

Modulation of the $\text{Bi}^{3+} 6s^2$ Lone Pair State in Perovskites for High-Mobility p-Type Oxide Semiconductors

Jueli Shi, Ethan A. Rubinstein, Weiwei Li, Jiaye Zhang, Ye Yang, Tien-Lin Lee, Changdong Qin, Pengfei Yan, Judith L. MacManus-Driscoll, David O. Scanlon,* and Kelvin H.L. Zhang*

Oxide semiconductors are key materials in many technologies from flat-panel displays, solar cells to transparent electronics. However, many potential applications are hindered by the lack of high mobility p-type oxide semiconductors due to the localized O-2p derived valence band (VB) structure. In this work, the VB structure modulation is reported for perovskite Ba_2BiMO_6 ($M = \text{Bi}, \text{Nb}, \text{Ta}$) via the Bi $6s^2$ lone pair state to achieve p-type oxide semiconductors with high hole mobility up to $21 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$, and optical bandgaps widely varying from 1.5 to 3.2 eV. Pulsed laser deposition is used to grow high quality epitaxial thin films. Synergistic combination of hard x-ray photoemission, x-ray absorption spectroscopies, and density functional theory calculations are used to gain insight into the electronic structure of Ba_2BiMO_6 . The high mobility is attributed to the highly dispersive VB edges contributed from the strong coupling of Bi 6s with O 2p at the top of VB that lead to low hole effective masses ($0.4\text{--}0.7 m_e$). Large variation in bandgaps results from the change in the energy positions of unoccupied Bi 6s orbital or Nb/Ta d orbitals that form the bottom of conduction band. P–N junction diode constructed with p-type $\text{Ba}_2\text{BiTaO}_6$ and n-type Nb doped SrTiO_3 exhibits high rectifying ratio of 1.3×10^4 at $\pm 3 \text{ V}$, showing great potential in fabricating high-quality devices. This work provides deep insight into the electronic structure of Bi^{3+} based perovskites and guides the development of new p-type oxide semiconductors.


1. Introduction

Oxide semiconductors are being extensively used as key materials in modern optoelectronics technologies including flat panel displays, solar cells, light emitting diodes, and transparent electronics.^[1] Oxides such as ZnO, In_2O_3 , Ga_2O_3 , and SnO_2 are typical wide bandgap n-type semiconductors, in which the filled oxygen $2p^6$ orbitals form the valence band (VB), and the spatially extended metal s orbitals form the conduction band (CB), giving rise to a dispersive CB with a high electron mobility. In contrast, the development of high mobility p-type oxide semiconductors remains challenging.^[2] The lack of p-type oxide semiconductors severely hinders the development of many crucial technologies, e.g., p-channel thin film transistors (TFT) and CMOS inverters for high-resolution energy-saving displays; p-type semiconductor layers for efficient hole transport in photovoltaics and visible-light active photocathodes for solar water splitting.^[2a,3]

The difficulty in realizing high mobility p-type oxide semiconductors arises from

J. Shi, J. Zhang, Y. Yang, K. H. Zhang
State Key Laboratory of Physical Chemistry of Solid Surfaces
Collaborative Innovation Center of Chemistry for Energy Materials
College of Chemistry and Chemical Engineering
Xiamen University
Xiamen 361005, China
E-mail: Kelvinzhang@xmu.edu.cn
E. A. Rubinstein, D. O. Scanlon
Department of Chemistry and Thomas Young Centre
University College London
London WC1H 0AJ, UK
E-mail: d.scanlon@ucl.ac.uk

W. Li
MIIT Key Laboratory of Aerospace Information Materials and Physics
College of Science
Nanjing University of Aeronautics and Astronautics
Nanjing 211106, China
W. Li, J. L. MacManus-Driscoll
Department of Materials Science and Metallurgy
University of Cambridge
27 Charles Babbage Road, Cambridge CB3 0FS, UK
T.-L. Lee
Diamond Light Source Ltd.
Harwell Science and Innovation Campus
Didcot OX11 0DE, UK
C. Qin, P. Yan
Beijing Key Laboratory of Microstructure and Property of Solids
Faculty of Materials and Manufacturing
Beijing University of Technology
Beijing 100124, China

 The ORCID identification number(s) for the author(s) of this article can be found under <https://doi.org/10.1002/adv.202104141>

© 2021 The Authors. Advanced Science published by Wiley-VCH GmbH. This is an open access article under the terms of the Creative Commons Attribution License, which permits use, distribution and reproduction in any medium, provided the original work is properly cited.

DOI: 10.1002/adv.202104141

the electronic structure of oxides: the localized O 2p-derived VB maximum (VBM) leading to difficulty in introducing shallow acceptors and large hole effective masses.^[2a,4] A strategy to mitigate the low mobility problem is to use the hybridization of O 2p with partially occupied d orbitals of transition metals (TM) to modulate band dispersion at the top of VB.^[5] TM oxides with closed-shell Cu 3d¹⁰ (CuMO₂, M = Al, Cr, etc.), quasi-closed shell d⁶ (ZnM₂O₄, M = Co, Rh, Ir) and d³ configurations (LaCrO₃) have been explored as p-type semiconductors.^[5,6] However, these oxides still show limited improvement in the hole mobility (<5 cm² V⁻¹ s⁻¹) or instability issue.^[7] An alternative approach is to use the ns² lone pair orbitals from heavy post-transition metal cations (e.g., Sn²⁺, Bi³⁺, Pb²⁺) to interact with O 2p, forming the filled antibonding states at the top of VB. The spatially extended s orbitals work more effectively to delocalize the hole states at the VB edge than TM d orbitals. This leads to more dispersive VBM and much smaller hole effective masses for high p-type mobility. Following this concept, SnO is one of the most promising p-type oxides owing to the dispersive Sn 5s O 2p derived VB. High hole mobility up to 30 cm² V⁻¹ s⁻¹ have been reported for SnO bulk polycrystals and ≈10 cm² V⁻¹ s⁻¹ for epitaxial thin films.^[8] SnO-based p-type TFTs and CMOS inverters were also investigated. However, phase instability of SnO still presents significant technical challenges for thin-film synthesis and device integration.^[8b,9] The presence of Pb 6s² lone pair electrons in halide perovskites is also the key factor for their appealing optoelectronic properties as photovoltaic materials.^[10]

Bi³⁺ based oxides are also receiving increasing attentions as p-type oxide semiconductors. Many Bi³⁺ based oxides show p-type conductivity owing to the native Bi vacancies or aliovalent doping.^[11] The involvement of Bi³⁺ 6s² lone pair states at VB could also provide a dispersive VBM for hole transportation, leading to high p-type mobility, as demonstrated in the cases of BiVO₄ and p-type BiOI.^[12] To unleash the potential of s-orbital chemistry of Bi³⁺ for p-type oxide semiconductors, we turn to Bi-based perovskites. The perovskites have the advantage of structural and compositional flexibility to allow design of novel multifunctional materials via doping or alloying. BaBiO₃ has previously received much attention, because of its superconductivity upon doping with Pb or K.^[13] BaBiO₃ actually has the structure of Ba₂Bi³⁺Bi⁵⁺O₆, due to the charge disproportionation of 2Bi⁴⁺ → Bi³⁺ + Bi⁵⁺. The Bi 6s² lone pair state arising from Bi³⁺ could hybridize with O 2p to form the top of VB, of potential to provide a high p-type mobility, whereas the empty Bi 6s⁰ from Bi⁵⁺ form the bottom of CB. Although no consensus has been reached on the exact values of its bandgap (varying from 0.3 to 2.0 eV),^[14] several previous works reported that BaBiO₃ is a small bandgap semiconductor. On the other hand, as a result of the structural flexibility of perovskite, the Bi⁵⁺ could be replaced with other pentavalent cations such as Nb⁵⁺ or Ta⁵⁺ to form Ba₂Bi³⁺M⁵⁺O₆. The bandgaps could be tuned to large values, because the bottom of CB would be then replaced by higher energy level d orbitals of the pentavalent cations, whereas the Bi 6s-O 2p derived top of the VB remains the same. Indeed, Bhatia et al. reported that Ba₂BiTaO₆ has an ultra-wide bandgap of 4.5 eV and K⁺ doped Ba₂BiTaO₆ polycrystalline pellets showed a large hole mobility of up to 30 cm² V⁻¹ s⁻¹.^[15] The Bi 6s²-derived VB electronic structure and tuneable bandgaps make the perovskite Ba₂BiMO₆ (M = Bi, Nb, Ta) a very attractive material system as p-type oxide

semiconductors.^[14a,16] However, there is still lack of investigations of the optical and electronic properties on this material system, and even the nature and values of bandgaps remain elusive.

