

1 Perforation of Aluminium Alloy-CFRP Bilayer Plates under Quasi-static and  
2 Impact Loading

3 B. Yu<sup>ab</sup>, V. S. Deshpande<sup>a</sup>, N. A. Fleck<sup>a 1</sup>

4 <sup>a</sup> *Department of Engineering, University of Cambridge, Trumpington St., Cambridge, CB2 1PZ, UK*

5 <sup>b</sup> *Department of Material Science and Engineering, University of Toronto, 184 College St., Toronto, Ontario, M5S*  
6 *3E4, Canada*

7  
8 **Abstract**

9 The ability of a metallic surface layer to protect CFRP cross-ply plates against perforation  
10 is explored. Aluminium alloy plates (either AA1050A or AA6082-T6) were placed in front of a  
11 CFRP layer, and the bilayer was subjected to either quasi-static indentation or to ballistic impact  
12 by a spherical projectile, with rigid back support or an edge-clamped boundary condition. The  
13 observed perforation mechanism of the CFRP layer is neither influenced by the presence of the  
14 metallic layer nor by the choice of loading rate (i.e. quasi-static versus ballistic). In the back-  
15 supported condition, the CFRP layers fail by an indirect tension mode that consists of tensile failure  
16 of plies in the material directly beneath the indenter or projectile. Alternatively, in the edge-  
17 clamped condition, the CFRP layers fail by a shear plugging mechanism. Although the presence  
18 of metallic layers does not suppress the shear plugging of the underlying CFRP layer, the loaded  
19 area in the CFRP layer increases by the addition of the protective metallic layer, thereby increasing  
20 the perforation resistance of the CFRP layer.

21  
22 **Keywords:** multi-layer composites, perforation mechanisms, quasi-static indentation, ballistics,  
23 shear plugging, indirect tension

24  

---

<sup>1</sup> Corresponding author. Tel.: +44-1223-748240; fax: +44-1223-332662. E-mail address: naf1@eng.cam.ac.uk

## 25 **1 Introduction**

26 Carbon fibre reinforced plastic (CFRP) composites are increasingly used for structural  
27 applications due to their high stiffness and strength-to-weight ratios. Applications range from the  
28 structural frame and panels of automobiles and aircraft to fan blades for gas turbines. However,  
29 CFRP has an inferior impact resistance to composites such as ultrahigh molecular weight  
30 polyethylene (UHMWPE) fibre-based Dyneema<sup>®</sup> laminates. The high impact resistance of  
31 Dyneema<sup>®</sup> cross-ply laminates can be traced to its failure mechanism of indirect tension [1–5].  
32 In contrast, under ballistic loading, conventional CFRP laminates of high matrix shear strength fail  
33 by a shear plugging mode (involving matrix crack formation, ply delamination, and fibre fracture)  
34 [6–8], and consequently have inferior ballistic resistance. If a strategy can be developed whereby  
35 CFRP fails by indirect tension rather than by shear plugging, then a major advance could be made  
36 in terms of its penetration resistance. Recently, it has been shown that the indirect tension  
37 mechanism can be activated in CFRP cross-ply laminates under quasi-static out-of-plane  
38 compressive loading [9], indentation loading [10], and ballistic impact loading [10]. The ballistic  
39 limit (i.e. penetration velocity) of CFRP cross-ply laminates is increased by suppressing the shear  
40 plugging mode and by activating the indirect tension mode through the reduction of matrix shear  
41 strength. The aim of the current study is to explore the possibility of improving the impact  
42 resistance of CFRP laminates by activating the indirect tension mechanism without a reduction in  
43 matrix shear strength. A possible strategy is to place a protective metallic layer in front of the  
44 laminate and thereby reduce the level of contact stress both for quasi-static indentation (as in  
45 automobile impact) and for ballistic impact, for example in the protection of lightweight armor-  
46 clad vehicles. This is the motivation for the current study.

47 An established method of increasing the impact resistance of long fibre composites is to  
48 add metallic interlayers, for example by alternating layers of fibre composite and aluminium alloy,  
49 the so-called fibre-metal laminate [11–16]. Currently, the most common types of fibre-metal  
50 laminate are glass reinforced aluminium laminates (GLARE<sup>®</sup>), aramid fibre reinforced  
51 aluminium laminates (ARALL<sup>®</sup>), and carbon fibre reinforced aluminium laminates (CARAL).

