by introducing the smaller possible number of unknown variables.

Thus, initial estimates for each one of the three free parameters in equation (1) have been assumed, and a similar iterative procedure to the one introduced in [17] has been used. We have reduced the ambiguity on the initial guesses by taking into consideration that the electron mass anisotropy ratio, γ , ranges between 1 for fully isotropic samples to about 25 for $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ grains with highly anisotropic conductivity [18]. Also, it has been already reported that the flux creep exponent β for YBCO samples is commonly lesser than 2 [14, 17]. Then, for a determined number of estimates, (γ, B_0, β) , the MAPD and RMSD of equation (1) with respect to the experimental measurements have been calculated for each one of these sets, and the overall number of resulting expressions minimized according to the following expressions:

$$\begin{aligned} & \text{Min}[\xi_{\text{MAPD}}] \\ &= \text{Min} \left[\sum_{k=1}^{N_B \cdot N_\theta} \frac{1}{N_B \cdot N_\theta} \left(\frac{|I_c^{(\gamma, B_0, \beta)} - I_c^{(\text{exp.})}|}{I_c^{(\text{exp.})}} \right)_{(k)} \right] \end{aligned} \quad (3)$$

and

$$\begin{aligned} & \text{Min}[\xi_{\text{RMSD}}] \\ &= \text{Min} \left[\sqrt{\frac{\sum_{k=1}^{N_B \cdot N_\theta} (|I_c^{(\gamma, B_0, \beta)} - I_c^{(\text{exp.})}|)_{(k)}^2}{N_B \cdot N_\theta}} \right] \end{aligned} \quad (4)$$

where the sub-index (k) indicates the subset of data taken from the N_θ angular measurements at the N_B different values of applied magnetic field, and $I_c^{(\gamma, B_0, \beta)}$ is the numerical value obtained during the minimization for the best fitting to the experimental results $I_c^{(\text{exp.})}$ by means of equations (1) and (2).

The optimal minimization process for the fitting of the (γ, B_0, β) parameters depends therefore on the number of estimates allocated to each one of these parameters, separately. For instance, if 20 different values are considered for each one of the parameters, γ , B_0 , and β , respectively, the minimization runs over a total of 8000 possible combinations for each N_B curve, and the percent deviations of the MAPD (ξ_{MAPD}) and RMSD (ξ_{RMSD}) have to be constrained to a maximum threshold in order to accept the solution. Thus, we have constrained the solution of equation (3) to satisfy the conditions $\xi_{\text{MAPD}} \leq \epsilon$ and $\xi_{\text{RMSD}} \leq \epsilon^2$ with $\epsilon = 3\%$ for all the N_B curves, simultaneously. As a result, less than 1% of the $8000 \times N_B$ suitable combinations for $I_c^{(\gamma, B_0, \beta)}$ survive for all N_θ measurements, and the results obtained for the minimum relative average between ξ_{MAPD} and ξ_{RMSD} are shown in table 3. Nevertheless, a univocal value for the parameter B_0 was only obtained for the SCS4050 and AMSC8612 samples,

this imposes an additional challenge for the determination of a singular $I_c(B, \theta)$ function for the 2G-HTS tapes: AMSC8700, SF12100, and ST-06-L. For instance, for the AMSC8700 sample, the lowest ξ_{MAPD} and ξ_{RMSD} values that have been obtained for a single definition of B_0 were 6.75 and 7.24, respectively, what does not satisfy the threshold condition for ξ_{MAPD} resulting in a deviation of more than 15% in the peak of current $I_c(B, 0^\circ)$.

Thus, in order to satisfy the tolerance conditions and reduce the deviation between the numerical results and the experimental observations, it is at this point that it is necessary to consider that the parameter B_0 depends on the magnitude of the applied magnetic field. Two essential conditions need to be satisfied during the derivation of this equation: First, the resulting expression has to be as simple as possible, i.e., by introducing the minimum number of free parameters that may allow the reproduction of the experimental results in even different coated conductors. Secondly, the resulting equation has to be physically consistent with the units in equation (1). The latter is important because the uncertainty on the physical nature of B_0 has led in the past to the formulation of cumbersome but yet accurate fitting expressions on specific batches of commercial tapes [14], that in some cases allows the adding of a significantly large number of physically unknown parameters with severe inconsistencies on the physical units [15]. However, we recognize that there is not a single way for finding this kind of expression, and different fitting equations can be obtained depending on the initial ansatz for the mathematical structure of the function $I_c(B, \theta)$. Therefore, finding an univocal solution for $I_c(B, \theta)$ is indeed cumbersome, and in general requires of the initial consideration of a larger number of variables during the minimization procedure.