In this article, we present the modulation of the VB and CB structure of Ba₂BiMO₆ (M = Bi, Nb, Ta) via Bi 6s² state to achieve high p-type mobility up to 21 cm² V⁻¹ s⁻¹ and optical bandgaps varying widely from 1.5, 2.8 to 3.2 eV. A set of high-quality Ba₂BiMO₆ epitaxial thin films were grown by pulsed laser deposition (PLD). Hard X-ray photoemission spectroscopy (HAXPES), X-ray absorption spectroscopy (XAS) in conjunction with density functional theory (DFT) calculations are used to reveal insights into the electronic structures of Ba₂BiMO₆ responsible for their appealing properties. We show that the Bi 6s² state interacts strongly with O 2p to form an s-p antibonding state at the top of VB, leading to highly dispersive VB edges and thus low hole effective masses (0.4–0.7 m_e) for the high hole mobility in Ba₂BiMO₆. The large variation of the bandgaps results from the change in the energy positions of the unoccupied s orbital of Bi⁵⁺ or d orbitals of Nb/Ta that form the bottom of the CB (**Figure 1**). Furthermore, our detailed study on the electronic structure also resolves discrepancies existing in the literature regarding the nature of the bandgaps and optical properties of Ba₂BiMO₆. Finally, the application potential of Ba₂BiMO₆ for optoelectronic devices were demonstrated by the fabrication of Ba₂BiTaO₆ – Nb doped SrTiO₃ p–n junction diodes.

2. Results and Discussion

2.1. Thin Film Growth and Crystal Structures

Ba₂BiMO₆ (M = Bi, Nb, Ta) epitaxial films with thickness of ≈40 nm were grown on (001) oriented SrTiO₃ (STO) and MgO substrates using PLD from respective targets. BaBiO₃ (BBO) possesses a distorted perovskite structure with a pseudo-cubic parameter of 4.35 Å. The lattice parameters slightly decrease for Ba₂BiNbO₆ (BBNO) (≈4.31 Å) and Ba₂BiTaO₆ (BBTO) (≈4.28 Å), because of the smaller ionic radii of Nb⁵⁺ and Ta⁵⁺ than that of Bi⁵⁺ (see schematic model in **Figure 1**). There is a lattice mismatch of ≈10% for Ba₂BiMO₆ grown on STO (3.905 Å), and ≈2% on MgO (4.212 Å). X-ray diffraction (XRD) θ–2θ out-of-plane scans in **Figure 2a** and **Figure S1** (Supporting Information) and reciprocal space mapping (RSM) in **Figure S2** (Supporting Information) indicate the epitaxial growth of Ba₂BiMO₆ thin films grown on both SrTiO₃ and MgO substrates. **Figure 2b** and **Table S1** (Supporting Information) summarize the in-plane (IP) and out-of-plane (OP) lattice parameters of the films extracted from XRD. In general, the films grown on both substrates show the same crystalline structure and the lattice parameters decrease from Bi, Nb to Ta. The IP and OP lattice parameters are close to their respective bulk values, indicating the epitaxial strain resulting from lattice mismatch with the substrate is nearly relaxed.

Cross-sectional scanning transmission electron microscopy (STEM) measurements were performed to further examine the interfacial structure and epitaxial relationship. A uniform film over a large lateral length scale is evident from a low-magnification high-angle annular dark-field (HAADF)-STEM image (**Figure S3a**, Supporting Information). **Figure 2c** shows an atomic-resolution HAADF-STEM image at the interface region of

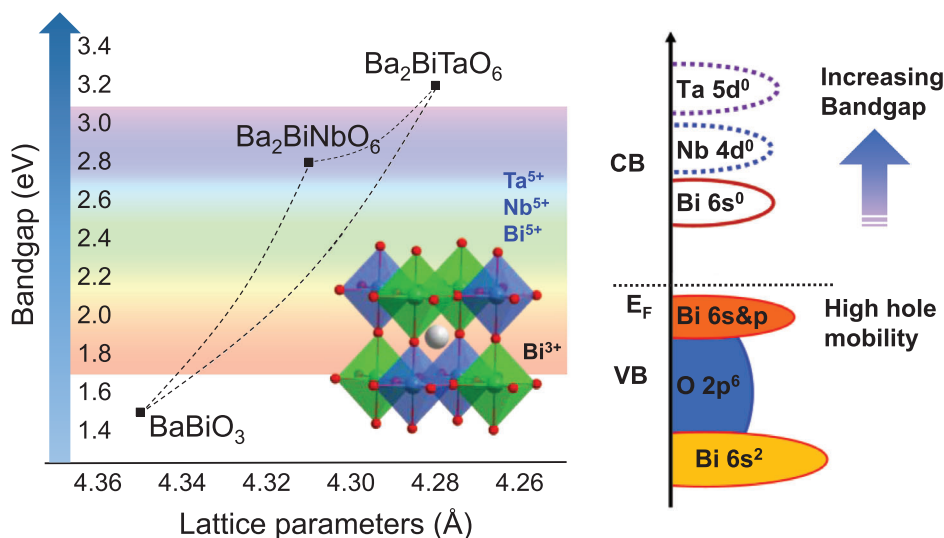


Figure 1. Schematic illustration of structure and bandgap modulation of perovskites Ba_2BiMO_6 ($M = \text{Bi, Nb, Ta}$).