52 The failure mechanism of the fibre-metal laminates under impact loading is complex as it  
53 involves both matrix and fibre failure in the composite layer, plastic deformation of the metallic  
54 layer, and debonding at the metal-composite interface [17]. While many researchers have focused

55 on the mechanics of GLARE<sup>®</sup> [18–22] and ARALL<sup>®</sup> [18,19,23–25], a relatively limited amount  
56 of literature is available on the impact mechanics of CARAL [13,14,16]. A recent study by Bienias  
57 et al. [14] investigated the damage mechanism of a composite sandwich consisting of a CFRP core  
58 and aluminium alloy face sheets, subjected to a low-velocity impact. They observed that the  
59 damage comprises transverse matrix cracks and ply delamination in the CFRP layer, plastic  
60 deformation of the aluminium alloy layers, and debonding of the metal-CFRP interfaces.  
61 Furthermore, the presence of the metallic layers reduces the extent of matrix cracking and  
62 delamination within the CFRP layer compared to that of monolithic CFRP of identical thickness.  
63 However, their study did not investigate perforation involving fibre failure at higher impact  
64 velocities. Thus, it remains unclear whether the presence of a protective metallic layer can activate  
65 the indirect tension mechanism in the CFRP layer at impact velocities near the ballistic limit of  
66 CFRP. To resolve this question, the effect of protective metallic layers on the perforation  
67 mechanism and the ballistic resistance of aluminium alloy/CFRP bilayer plates is explored herein.

68

### 69 *Scope of Study*

70 The objective of the current study is to determine the degree of protection by an aluminium  
71 alloy layer on the impact resistance and perforation mechanism of a CFRP plate. Figure 1  
72 illustrates the general problem. An aluminium alloy layer is placed in front of a CFRP cross-ply  
73 laminate, thereby creating an aluminium alloy-CFRP bilayer plate. The bilayer plates are subjected  
74 to quasi-static indentation and ballistic impact by a spherical indenter or projectile under two types  
75 of support condition: a rigid back support (simulating a thick laminate) and edge-clamped. In total,  
76 four types of tests were conducted: (i) quasi-static indentation with rigid back support, (ii) quasi-  
77 static indentation test with edge-clamping, (iii) ballistic test with rigid back support, and (iv)  
78 ballistic test with edge-clamping. Two grades of aluminium alloy were used in the fabrication of  
79 the bilayer plates: (i) AA1050A-H6 and (ii) AA6082-T6. The quasi-static and ballistic  
80 performance of the bilayer plates were compared with the unprotected monolithic CFRP plate. The  
81 majority of the bilayers had no bonding of the metal/CFRP interface. However, to gain insight into  
82 the role of bonding, samples with and without adhesive were compared in selected tests.

83

## 84 2 Specimen Manufacture

85 Cross-ply laminates  $[0^\circ/90^\circ]_{16}$  were made from Hexply<sup>®</sup> 8552/35%134/IM7 carbon  
86 fibre/epoxy prepregs (of ply thickness 0.131 mm). They were cured in an autoclave following the  
87 procedure as recommended by the Hexcel Corporation [26]. Three classes of composite plate were  
88 manufactured by making use of the cured CFRP: a monolithic CFRP plate, or by placing a single  
89 aluminium alloy sheet, AA1050A-H6 (40 Vickers) or AA6082-T6 (120 Vickers), in front of the  
90 CFRP plates. The monolithic CFRP plates were made by cutting the as-cured CFRP laminates  
91 using a diamond saw into squares of dimension  $w \times w$  (where  $w = 75$  mm, thickness = 4 mm, and  
92 an areal density of  $6.28 \text{ kg/m}^2$ ). The tensile properties of the aluminum alloy sheets were  
93 measured by uniaxial tensile tests using standard dog-bone shaped specimens and a strain rate of  
94  $10^{-3} \text{ s}^{-1}$ . The AA1050A-H6 has a 0.2% offset yield strength  $\sigma_y$  of 107 MPa, an ultimate tensile  
95 strength (UTS) of 117 MPa, and elongation to failure of 7%. In contrast, the AA6082-T6 has  $\sigma_y$   
96 = 262 MPa, UTS = 303 MPa, and an elongation to failure of 16%, see Figure 2.