However, returning to the root of the problem, equation (1) can be rewritten in a more general way as

$$I_c(f(B), \theta) = I_{c0}(1 + \varepsilon_\theta f(B))^{-\beta}, \quad (5)$$

with $f(B) = [(\zeta B + \delta)/B_0]^\alpha$, being the parameters ζ , δ , and α , new variables into the minimization procedure, such that in equations (3) and (4) the function of three variables $I_c^{(\gamma, B_0, \beta)} = I_c(B, \theta)$ in equation (1) is replaced by $I_c(f(B), \theta)$, in a first approach. The parameter δ , which is the only one with physical units, has been introduced for mathematical convenience as it allows a faster minimization of the powers α and β by compensating the impact of the highly nonlinear terms. Moreover, the minimization of the objective functions is conditioned to progressively achieve a reduction of δ , i.e., to $\delta_{t+1} < \delta$, for $\delta_{t+1} \geq 0$ in order to avoid the occurrence of complex singularities in I_c . Also it is possible to help further the minimization by imposing the conditions $\zeta \geq 1$, and $\alpha \geq 0$. Thereby, we have found that the function $f(B)$ is strikingly reduced to a very simple and elegant expression:

$$f(B) = \left(\frac{B}{B_0} \right)^\alpha, \quad (6)$$

with our final results presented in table 3, and showing an excellent agreement with the experimental results displayed in figure 2.

Table 2. In-field magneto-angular dependence of the critical current I_c for the 2G-HTS tapes summarized in table 1 for the external magnetic field intensities displayed in figure 2, and for the angles $\theta = 0$ ($B \parallel ab$ -plane, $B \perp I$) and $\theta = \pm 90^\circ$ ($B \parallel c$ -axis, $B \perp I$).

2G-HTS tape	YBCO w (mm)	$I_c(0, 0^\circ)$ (A)	$I_c(50 \text{ mT}, 0^\circ)$ (A)	$I_c(100 \text{ mT}, 0^\circ)$ (A)	$I_c(200 \text{ mT}, 0^\circ)$ (A)	$I_c(300 \text{ mT}, 0^\circ)$ (A)	$I_c(400 \text{ mT}, 0^\circ)$ (A)
SCS4050	4	114	108.2	100	91.26	82.12	76.2
AMSC8700	4.4	98.2	89.04	80.58	65.39	54.11	49.12
ST-06-L	5.8	167	149.2	125.3	106.9	88.95	77
SF12100	12	388	363.2	345.8	284.6	239.6	204.77
AMSC8612	12	533	509.5	448.2	344	283	235

2G-HTS	YBCO	$I_c(0, \pm 90^\circ)$	$I_c(50 \text{ mT}, \pm 90^\circ)$	$I_c(100 \text{ mT}, \pm 90^\circ)$	$I_c(200 \text{ mT}, \pm 90^\circ)$	$I_c(300 \text{ mT}, \pm 90^\circ)$	$I_c(400 \text{ mT}, \pm 90^\circ)$
SCS4050	4	114	88.19	71.04	48.66	33.91	25.17
AMSC8700	4.4	98.2	85.59	70.17	48.33	37.25	33.78
ST-06-L	5.8	167	137.7	97.33	65.34	44.99	31.86
SF12100	12	388	322	229.8	147.7	140.1	120.9
AMSC8612	12	533	496.7	422.3	301.2	238.6	190