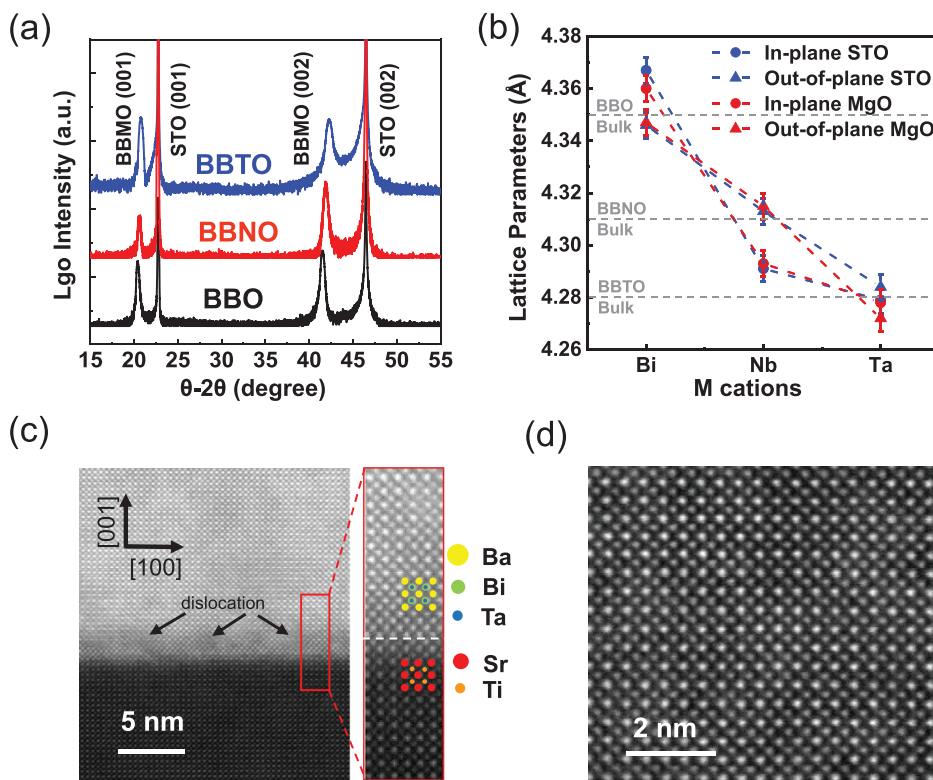


Figure 2. The structural and optical properties of Ba_2BiMO_6 thin films. a) X-ray diffraction (XRD) of Ba_2BiMO_6 thin films grown on STO (001) substrates; b) in-plane and out-of-plane lattice parameters extracted from reciprocal space mapping (RSM) of Ba_2BiMO_6 thin film grown on STO (001) and MgO (001) substrates; c) HAADF-STEM image of the interface of $\text{Ba}_2\text{BiTaO}_6$ and STO , and zoom-in into the lattice region marked by the red rectangle; d) HAADF-STEM image of the bulk region of $\text{Ba}_2\text{BiTaO}_6$.

BBTO/STO viewed down to the $[100]$ zone axis direction. Due to the large lattice mismatch, dislocations are observed in the interfacial region between BBTO and STO . However, with the increase of thin film thickness, the epitaxial strain is gradually relaxed and high crystallinity and lattice ordering are observed in the bulk region of BBTO , as shown in Figure 2d.

2.2. Optical and Transport Properties

The optical properties of the films were measured by UV-vis-NIR absorption spectroscopy. Because of the small bandgap of STO (3.2 eV) which limits the spectrum in the UV region, we used films grown on MgO ($E_g = 7.8$ eV) for optical measurement.

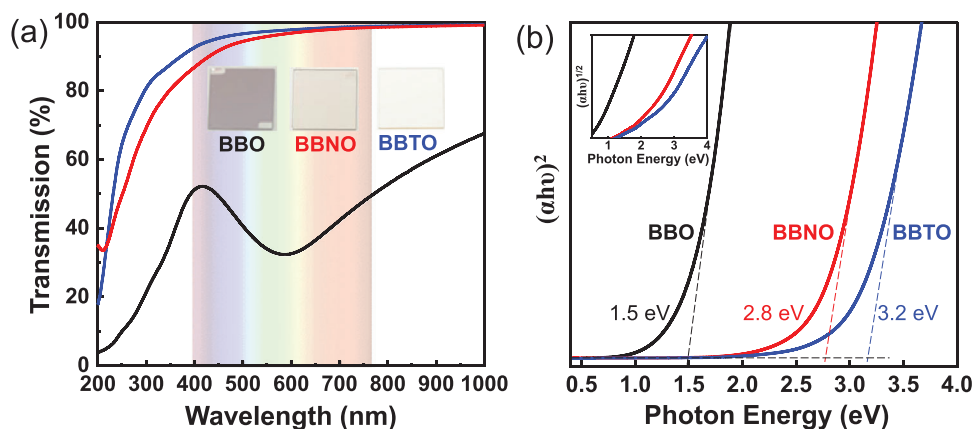


Figure 3. a) Optical transmittance spectra and photographs (inset) of Ba₂BiMO₆ films grown on MgO (001) substrates; b) $(\alpha h\nu)^2$ plot and $(\alpha h\nu)^{1/2}$ plot (inset) of Ba₂BiMO₆ films grown on MgO (001) substrates.

Figure 3a shows the optical transmittance of 40 nm Ba₂BiMO₆ films. BBO films show relatively low transmission of 30–40% in the visible light region. After substitution of Nb and Ta, the films show high transparency of >85% for BBNO and > 90% for BBTO from visible light towards infra-red region. The high transparency in the visible light region makes BBNO and BBTO promising p-type oxide semiconductors for transparent electronics.

To elucidate the bandgap values of Ba₂BiMO₆, we further analyzed the absorption spectra using Tauc plot (Figure 3b). The extracted absorption coefficients of the films are shown in Figure S4 in the Supporting Information. Based on the slow rising of the absorption onset in the infrared light region and band structure calculations, we determined that BBO has an indirect bandgap of 0.7 eV (inset in Figure 3b showing the Tauc plot for indirect bandgap). A direct bandgap of 1.5 eV was measured. Also, a high absorption coefficient up to $3 \times 10^5 \text{ cm}^{-1}$ in the visible light region was determined, which makes BBO an attractive p-type perovskite material for solar energy harvesting.^[14a,b,17] The absorption from the infrared to visible region in BBO originates from the optical transition from the occupied antibonding state of Bi 6s-O 2p formed at the top of VB to the unoccupied Bi 6s state at bottom of CB, which will be discussed in detail in Section 2.3. For BBNO and BBTO, the absorption band disappears and there is a gradually increased bandgap to 2.8 and 3.2 eV, which could be assigned to the substitution of unoccupied Nb 4d and Ta 5d orbitals as discussed later in Section 2.3. To further verify our concept of bandgap modulation, we also grew epitaxial films of 50% Ta⁵⁺ substituted BBTO (Ba₂Bi_{1.5}Ta_{0.5}O₆) and measured the optical properties (shown in Figure S5 in the Supporting Information). The direct bandgap of Ba₂Bi_{1.5}Ta_{0.5}O₆ slightly increased to 1.7 eV and the indirect bandgap increased to 1.0 eV. This demonstrates that the bandgap values could be continuously tuned by simply modulating the cation ratio of Bi and M in Ba₂BiMO₆.

We found the undoped Ba₂BiMO₆ in the form of both thin films and polycrystalline pellets are quite insulating, probably due to the low carrier concentration. To measure the transport properties, we used K⁺ to dope the Ba₂BiMO₆ thin films and pellets and conducted Hall measurement at room temperature and detailed electrical properties are summarized in Table S2 in

the Supporting Information. A high hole mobility of $11.3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ was obtained for 5% K doped BBO (K_{0.05}Ba_{0.95}BiO₃) thin films, and 14.1 and 21.0 $\text{cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ for 20% K doped BBNO and BBTO polycrystalline pellets respectively, corroborating the success of using a Bi³⁺ 6s² modulated VBM to achieve high mobility p-type oxides. We also compare the properties of Ba₂BiMO₆ with other p-type oxide semiconductors in Table 1. It is obvious that Ba₂BiMO₆ outperforms most of the other p-type oxides in terms of mobility. The high hole mobility, together with the continuously tunable bandgaps from 1.5 to 3.2 eV make Ba₂BiMO₆ promising materials as solar energy absorber in PV and also for transparent p-type semiconducting layers for p-channel TFTs and P–N heterojunctions.

2.3. Electronic Structure

A combination of HAXPES, XAS, and DFT provide crucial insights into the electronic density of states (DOS). **Figure 4a** shows the VB spectra excited with photon energies of 2200 and 5930 eV. The VB spectra provide information about the occupied DOS weighted by the photoionization cross-sections (PICs) of the contributing orbitals. The comparison of VB spectra excited by two photon energies allows identification of the contribution of the Bi 6s² state, because the PIC of the s orbital decreases much more slowly than those of O 2p or d orbitals with increasing photon energy. As shown in Figure 4a, the three oxides show very similar VB spectra. The presence of the Bi 6s state can be clearly observed at the top of VB in the energy region of 0.5–2.5 eV (Region I). Spectral features in the energy region of 2.5–7 eV (Region II) are mainly from O 2p states. Significant contributions from Bi 6s states are also seen in Region III (9–11 eV) at the bottom of VB.