97 The aluminium alloy sheets were also cut into squares of in-plane dimension  $w \times w$  (where  
98  $w = 75$  mm, thickness  $h = 1.5$  mm, and an areal density of  $3.45 \text{ kg/m}^2$ ). The following labelling  
99 procedure is used throughout this study for each group of specimens: (A) monolithic CFRP panels,  
100 (B) bilayer panels with an AA1050A-H6 sheet in front of CFRP, and (C) bilayer panels with an  
101 AA6082-T6 sheet in front of CFRP. Each monolithic plate (A) had a thickness of  $H = 4$  mm and  
102 an areal density  $\rho_A$  of  $6.28 \text{ kg/m}^2$  while the bilayer plates (B) and (C) each had a total thickness  
103 of 5.5 mm and an areal density  $\rho_A$  of  $9.73 \text{ kg/m}^2$ ; these parameters are summarised in Table 1.

104 Unless otherwise specified, the bilayer plates (B) and (C) contained no adhesive between  
105 the aluminium alloy layer and the CFRP layer. This allowed for the placement of pressure sensitive  
106 films between the alloy and the CFRP layer in order to measure the contact pressure during  
107 indentation tests. The effect of a bonding between metallic layer and underlying CFRP plate on  
108 the penetration mechanism was determined by the application of an epoxy adhesive<sup>1</sup>, Redux 810

---

<sup>1</sup> The adhesive was applied between the metal and the composite layers. The layers were then bonded under a pressure of 22 kPa for 5 hours at room temperature, and the bilayer plates were allowed to cure for a further 120 hours at room temperature to attain the fully cured state.

109 <sup>®</sup> to a selective set of specimens, followed by quasi-static indentation tests under an edge-clamped  
110 condition.

111

## 112 **3 Test Methods**

### 113 **3.1 Ballistic Tests**

114 Composite plates (A) and bilayer plates (B) and (C) were subjected to ballistic impact by a  
115 hardened steel ball bearing of diameter  $D = 5.6$  mm and a mass  $m_p = 7.2 \times 10^{-4}$  kg. (For the  
116 bilayer plates, the aluminium alloy sheet is on the front face of the plate.) Spherical projectiles  
117 were launched using a gas gun (with helium or nitrogen compressed gas, depending upon the desired  
118 velocity) with a 4.5 m long aluminium barrel having a bore diameter of 6 mm. The projectile  
119 impacted the specimens normally and centrally at an impact velocity  $v_0$  from 30 m/s to 380 m/s  
120 , as measured using a set of laser gates placed near the exit of the barrel. High-speed images were  
121 taken using a Phantom <sup>®</sup> V1610 camera (with an inter-frame time of 16  $\mu$ s and an exposure time  
122 of 0.43  $\mu$ s ) to record the rebound velocity  $v_r$  and to confirm the laser measurements of the impact  
123 velocity  $v_0$  . The ballistic tests were performed for two choices of boundary condition: (i) edge-  
124 clamped and (ii) back-supported, as follows.

125 (i) *Edge-clamped tests*. The composite plates were friction-clamped between two 12.7 mm thick  
126 steel plates using M6 bolts each with 8 Nm torque, as illustrated in Figure 3a. To achieve this, the  
127 front and back plates were surface-roughened by sand blasting. The front and backing plates each  
128 consisted of 12 equi-spaced holes (with hole diameter of 6 mm and pitch diameter of 90 mm) and  
129 a concentric opening window of diameter of  $D_s = 55$  mm that allowed for the back face deflection  
130 and perforation of the specimens. The backing plate was mounted onto an outer frame allowing a  
131 projectile to impact the specimen normally through the centre of the opening.

132 (ii) *Back-supported tests*. The composite plates were placed in front of a hardened silver steel (560  
133 Vickers) backing plate of thickness 45 mm. The projectile impacted normally and centrally in the  
134 negative z-direction as defined in Figure 3b. The specimens were loosely adhered to the backing  
135 plate using double-sided adhesive tape.