Despite SCS4050 and AMSC8612 samples have different width and consequently different self-field critical current density [$I_c(0, 0^\circ)$ in table 2], they possess very close fitting parameters: B_0 , α and β . Therefore, the magneto-angular dependence of the SCS4050 and AMSC8612 samples is rather similar, although the electron mass anisotropy ratio of SCS4050 is about 4 times greater than in the AMSC8612 sample ($\gamma_{\text{SCS4050}}/\gamma_{\text{AMSC8612}} = 4.016$). This fact explains the high increase on the critical current density when the magnetic field in the Lorentz-force configuration is applied parallel to the surface of the ab -planes of the SCS4050 tape, i.e., $\theta = 0$ at figure 2, a phenomenon which is nearly unseen at 50 mT with the AMSC samples. A similar comparison can be made between the SF12100 and the AMSC8700 samples ($\gamma_{\text{SF12100}}/\gamma_{\text{AMSC8700}} = 3.33$). Thus, further to the general expression that we have found for the magneto-angular in-field function $I_c(B, \theta)$, from our previous analysis it is possible to conclude that the contribution due to the charge carriers along the c -axis of the YBCO tapes manufactured by SP is greater than in those manufactured by AMSC or SHSC, a phenomenon that is increased when the YBCO tape is not coated by Cu stabilizer layers. Nevertheless, the sample manufactured by SHSC (ST-06-L) has shown a stronger dependence of the mass anisotropy factor γ on the intensity of the applied magnetic field. In this case it was not possible to find a solution capable of satisfying the threshold values for ξ_{MAPD} and ξ_{RMSD} , simultaneously. Thus, although these threshold values can be adjusted, it is worth mentioning that for the best of the cases we have found that $\gamma \sim 4.35$ for $\xi_{\text{MAPD}} \sim 3.5\%$ and $\xi_{\text{MAPD}} \sim 4.2\%$. However, it produces an acute deviation of the peak values of the critical current density at $\theta = 0^\circ$, particularly noticeable at lower magnetic fields ($B \lesssim 100$ mT), with the experimental results being overestimated by more than a 10% difference. It could be seen maybe as a small difference for the reader, but it has to be noticed from table 2 that the percentage differences between the self-field critical current $I_c(0, 0^\circ)$ and the peaks values of the critical current at 50 mT and 100 mT are of $\sim 10.7\%$ and $\sim 25\%$. Consequently, by accepting the

Table 3. Fitting parameters found after the minimization procedure of equation (5) is performed, it leading to equation (6) and the matching of the experimental results displayed in figure 2.

2G-tape	B_0 (mT)	α	β	γ	ξ_{MAPD}	ξ_{RMSD}
SCS4050 [9]	240	1	1.50	5.02	1.57	1.21
SF12100 [9]	44.83	2.4	0.24	13.32	2.93	8.25
AMSC8700 [10]	72.75	2.4	0.25	4.00	1.89	1.64
AMSC8612 [10]	280	1	1.30	1.25	1.27	5.91
ST-06-L [11]	91.03	1.7	0.58	4.17 ^a	2.91	2.51

^a For applied magnetic fields lower than 200 mT, the obtained electron mass anisotropy ratio for the ST-06-L sample and under the same conditions displayed in this table corresponds to $\gamma = 2.08$. Thus, the theoretical curves shown in the ST-06-L pane of figure 2 for $B_{\text{ext}} = 50$ and 100 mT are obtained with $\gamma = 2.08$, otherwise the results therein are for $\gamma = 4.17$.

aforementioned condition, the actual overestimation of the increase in the critical current density in the in-field configuration results in a deviation of more than 20% from the self-field critical current value. Thus this simplified approach is not acceptable. Consequently, we conclude that there is a weaker influence of the charge carriers along the c -axis of the YBCO layer in the ST-06-L tape for magnetic fields lower than 200 mT, i.e., with $\gamma = 2.08$, than what is observed for greater magnetic fields where the minimum γ has been found to be double (see table 3).

4. Conclusion

In this paper, we have presented a thorough study of the magneto-angular dependence of the in-field critical current function in the so called Lorentz configuration, $I_c(B, \theta)$ with $B \perp I$, of five different samples of commercially available 2G-HTS tapes. The experimental results have been obtained for external magnetic fields of up to 400 mT, and range from

0° to $\pm 90^\circ$, i.e., with B parallel to the ab -plane of the YBCO tape, towards the perpendicularity conditions where B is parallel to the c -axis. In general, we have selected 2G-HTS tapes with broad differences regarding their width, fabrication process, and laminar structure (materials composition), in order to seek for a universal function that may describe the $I_c(B, \theta)$ behaviour of different commercial tapes from the numerical minimization of the objective functions introduced in equations (3) and (4).