Figure 4b shows the O K-edge XAS spectra. The O K-edge XAS probes the transition from O 1s core electrons to the unoccupied states with O 2p characters hybridized with unoccupied Bi 6s/6p or d orbitals of Nb/Ta. Therefore, the O K-edge XAS can be qualitatively related to the unoccupied DOS at the CB.^[18] Based on DFT DOS calculations, the feature centered at $\approx 529 \text{ eV}$ for BBO in Figure 4b is assigned to the unoccupied Bi 6s⁰ orbital hybridized with O 2p, forming the bottom of the CB of BBO.

Table 1. Comparison between Ba_2BiMO_6 with other p-type oxide semiconductors in terms of bandgap, transparency and mobility.

Materials	Bandgap / [eV]	Transparency / [T%]	Mobility / [$\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$]	Hole effective mass / [m_e]	Ref.
BaBiO_3	1.5	40	11.3	0.399	This work
$\text{Ba}_2\text{BiNbO}_6$	2.8	85	14.1	0.713	This work
$\text{Ba}_2\text{BiTaO}_6$	3.2	90	21.0	0.590	This work
SnO	2.8	50–70	1.4–10.8	0.64	[30]
Cu_2O	2.17	47–60	90–256	0.24	[31]
CuGaO_2	3.6	80	0.23	2.23	[32]
SrCu_2O_2	3.25	60	0.46	0.79	[33]
CuBi_2O_4	1.8	50–85	0.02	2.29	[11a]
NiO	3.4	87	<0.05	–	[34]
BiOI	2.04	–	–	1.9	[12b,35]

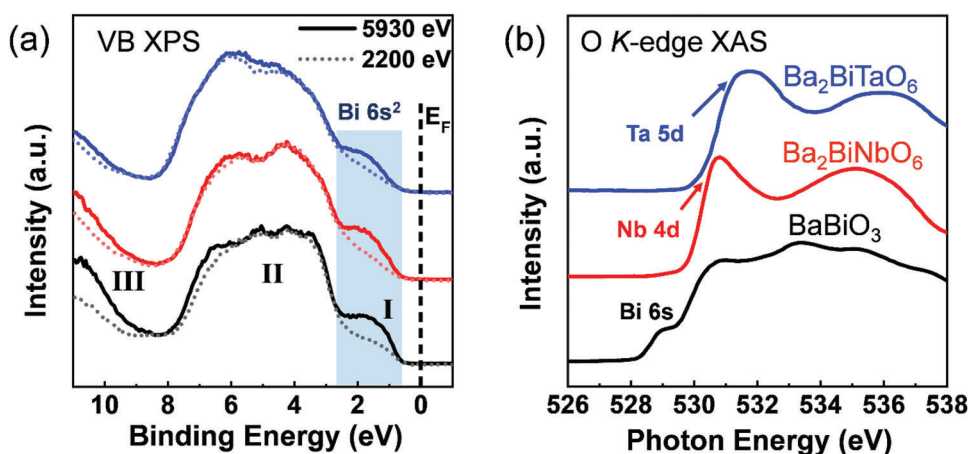


Figure 4. a) Valence band spectra of BaBiO_3 (lines in black), $\text{Ba}_2\text{BiNbO}_6$ (lines in red) and $\text{Ba}_2\text{BiTaO}_6$ (lines in blue) excited with photon energy of 5930 eV (solid) and 2200 eV (dotted), three spectral regions are marked as I (0.5–2.5 eV), II (2.5–7 eV), and III (9–11 eV); b) corresponding O K-edge XAS spectra, indicating the information about the conduction band.

For BBNO and BBTO, the low energy lying $\text{Bi } 6s^0$ is replaced by higher energy $\text{Nb } 4d^0$ and $\text{Ta } 5d^0$ orbitals centered at 531 eV for BBNO and 531.7 eV for BBTO. This observation agrees well with the trend of increasing bandgaps from Bi, Nb to Ta.

We further performed hybrid DFT calculations with the explicit addition of spin–orbit coupling (HSE06 + SOC) to calculate the electronic DOS near the E_F . HSE06 + SOC has been proven to more accurately calculate the electronic structure of materials with strong spin–orbit coupling such as Bi based compounds.^[19] The calculated lattice parameters and bond lengths were minimally changed by geometry optimization (Tables S3 and S4, Supporting Information) and the calculated bandgaps match well with our experimental values (Table S5, Supporting Information). **Figure 5a–c** plots the calculated electronic DOS for three oxides (insets showing the zoomed band-edge region from –2.5 to 4.5 eV). The DOS with a wide energy range from –11 to 6 eV is shown in Figure S6 in the Supporting Information. Overall, the calculated DOS well reproduce the features observed in the experimental spectra of the VB photoemission and O K-edge absorption. The presence of Bi 6s states with strong hybridization with O 2p at the top of VB is further confirmed by the partial DOS in the energy region from –2 to 0 eV for all three oxides. The DOS

in the energy region from –6 to –2 eV (region II in Figure 4b) are mainly derived from O 2p with some contributions from Bi 6p or Nb/Ta d orbitals. The DOS also confirm the presence of Bi 6s states at the bottom of the VB, shown in the energy region from –11 to –9 eV (region III in Figure 4b). The hybridization between Bi^{3+} 6s and 6p orbitals with O 2p orbitals in Ba_2BiMO_6 could be described via the revised lone pair (RLP) model proposed by Walsh and Payne et al.^[12a,20] the Bi^{3+} lone pair $6s^2$ states strongly hybridized with O 2p, forming Bi 6s – O 2p bonding states at the bottom of VB. The high-energy antibonding (Bi 6s – O 2p)* states further interact with unoccupied Bi 6p states due to lattice distortion, resulting in asymmetric occupied bonding states at the top of VB. The bottom of the CB of BBO is mostly derived from empty Bi 6s and 6p hybridized with O 2p. The low energy position of the empty Bi 6s results in the small indirect bandgap of 0.7 eV for BBO. On the other hand, for BBNO and BBTO, the low energy Bi 6s that formed the bottom of CB is replaced by the Nb 4d state (Figure 5b) or the Ta 5d state (Figure 5c) located at higher energy, leading to a considerable increase in the bandgap values, i.e., 2.8 eV for BBNO and 3.2 eV for BBTO. Meanwhile, the top of the VB remains nearly unchanged, because the occupied Bi $6s^2$ from Bi^{3+} is retained. The amount of increase in the