136

### 137 3.2 Quasi-static Indentation Tests

138 Composite plates (A) to (C) were subjected to out-of-plane indentation by a hemispherical  
139 indenter made of hardened silver steel (700 Vickers) with a diameter of  $D = 5.6$  mm under (i) an  
140 edge-clamped condition and (ii) a back-supported condition. With the exception of the indenter,  
141 the specimen dimensions and the test set-up of the indentation test were identical to those in the  
142 ballistic test as shown in Figures 3a and 3b. A displacement rate  $\dot{u}_z = 1.7 \times 10^{-4}$  m/s was applied  
143 in the out-of-plane direction via a screw-driven test machine. The indentation load  $F$  was recorded  
144 by the machine load cell and the displacement of the indenter  $u_z$  was measured using ac<sup>1</sup>.

145 For selected samples, the contact area of the CFRP layer (i.e. the contact area of the top  
146 face in the monolithic plates, the contact area between the aluminium alloy layer and the CFRP in  
147 the bilayer plates) and the average contact pressure were measured during the interrupted  
148 indentation tests by placing pressure measurement films<sup>2</sup> on top of the CFRP layer for each  
149 incremental displacement level. The pressure sensitive film contains microcapsules with various  
150 sizes and wall strengths that are correlated with pressure. The microcapsules break when a pressure  
151 of above 35 MPa is applied, creating a red coloured patch. The MS films were employed to  
152 measure the contact radius  $a$  in order to calculate the average pressure  $\bar{p}$  in the subsequent  
153 interrupted tests. During the interrupted tests, a layer of MS film (of thickness 90  $\mu\text{m}$ ) was placed  
154 on top of the CFRP layer (i.e. on top of the monolithic CFRP plate (A) or between the CFRP layer  
155 and the aluminium alloy layer of the bilayer plates (B) and (C)). The contact radius  $a$  was estimated  
156 to be the radius at which the contact pressure exceeded the lower limit of the calibrated pressure  
157 range (i.e. 35 MPa). At a sufficiently high indentation displacement, the indenter penetrated both  
158 the pressure film and the CFRP layer and thus the contact radius was assumed to equal the indenter  
159 radius (i.e.  $a = R$ ).

---

<sup>1</sup> The laser extensometer (EIR LE-05, manufactured by the Electronic Instrument Research) was operated at a scan frequency of 100 Hz.

<sup>2</sup> Fuji Prescale<sup>®</sup> MS. Fujifilm Holdings Corporation, 7-3, Akasaka 9-chome, Minato-ku, Tokyo 107-0052, Japan

## 160 4 Results

### 161 4.1 Failure Mechanism

162 As-tested specimens were sectioned across the impact zone along the fibre direction in the top ply,  
163 using an abrasive cut-off wheel. Examples of the cross-sectional microscopy images of materials  
164 (A) and (C) are shown in Figures 4 and 5, respectively. The failure mechanism of the CFRP layer  
165 depended on the imposed boundary condition (i.e. back-supported versus edge-clamped) but was  
166 neither affected by the presence of the metallic layer nor by the loading rate (quasi-static versus  
167 ballistic). In the back-supported condition, the CFRP layers failed by an indirect tension mode  
168 consisting of tensile failure of plies in the material directly beneath, and near the center line of, the  
169 indenter/projectile. In contrast, for the edge-clamped case, the CFRP layers failed by a shear  
170 plugging mechanism consisting of matrix shear cracks, ply delamination, and fibre fracture at the  
171 edge of contact. Note that, in the case of the edge-clamped condition, material (A) has a lower  
172 perforation resistance than material (C) for a given level of threat. Thus, material (C) shows a  
173 lower level of damage (i.e. a lower number of plies with fibre failure). However, the location of  
174 fibre failure in both material (A) and material (C) can easily be identified to be at the edge of  
175 contact. At a higher level of threat, more plies in material (C) would show fibre failure and its  
176 fractography would appear more similar to that of material (A) (see example in Fig. 10d).

177

### 178 4.2 Quasi-static Edge-clamped Indentation

179 The indentation response (in terms of load  $F$  versus displacement  $u_z$ ) of the monolithic  
180 CFRP and of the bilayer plates are presented in Figure 6a for an edge-clamped boundary condition.  
181 All specimens exhibited an initial peak load  $F_i$  at  $u_z$  of 1-2 mm, and for illustrative purposes this  
182 point is labelled (i) for the monolithic CFRP (A). The CFRP plate (A) showed the lowest value of  
183  $F_i$ , followed by the bilayer plate (B) and then the bilayer plates (C). Post-test inspection revealed  
184 that the initial peak load  $F_i$  was associated with matrix shear crack formation in the area beneath  
185 the edge of contact, while the fibres remained intact. Beyond the initial peak load, the indentation  
186 load increased up to a displacement of  $u_z$  of 4 mm, as labelled by point (ii) in the figure for the  
187 CFRP plate (A), again for illustration. Beyond this displacement, the indentation load began to fall  
188 in a series of dynamic events, indicating a series of failures in the CFRP layer. Post-test inspection

189 revealed that the spikes in load were associated with fibre fracture beneath the edge of contact, as  
 190 membrane tension develops within the stretched plate.