Two samples of 12 mm YBCO-width tapes have been considered, each fabricated by a different company, namely, the SF12100 tape by SuperPower Inc. [9], and the double layered YBCO tape AMS8612 by American Superconductor (AMSC) [10]. Analogously, measurements have been performed for the 4 mm width SCS4050 tape fabricated by SuperPower, the 4.4 mm width AMSC8700 tape by AMSC. Finally, the ST-06-L tape produced by Shanghai Superconductor Technology Co., Ltd. (SHSC) [11] has been considered. It is shown that, in spite of the apparently strong differences between these tapes, at liquid nitrogen temperature the magneto-angular dependence of the in-field critical current can be described by a universal function, $I_c(f(B), \theta)$, with a power law field dependence dominated by the Kim's factor B/B_0 (see equations (5) and (6)), and the angular dependence moderated by the electron mass anisotropy ratio in equation (2). A similar power law dependence with the magnetic field has been recently observed by Barth *et al* [19], for fields of up to 60% of the irreversibility field and at temperatures lower than 77 K. In fact, an exponential law for the temperature dependence has been already determined by these authors, which in the future could be used as the initial estimates at the outset of our general approach.

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References

- [1] Ruiz H S, Zhang X and Coombs T A 2015 *IEEE Trans. Appl. Supercond.* **25** 5601405
- [2] Tixador P 2010 *Physica C* **470** 971–9
- [3] Huang Z, Ruiz H S, Zhai Y, Geng J, Shen B and Coombs T A 2016 *IEEE Trans. Appl. Supercond.* **26** 55202105
- [4] Baghdadi M, Ruiz H S and Coombs T 2014 *Appl. Phys. Lett.* **104** 232602
- [5] Vojenčiak M, Šouc J, Ceballos J, Gömöry F, Klinčok B, Pardo E and Grilli F 2006 *Supercond. Sci. Technol.* **19** 397
- [6] Campbell A M and Evetts J E 1972 *Adv. Phys.* **21** 199
- [7] Badía-Majós A, Lopez C and Ruiz H S 2009 *Phys. Rev. B* **80** 144509
- [8] Ruiz H S, Lopez C and Badía-Majós A 2011 *Phys. Rev. B* **83** 014506
- [9] SuperPower® 2G HTS Wire. Technical information available at www.superpower-inc.com/content/2g-hts-wire
- [10] American Superconductor, AMSC Amperium® HTS wire. Technical information available at www.amsc.com/solutions-products/hts_wire.html
- [11] Shanghai Superconductor Technology Co. Ltda. 2G HTS strip. Technical information available at <http://shsctec.com/en/index.asp>
- [12] Kim Y, Hempstead C and Strnad A 1962 *Phys. Rev. Lett.* **9** 306
- [13] Blatter G, Feigel'Man M, Geshkenbein V, Larkin A and Vinokur V M 1994 *Rev. Mod. Phys.* **66** 1125
- [14] Grilli F, Sirois F, Zerméño V M and Vojenčiak M 2014 *IEEE Trans. Appl. Supercond.* **24** 8000508
- [15] Hu D, Ainslie M D, Raine M J, Hampshire D P and Zou J 2016 *IEEE Trans. Appl. Supercond.* **26** 6600906
- [16] Anderson P W 1962 *Phys. Rev. Lett.* **9** 309
- [17] Rostila L, Lehtonen J, Mikkonen R, Šouc J, Seiler E, Melišek T and Vojenčiak M 2007 *Supercond. Sci. Technol.* **20** 1097
- [18] Harshman D R, Schneemeyer L F, Waszczak J V, Aeppli G, Ansaldo E J and Williams D L 1989 *Phys. Rev. B* **39** 851
- [19] Senatore C, Barth C, Bonura M, Kulich M and Mondonico G 2016 *Supercond. Sci. Technol.* **29** 014002