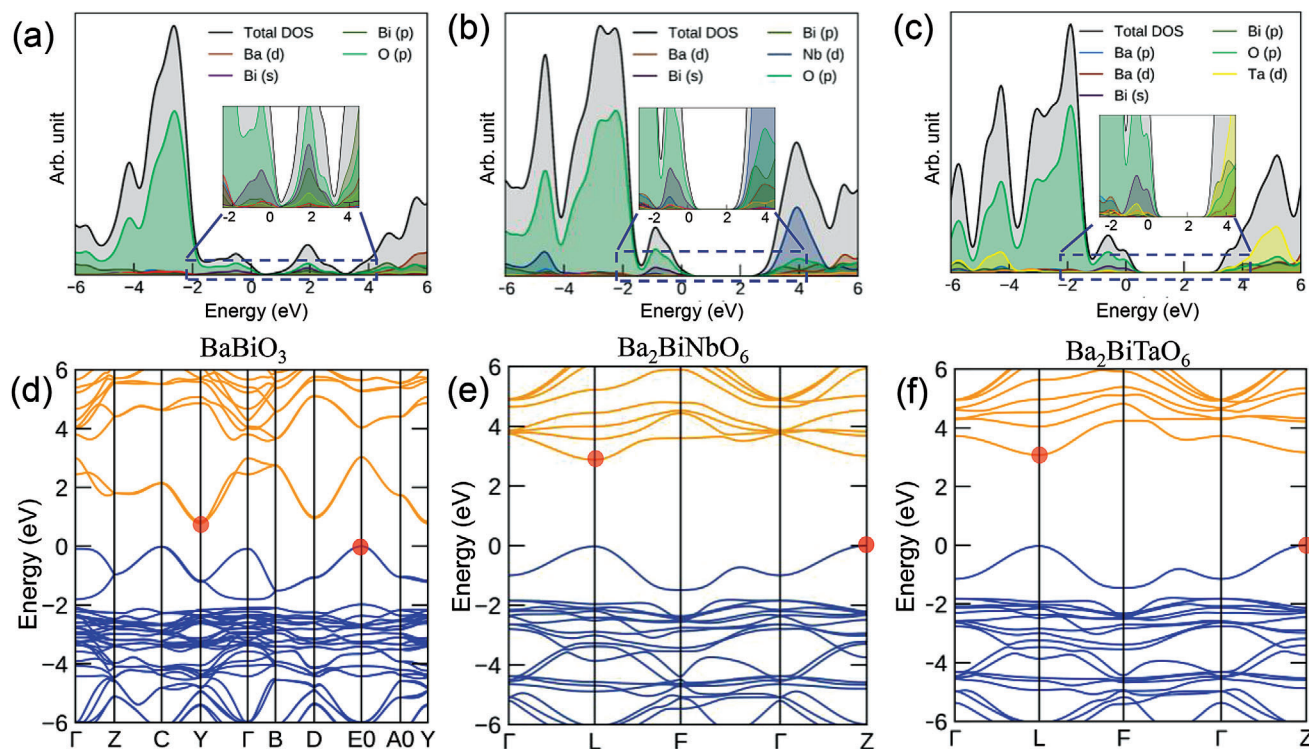


Figure 5. HSE06+SOC calculated a–c) DOSs and d–f) band structures for BaBiO₃, Ba₂BiNbO₆, and Ba₂BiTaO₆, respectively. Insets in (a)–(c) show the zoomed band edge area from –2.5 to 4.5 eV. Valence band maximum (VBM) and conduction band minimum (CBM) points are marked with red point in (d)–(f).

bandgap is in agreement with the shift of photon energies for the features associated with Nb 4d⁰ and Ta 5d⁰ orbitals in O K-edge XAS spectra.

It should be noted that different bandgap values for BBO have been reported in the literatures from indirect values of 0.3,^[21] 0.84 eV,^[21] to direct values of 1.4,^[21] 2.0 eV.^[14b] This inconsistency in the reported values of BBO bandgap might be attributed to the different computational methods or sample characteristics (e.g., polycrystalline powders or single crystalline). Our determined bandgap of 3.2 eV for BBTO is much smaller than the value of >4.5 eV reported by Bhatia et al.^[15a] However, considering the bandgaps of Ta₂O₅ (3.8 eV) and KTaO₃ (3.6 eV) whose VB are of mainly O 2p and CB of Ta 5d states, it is reasonable to believe that the bandgap of BBTO should be smaller than 3.6 eV, because the involvement of the Bi 6s – O 2p antibonding states in BBTO would raise the VB edge to a higher energy position compared with O 2p-dominated VB in Ta₂O₅ and KTaO₃. In general, we believe that our synergistic combination of optical absorption, XPS/XAS and DFT calculations has allowed a more accurately determination of the nature and values of bandgaps for BBO and BBTO.

2.4. Band Structure and Effective Mass

The calculated band structures are shown in Figure 5d–f. All three Ba₂BiMO₆ exhibit dispersive VBM in the energy region of

Table 2. The parabolic fitted effective mass of electrons and holes at different k-points in the Brillion zone for BaBiO₃, Ba₂BiNbO₆ and Ba₂BiTaO₆.

	BaBiO ₃		Ba ₂ BiNbO ₆		Ba ₂ BiTaO ₆	
m_{hole}^*/m_e	0.40	E0	0.71	Z	0.59	Z
m_{elec}^*/m_e	0.20	Y	0.41	L	0.41	L

–2 to 0 eV, providing a facile pathway for hole transport. The carrier effective mass m^* is linked to mobility (μ) and scattering time (τ), via $\mu = \frac{e\tau}{m^*}$. Thus, a smaller m^* would result in a larger μ . The parabolic-curve fitted effective mass of electrons and holes at different k-points in the Brillion zone for BBTO, BBNO, and BBTO are summarized in Table 2. As shown in Figure 5d, BBO exhibits both dispersive CBM and VBM, with a small electron effective mass (m_{elec}^*) of 0.20 m_e and hole effective mass (m_{hole}^*) of 0.40 m_e . The result also indicates that BBO has an indirect bandgap of 0.78 eV and direct bandgap of 1.92 eV, in agreement with the optical absorption result (see Figure S4 in the Supporting Information). The indirect bandgap of BBO results from the optical transition between the VB at k-point E0 and the CB at Y (labeled in Figure 5d). The substitution of Bi⁵⁺ with Nb⁵⁺ and Ta⁵⁺ not only considerably increases the bandgap values of BBNO and BBTO, but also change the bandgaps into pseudo-direct ones (where direct and indirect gap values show small differences) because of the dramatic modification of the

band structure at the CB edges. Their CB edges are less dispersive than that of BBO, due to the more localized d orbitals of Nb/Ta than Bi 6s. The m_{elec}^* is 0.413 m_e for BBNO and 0.406 m_e for BBTO. On the other hand, the dispersive VB edges are still maintained in BBNO and BBTO, because of the same Bi 6s²-O 2p antibonding states remaining at the top of VB. The m_{hole}^* is 0.590 m_e for BBTO and 0.713 m_e for BBNO. The increase in m_{hole}^* compared to that of BBO is due to a decreased DOS of Bi 6s at the top of VB after the substitution of Nb and Ta, which slightly weakens the s-orbital mediation of band dispersion. Overall, the presence of Bi 6s² states successfully mediates the band dispersion at the VBM, leading to small m_{hole}^* and the observed high hole mobility.

2.5. Discussion

Our research reveals the origin of an observed dispersive VB and resulted high hole mobility of Ba₂BiMO₆ perovskites by investigating their bandgap modulation and electronic structure. This would provide a viable route towards the development of high-performance p-type oxide semiconductors using occupied ns states from p-block cations. As demonstrated for Ba₂BiMO₆, the bandgap values of Bi³⁺ oxides can be modulated by choosing appropriate substitutional cations without sacrificing the dispersive 6s²-modulated VB. Following this idea, other p-block oxides with ns² states at the VB could also be promising p-type semiconductors with high mobility, such as the recently reported Sn²⁺ based oxides Sn₂Nb₂O₇ and Sn₂Ta₂O₇.^[22] Pb²⁺-based oxides are also attractive choices due the similar 6s²-derived VB. However, the toxicity intrinsic to Pb-based compounds limit their further application in daily life. Additionally, the structural stability and compositional flexibility of perovskites allow us to modulate bandgap values for different applications. For example, BBO with a relatively small bandgap of 1.5 eV could be used as photocathode for solar water splitting, while the transparent BBNO and BBTO could work as p-type channel materials for transparent TFTs or hole transport layers for photovoltaics. Bi-excess Ba₂Bi_xNb_{2-x}O₆ and Ba₂Bi_xTa_{2-x}O₆ (1 < x ≤ 2) are also ideal platforms for developing high-performance photocatalysts, arising from the joint advantages of lone pair s² cations as chromophores, catalytically active metal d⁰ cations, and adaptable bandgap values all together enabling efficient solar water splitting. This has been demonstrated in the examples of BiVO₄ and Ba₂Bi_xNb_{2-x}O₆.^[16,23] Furthermore, Ba₂BiMO₆ could be combined with other n-type perovskite oxide materials to design novel multifunctional devices. Several n-type perovskite oxides have been developed, such as Nb-doped SrTiO₃ (NbSTO) and La-doped BaSnO₃ (LBSO). To give an example of this, we constructed a 60 nm thick BBTO on n-type NbSTO p-n junction and measured its current-voltage (*I*-*V*) characteristics, as shown in Figure 6. This diode shows a distinct rectifying behavior by applying both reverse and forward bias. The rectifying ratio is about 1.3 × 10⁴ at ±3 V, which is a high value compared to those of other oxide-based p-n diodes.^[24] Our development of perovskite Ba₂BiMO₆ would guide the rational design of p-type semiconductor towards efficient carrier transport, adjustable compositions and variable bandgaps, and further promote the development of high-performance oxide optoelectronics.