191 At any given stage of indentation, write  $a$  as the contact radius, and write  $h$  as the height  
 192 of the aluminium layer ( $h = 1.5$  mm),  $H$  as the height of the CFRP layer ( $H = 4$  mm),  $\tau_{Al}$  as  
 193 shear yield strength of the aluminium alloy layer (taken to be  $\sigma_y / 2$  of the aluminium alloy), and  
 194  $\bar{\tau}$  as the average shear stress of the CFRP layer beneath the circumference of the contact area.  
 195 Then, the indentation force  $F$  required to produce shear failure of the matrix in the CFRP layer  
 196 of the bilayer plate, at the edge of the contact, can be estimated as:

$$197 \quad F = 2\pi a(h\tau_{Al} + H\bar{\tau}) \quad (1)$$

198 Rearrangement of (1) gives  $\bar{\tau}$  in terms of load  $F$  such that:

$$199 \quad \bar{\tau} = \frac{F}{2\pi aH} - \frac{h\tau_{Al}}{H} \quad (2)$$

200 Recall that the contact radius  $a$  on the top face of the CFRP layer was measured during  
 201 the interrupted indentation tests by placing a Prescale<sup>®</sup> film on top of the CFRP layer for each  
 202 incremental displacement level (at least 17 levels for each material). The measurements of the  
 203 contact radius are summarised in Figure 6b by plotting  $a/R$  (the radius of the indenter is  $R = 2.8$   
 204 mm) as a function of displacement  $u_z$ . Upon making use of the measured values of  $a$ , the  
 205 normalised average shear stresses  $\bar{\tau}/\tau_y$  (where  $\tau_y$  is defined to be the short beam shear strength  
 206 of the CFRP layer, i.e. 99 MPa) is obtained via (2) and is plotted as a function of versus  $u_z$  in  
 207 Figure 6c for materials (A) to (C). Consider first the composite plate (A). Note that damage  
 208 initiation occurred at  $\bar{\tau}/\tau_y \sim 1$  due to matrix shear failure (i.e. when the average shear stress  
 209 reached the shear strength of the CFRP layer), as labelled (i) in the figure. As the displacement  
 210 increased to  $u_z = 4$  mm, the normalised average shear stress of  $\bar{\tau}/\tau_y$  exceeded unity and fibre  
 211 fracture occurred beneath the edge of contact, as labelled by point (ii). We conclude that for an  
 212 indent depth on the order of the ply thickness (4 mm), tensile membrane stresses develop, and  
 213 failure involves the tensile fracture of the fibres contributes to the indentation strength of the CFRP  
 214 and so the average shear stress exceeds unity. A similar characteristic is observed for the bilayer  
 215 plates: shear failure occurs, and is followed by a more complex failure mode involving membrane  
 216 tension at larger indent depths.



217

### 218 **4.3 Quasi-static, Back-supported Indentation**

219 The indentation responses (in terms of load  $F$  versus displacement  $u_z$ ) of the composite  
220 plate (A) and bilayer plates (B) and (C) are presented in Figure 7a for the back-supported condition.  
221 Monolithic material (A) exhibited an initial peak load  $F_i = 14.7$  kN at displacement  $u_z \sim 0.8$  mm,  
222 as labelled (i) in Figure 7a. In contrast, specimens types (B) and (C) yielded at a displacement  $u_z$   
223  $\sim 1$ -2 mm due to plastic deformation of the aluminium alloy layers, delaying the peak loads  $F_i$  to  
224  $u_z \sim 2.5$  mm. Their initial peak loads were higher than for material (A), with material (B) at  
225  $F_i = 22.2$  kN and material (C) at  $F_i = 25.3$  kN. Post-test inspection revealed that the initial peak  
226 load  $F_i$  for all 3 materials (A) to (C) was associated with fibre tensile failure of the top ply in the  
227 zone directly beneath and near the centre line of the indenter.