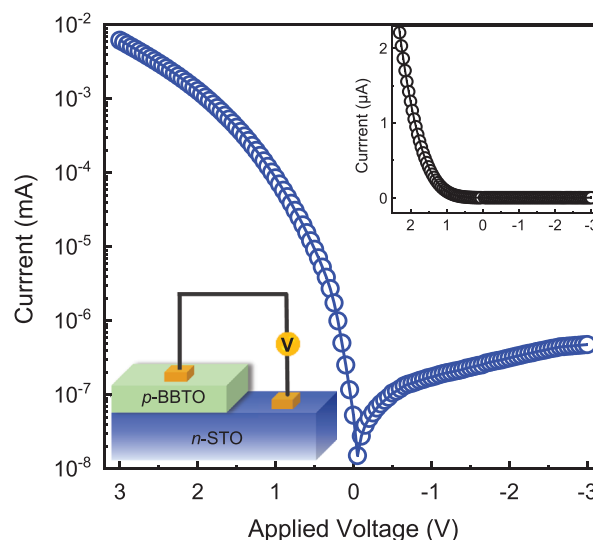


Figure 6. Semilogarithmic current versus voltage characteristics of the BBTO/NbSTO p-n heterojunction measured at room temperature; the inset shows the corresponding *I*-*V* curve in linear scale, and a schematic diagram for device measurement is also shown.

3. Conclusions

In this work, we present experimental and computational investigation on the bandgap modulation and electronic structure of perovskite oxides Ba₂BiMO₆. The bandgap of Ba₂BiMO₆ could be gradually tuned in a wide range from 1.5, 2.8 to 3.2 eV by simply changing the *M* cations and their component proportion. Using HAXPES, the existences of Bi³⁺ 6s² are experimentally observed at VBM in all three Ba₂BiMO₆. The involvement of Bi³⁺ 6s² states which help to maintain a dispersive valence band and thus give smaller hole effective masses compared with other oxides, leading to high hole mobilities up to 21 cm² V⁻¹ s⁻¹. By combining optical absorption results, and experimental band edge structures from XPS, XAS, and DFT calculations, an accurate determination of the electronic structure and bandgap values of Ba₂BiMO₆ is presented. The enlargement of bandgap values after the substitution of Nb and Ta at the *M* site, which is attributed to the involvement of *d* orbitals at the CBM, helps BBNO and BBTO to exhibit high optical transparency (>85%) from visible light to infra-red region. Finally, the potential of Ba₂BiMO₆ for the fabrication of all-perovskite oxide devices is further confirmed by demonstrating a BBTO-NbSTO p-n junction diode with high rectifying ratio up to 1.3 × 10⁴ at ±3 V. Our combined spectroscopic and computational methods, especially the use of varied photon energy for the probing of *s* states, could be further extended to the investigation of other p-block oxides with *s* lone pair electrons. Our results add to the current understanding of the electronic structure of Bi-based perovskite oxides and provide guidance for the development of p-type oxide semiconductors with high mobilities.

4. Experimental Section

Epitaxial BaBiO₃, Ba₂BiNbO₆, and Ba₂BiTaO₆ thin films were grown on double-side polished (001)-oriented SrTiO₃ substrates and (001)-oriented

MgO substrates by PLD from respective targets. Laser ablation was performed at a repetition rate of 1 Hz and an energy density of 1.0 J cm^{-2} with a 248 nm KrF excimer laser. Films were grown at a substrate temperature of 550 °C. The oxygen partial pressure during growth was 1 Pa. The polycrystalline-pellets of 20% K^+ doped $\text{Ba}_2\text{BiNbO}_6$ and $\text{Ba}_2\text{BiTaO}_6$ were prepared using a solid-state synthesis method. Briefly, stoichiometric amounts of K_2CO_3 (99.98%, Alfa Aesar), BaCO_3 (99.95%, Alfa Aesar), Bi_2O_3 (99.999%, Alfa Aesar), Nb_2O_5 (99.985%, Alfa Aesar), and Ta_2O_5 (99.993%, Alfa Aesar) were thoroughly ground with agate mortar and pestle. The mixture was firstly pressed into a pellet and heat treated in a furnace at 750 °C for 12 h. Then, the pellet was reground and heated again in a furnace at 950 °C for 12 h. The crystal structure and epitaxial relationship in the films was determined by high-resolution XRD using a PANalytical four-circle diffractometer in θ - 2θ scans and reciprocal space maps (RSM) mode. Cross-sectional STEM specimens were prepared with an FEI Helios dual-beam focused ion beam/scanning electron microscope using a standard lift-out approach. The FIB-prepared samples were examined using an FEI Titan80-300 STEM microscope with a probe spherical aberration corrector at 300 kV for high-angle annular dark-field (HAADF) STEM imaging. STEM-EDS were performed on a probe aberration-corrected JEOL JEM-ARM200CF at 200 kV.

Optical absorption measurements were performed at room temperature using a Cary 5000 spectrophotometer in the photon energy range of 0.5–6.0 eV. Carrier mobility measurements were performed at room temperature using a Semishare Hall effect measurement system using the van der Pauw method at a magnetic field of 0.5 T. For sample preparation, the powder samples of 20% K^+ doped $\text{Ba}_2\text{BiNbO}_6$ and $\text{Ba}_2\text{BiTaO}_6$ were firstly pressed into pellets and sintered in a furnace at 950 °C for 12 h. The as-sintered pellets with density of $\approx 5 \text{ g cm}^{-3}$ was then cut into square size ($\approx 10 \times 10 \text{ mm}$) and thickness of $\approx 1 \text{ mm}$ using diamond saw. The electrical contacts are made at the four corners of the samples, using magnetron sputtered Au electrodes for epitaxial thin films and Ag-ink covered Ga-In eutectics (Sigma-Aldrich) for pellet samples. The I - V characteristics of the BBTO-NbSTO heterojunction diodes were measured using a Keithley 2400 multifunctional digital source meter.

Hard XPS (HAXPES) measurements using photon energies of 5930 and 2200 eV and soft XAS measurements were all performed at the I09 beamline of the Diamond Light Source, located at the Harwell Science and Innovation Campus in Didcot, UK. HAXPES spectra were energy-resolved and measured using a VG Scienta EW4000 high-energy electron energy analyzer with a 56° acceptance angle. The overall energy resolution for XPS measurement was about 0.25 eV. XAS measurements were performed in total electron yield (TEY) mode. The energy resolution for O K-edge XAS was close to 0.1 eV.

All DFT calculations were performed using the Vienna ab initio Simulation Package (VASP),^[25] which uses the Projector Augmented Wave (PAW) method^[26] to model interactions between core and valence electrons. The Heyd, Scuseria, and Ernzerhof screened hybrid functional (HSE06),^[27] which truncates the 25% added Hartree Fock exchange used in the hybrid PBE0 functional developed by Adamo and Barone^[28] for the reduction of computational cost, was used for all calculations. The k -point mesh density and plane wave basis set energy cut-off were converged to within 1 and 2 meV Atom^{-1} respectively. Geometry optimization was performed for the three structures under HSE06 to a maximum interatomic force on each atom of 0.01 eV \AA^{-1} . Spin-orbit coupling was included for electronic structure calculations.

Statistical Analysis: The analysis and calibration of HAXPES data were performed using DAWN Science (Version 2.14.0, Diamond Light Source) and SpecsLab Prodigy (SPECS Surface Nano Analysis GmbH). All HAXPES data were calibrated using standard Au 4f core-level spectra. Analysis and plotting of DFT calculated electronic density of states and band structures were performed with the sumo python package.^[29] Effective masses were calculated by parabolic fit of the curvature at the band edges.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

Acknowledgements

J.-L.S. acknowledges support from Collaborative Innovation Center of Chemistry for Energy Materials (iChEM), Xiamen. K.H.L.Z. is grateful for funding support from the National Natural Science Foundation of China (Grant No. 21872116 and 22075232). D.O.S. acknowledges membership of the UK's HEC Materials Chemistry Consortium, which is funded by the EPSRC (EP/L000202, EP/R029431). D.O.S. also acknowledges the ARCHER UK National Supercomputing Service (www.archer.ac.uk) and the UK Materials and Molecular Modelling (MMM) Hub (Thomas | EP/P020194 & Young | EP/T022213), and the UCL Kathleen and Grace High Performance Computing Facilities for calculations. J.L.M.-D. and W.-W.L. acknowledge support from the EPSRC grants EP/L011700/1, EP/N004272/1, EP/P027032/1. J.L.M.-D. also acknowledges the Royal Academy of Engineering Chair in Emerging Technologies Grant CiET1819-24. W.-W.L. acknowledges support from the National Natural Science Foundation of China (Grant No. 52102177), the National Natural Science Foundation of Jiangsu Province (Grant No. BK20210313), and Top-notch Academic Programs Project of Jiangsu Higher Education Institutions (TAPP). W.-W.L. also acknowledges support from the Jiangsu Specially-Appointed Professor Program. The authors acknowledge technical support from LinkPhysics Corporation. The authors acknowledge Diamond Light Source for providing beam time and facilities at beamline I09 under proposal SI24219.

Conflict of Interest

The authors declare no conflict of interest.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

DFT calculations, electronic structures, p-type oxide semiconductors, photoluminescence spectroscopy

Received: September 16, 2021

Revised: November 12, 2021

Published online:

- [1] a) X. Yu, T. J. Marks, A. Facchetti, *Nat. Mater.* **2016**, *15*, 383; b) K. Nomura, H. Ohta, K. Ueda, T. Kamiya, M. Hirano, H. Hosono, *Science* **2003**, *300*, 1269; c) K. Nomura, H. Ohta, A. Takagi, T. Kamiya, M. Hirano, H. Hosono, *Nature* **2004**, *432*, 488; d) J. Shi, J. Zhang, L. Yang, M. Qu, D. C. Qi, K. H. L. Zhang, *Adv. Mater.* **2021**, *33*, 2006230; e) J. Zhang, J. Shi, D.-C. Qi, L. Chen, K. H. L. Zhang, *APL Mater.* **2020**, *8*, 020906; f) D. K. Lee, D. Lee, M. A. Lumley, K.-S. Choi, *Chem. Soc. Rev.* **2019**, *48*, 2126; g) W. Li, J. Shi, K. H. L. Zhang, J. L. MacManus-Driscoll, *Mater. Horiz.* **2020**, *7*, 2832.
- [2] a) K. H. L. Zhang, K. Xi, M. G. Blamire, R. G. Egdell, *J. Phys.: Condens. Matter* **2016**, *28*, 383002; b) Z. Wang, P. K. Nayak, J. A. Caraveo-Frescas, H. N. Alshareef, *Adv. Mater.* **2016**, *28*, 3831.
- [3] K. Sivula, R. van de Krol, *Nat. Rev. Mater.* **2016**, *1*, 15010; b) E. Fortunato, D. Ginley, H. Hosono, D. C. Paine, *MRS Bull.* **2007**, *32*, 242.
- [4] D. O. Scanlon, G. W. Watson, *J. Mater. Chem.* **2012**, *22*, 25236.
- [5] H. Kawazoe, M. Yasukawa, H. Hyodo, M. Kurita, H. Yanagi, H. Hosono, *Nature* **1997**, *389*, 939.

- [6] a) R. Nagarajan, A. D. Draeseke, A. W. Sleight, J. Tate, *J. Appl. Phys.* **2001**, 89, 8022; b) H. Yanagi, T. Hase, S. Ibuki, K. Ueda, H. Hosono, *Appl. Phys. Lett.* **2001**, 78, 1583; c) X. C. Huang, J. Y. Zhang, M. Wu, S. Zhang, H. Y. Xiao, W. Q. Han, T. L. Lee, A. Tadich, D. C. Qi, L. Qiao, L. Chen, K. H. L. Zhang, *Phys. Rev. B* **2019**, 100, 115301; d) M. J. Wahila, Z. W. Lebens-Higgins, A. J. Jackson, D. O. Scanlon, T.-L. Lee, J. Zhang, K. H. L. Zhang, L. F. J. Piper, *Phys. Rev. B* **2019**, <https://doi.org/10.1103/physrevb.100.085126>; e) K. H. L. Zhang, Y. Du, A. Papadogianni, O. Bierwagen, S. Sallis, L. F. J. Piper, M. E. Bowden, V. Shutthanandan, P. V. Sushko, S. A. Chambers, *Adv. Mater.* **2015**, 27, 5191.
- [7] T. Arnold, D. J. Payne, A. Bourlange, J. P. Hu, R. G. Egdell, L. F. J. Piper, L. Colakerol, A. De Masi, P.-A. Glans, T. Learmonth, K. E. Smith, J. Guo, D. O. Scanlon, A. Walsh, B. J. Morgan, G. W. Watson, *Phys. Rev. B* **2009**, <https://doi.org/10.1103/physrevb.79.075102>; H. Şahin, S. Cahangirov, M. Topsakal, E. Bekaroglu, E. Akturk, R. T. Senger, S. Ciraci, *Phys. Rev. B* **2009**, <https://doi.org/10.1103/physrevb.80.155453>; D. O. Scanlon, A. Walsh, B. J. Morgan, G. W. Watson, D. J. Payne, R. G. Egdell, *Phys. Rev. B* **2009**, <https://doi.org/10.1103/physrevb.79.035101>; d) D. O. Scanlon, K. G. Godinho, B. J. Morgan, G. W. Watson, *J. Chem. Phys.* **2010**, 132, 024707; e) D. O. Scanlon, G. W. Watson, *J. Phys. Chem. Lett.* **2010**, 1, 3195; f) D. O. Scanlon, G. W. Watson, *J. Mater. Chem.* **2011**, 21, 3655; g) D. O. Scanlon, G. W. Watson, *Phys. Chem. Chem. Phys.* **2011**, 13, 9667.
- [8] a) S. A. Miller, P. Gorai, U. Aydemir, T. O. Mason, V. Stevanović, E. S. Toberer, G. J. Snyder, *J. Mater. Chem. C* **2017**, 5, 8854; b) M. Minohara, N. Kikuchi, Y. Yoshida, H. Kumigashira, Y. Aiura, *J. Mater. Chem. C* **2019**, 7, 6332.
- [9] M. Minohara, A. Samizo, N. Kikuchi, K. K. Bando, Y. Yoshida, Y. Aiura, *J. Phys. Chem. C* **2020**, 124, 1755.
- [10] a) C. Wu, Q. Zhang, G. Liu, Z. Zhang, D. Wang, B. Qu, Z. Chen, L. Xiao, *Adv. Energy Mater.* **2020**, 10, 1902496; b) Q. Sun, J. Wang, W.-J. Yin, Y. Yan, *Adv. Mater.* **2018**, 30, 1705901.
- [11] a) F. E. Oropeza, N. Y. Dzade, A. Pons-Martí, Z. Yang, K. H. L. Zhang, N. H. De Leeuw, E. J. M. Hensen, J. P. Hofmann, *J. Phys. Chem. C* **2020**, 124, 22416; b) N. Masó, A. R. West, *Chem. Mater.* **2012**, 24, 2127; c) A. Tsurumaki, H. Yamada, A. Sawa, *Adv. Funct. Mater.* **2012**, 22, 1040.
- [12] a) D. J. Payne, M. D. M. Robinson, R. G. Egdell, A. Walsh, J. McNulty, K. E. Smith, L. F. J. Piper, *Appl. Phys. Lett.* **2011**, 98, 212110; b) R. L. Z. Hoye, L. C. Lee, R. C. Kurchin, T. N. Huq, K. H. L. Zhang, M. Sponseller, L. Nienhaus, R. E. Brandt, J. Jean, J. A. Polizzotti, A. Kursumović, M. G. Bawendi, V. Bulović, V. Stevanović, T. Buonassisi, J. L. Macmanus-Driscoll, *Adv. Mater.* **2017**, 29, 1702176.
- [13] a) D. G. Hinks, B. Dabrowski, J. D. Jorgensen, A. W. Mitchell, D. R. Richards, S. Pei, D. Shi, *Nature* **1988**, 333, 836; b) L. F. Mattheiss, D. R. Hamann, *Phys. Rev. Lett.* **1988**, 60, 2681; c) T. Nishio, J. Ahmad, H. Uwe, *Phys. Rev. Lett.* **2005**, 95, 176403; d) R. Nourafkan, F. Marsiglio, G. Kotliar, *Phys. Rev. Lett.* **2012**, 109, 017001; e) Z. Li, G. Antonius, M. Wu, F. H. da Jornada, S. G. Louie, *Phys. Rev. Lett.* **2019**, 122, 186402.
- [14] a) J. Tang, Z. Zou, J. Ye, *J. Phys. Chem. C* **2007**, 111, 12779; b) K. H. Kim, C. U. Jung, T. W. Noh, S. C. Kim, *Phys. Rev. B* **1997**, 55, 15393; c) M. E. Kozlov, X. Ji, H. Minami, H. Uwe, *Phys. Rev. B* **1997**, 56, 12211; d) S. M. Hasanuzzaman, K. Iwano, K. Nasu, *J. Phys. Soc. Jpn.* **1999**, 68, 1376.
- [15] a) A. Bhatia, G. Hautier, T. Nilgianskul, A. Miglio, J. Sun, H. J. Kim, K. H. Kim, S. Chen, G.-M. Rignanese, X. Gonze, J. Suntivich, *Chem. Mater.* **2016**, 28, 30; b) D. Dahliah, G.-M. Rignanese, G. Hautier, *J. Mater. Chem. C* **2020**, 8, 9352.
- [16] J. Ge, W.-J. Yin, Y. Yan, *Chem. Mater.* **2018**, 30, 1017.
- [17] a) J. F. Federici, B. I. Greene, E. H. Hartford, E. S. Hellman, *Phys. Rev. B* **1990**, 42, 923; b) H. Minami, *Phys. C* **1994**, 235–240, 1151.
- [18] a) F. M. F. De Groot, M. Grioni, J. C. Fuggle, J. Ghijsen, G. A. Sawatzky, H. Petersen, *Phys. Rev. B* **1989**, 40, 5715; b) F. Frati, M. O. J. Y. Hunault, F. M. F. De Groot, *Chem. Rev.* **2020**, 120, 4056.
- [19] a) C. N. Savory, A. Walsh, D. O. Scanlon, *ACS Energy Lett.* **2016**, 1, 949; b) B. Weng, Z. Xiao, W. Meng, C. R. Grice, T. Poudel, X. Deng, Y. Yan, *Adv. Energy Mater.* **2017**, 7, 1602260; c) B. Yan, M. Jansen, C. Felser, *Nat. Phys.* **2013**, 9, 709.
- [20] D. J. Payne, R. G. Egdell, A. Walsh, G. W. Watson, J. Guo, P.-A. Glans, T. Learmonth, K. E. Smith, *Phys. Rev. Lett.* **2006**, <https://doi.org/10.1103/physrevlett.96.157403>; b) A. Walsh, Y. Yan, M. N. Huda, M. M. Al-Jassim, S.-H. Wei, *Chem. Mater.* **2009**, 21, 547; c) A. Walsh, D. J. Payne, R. G. Egdell, G. W. Watson, *Chem. Soc. Rev.* **2011**, 40, 4455.
- [21] A. I. Liechtenstein, I. I. Mazin, C. O. Rodriguez, O. Jepsen, O. K. Andersen, M. Methfessel, *Phys. Rev. B* **1991**, 44, 5388.
- [22] a) Y. Aiura, K. Ozawa, I. Hase, K. Bando, H. Haga, H. Kawanaka, A. Samizo, N. Kikuchi, K. Mase, *J. Phys. Chem. C* **2017**, 121, 9480; b) N. Kikuchi, A. Samizo, S. Ikeda, Y. Aiura, K. Mibu, K. Nishio, *Phys. Rev. Mater.* **2017**, 1, 021601; c) I. Hase, T. Yanagisawa, Y. Aiura, K. Kawashima, *Phys. Rev. Lett.* **2018**, <https://doi.org/10.1103/physrevlett.120.196401>
- [23] I. D. Sharp, J. K. Cooper, F. M. Toma, R. Buonsanti, *ACS Energy Lett.* **2017**, 2, 139.
- [24] a) H. Yang, H. M. Luo, H. Wang, I. O. Usov, N. A. Suvorova, M. Jain, D. M. Feldmann, P. C. Dowden, R. F. Depaula, Q. X. Jia, *Appl. Phys. Lett.* **2008**, 92, 102113; b) J. Zhang, S. Han, W. Luo, S. Xiang, J. Zou, F. E. Oropeza, M. Gu, K. H. L. Zhang, *Appl. Phys. Lett.* **2018**, 112, 171605; c) J. Zhang, S. Han, M. Cui, X. Xu, W. Li, H. Xu, C. Jin, M. Gu, L. Chen, K. H. L. Zhang, *ACS Appl. Electron. Mater.* **2020**, 2, 456.
- [25] a) G. Kresse, J. Furthmüller, *Comput. Mater. Sci.* **1996**, 6, 15; b) G. Kresse, J. Furthmüller, *Phys. Rev. B* **1996**, 54, 11169.
- [26] P. E. Blöchl, *Phys. Rev. B* **1994**, 50, 17953.
- [27] A. V. Krukau, O. A. Vydrov, A. F. Izmaylov, G. E. Scuseria, *J. Chem. Phys.* **2006**, 125, 224106.
- [28] C. Adamo, V. Barone, *J. Chem. Phys.* **1999**, 110, 6158.
- [29] A. M. Ganose, A. J. Jackson, D. O. Scanlon, *J. Open Source Softw.* **2018**, 3, 717.
- [30] Y. Hu, J. Hwang, Y. Lee, P. Conlin, D. G. Schlom, S. Datta, K. Cho, *J. Appl. Phys.* **2019**, 126, 185701.
- [31] E. Ruiz, S. Alvarez, P. Alemany, R. A. Evarestov, *Phys. Rev. B* **1997**, 56, 7189.
- [32] T. F. T. Cerqueira, S. Lin, M. Amsler, S. Goedecker, S. Botti, M. A. L. Marques, *Chem. Mater.* **2015**, 27, 4562.
- [33] K. G. Godinho, J. J. Carey, B. J. Morgan, D. O. Scanlon, G. W. Watson, *J. Mater. Chem.* **2010**, 20, 1086.
- [34] J. Y. Zhang, W. W. Li, R. L. Z. Hoye, J. L. MacManus-Driscoll, M. Budde, O. Bierwagen, L. Wang, Y. Du, M. J. Wahila, L. F. J. Piper, T. L. Lee, H. J. Edwards, V. R. Dhanak, K. H. L. Zhang, *J. Mater. Chem. C* **2018**, 6, 2275.
- [35] A. M. Ganose, M. Cuff, K. T. Butler, A. Walsh, D. O. Scanlon, *Chem. Mater.* **2016**, 28, 1980.