228 The average indentation pressure  $\bar{p}$  beneath the indenter can be expressed as:

$$229 \quad \bar{p} = \frac{F}{\pi a^2} \quad (3)$$

230 where the contact radius  $a$  on the top face of the CFRP layer, as measured using Prescale<sup>®</sup> films,  
231 is plotted in Figure 7b. The normalised average pressure  $\bar{p}/\bar{p}_f$  (where  $\bar{p}_f = 1350$  MPa is  
232 defined to be the out-of-plane compressive strength of the CFRP layer) is plotted as a function of  
233 displacement  $u_z$  in Figure 7c. For specimens tested with back-support, damage occurred at  $\bar{p}/\bar{p}_f$   
234  $\sim 1$  as a result of out-of-plane compressive failure. For illustration, this is labelled (i) for the  
235 monolithic CFRP plate (A). Recall that the out-of-plane compressive strength  $\bar{p}_f$  of the CFRP  
236 layer was associated with an indirect tension mechanism (as mentioned in our recent studies  
237 [9,10]), and it is concluded that the CFRP layer and bilayer plates also failed by indirect tension  
238 when indented under back-support. The presence of the aluminium face layer leads to reduced  
239 contact pressures on the CFRP layer at small values of indent depth (less than 2 mm), and to a  
240 delay in the triggering of failure of the CFRP by the indirect tension mechanism.

241

#### 242 **4.4 Effect of Boundary Condition on the Average Indentation Pressure**

243 The average indentation pressure of composite plates under edge-clamped and back-  
244 supported conditions are compared in Figure 8 (with data for material (B) omitted for the sake of  
245 clarity and brevity). Recall that the back-supported CFRP layer for the monolithic case (A) and for  
246 the bilayer case (C) failed by the indirect tension mechanism when  $\bar{p}/\bar{p}_f$  is on the order of unity.  
247 At small indent depths, the aluminium face sheet of bilayer (C) yields at  $\bar{p}/\bar{p}_f$  below unity,  
248 thereby protecting the underlying CFRP layer. Now consider the edge-clamped cases (A) and (C).  
249 The CFRP failed by a shear plugging mechanism at an average pressure  $\bar{p}/\bar{p}_f$  that is significantly  
250 below unity, and the indirect tension mechanism is not triggered.

#### 252 **4.5 Effect of the presence of a Metallic Layer on the Indentation Cut Fraction**

253 The level of damage in the CFRP layer can be represented by the fraction of plies that  
254 exhibited fibre failure  $f$  (referred to as cut fraction). To determine  $f$ , all materials were tested  
255 at different levels of ballistic/indentation threat, with a minimum of four tests per material. The  
256 tested specimens were sectioned across the impact zone along the fibre direction in the top ply,  
257 using an abrasive cut-off wheel. The level of damage for each material was then examined through  
258 optical fractography (see example in Fig. 4 and 5 where the number of failed plies in the CFRP  
259 can be counted by observing the micrographs). Note that in the quasi-static experiments, the load-  
260 displacement responses from the repeated tests overlap one another for each material,  
261 demonstrating that the results presented here are repeatable (the data are omitted for the sake of  
262 brevity). Figure 9 compares the level of damage in the CFRP layer prior to and following the  
263 addition of a protective metallic layer, by plotting  $f$  against the indentation load  $F$ . Under an  
264 edge-clamped condition,  $f$  is defined to be the fraction of plies where fibre tensile failure was  
265 observed. Under a back-supported condition,  $f$  is defined to be the fraction of plies where fibre  
266 shear cutting was observed. Figure 9 shows that the indentation loads required to cause the same  
267 degree of damage were consistently higher for CFRP protected by a metallic layer. The resistance  
268 to damage increased in the following order: material (A), material (B), and material (C). The  
269 interrupted tests revealed that plastic deformation of the metallic layer relieves the pressure in the

270 underlying CFRP. As a result, a larger indentation load  $F$  is required to achieve the same level of  
271 damage as for unprotected CFRP.

272

#### 273 **4.6 Effect of Adhesive bonding on Indentation Response**

274 What is the effect of bonding face sheet to the underlying CFRP laminate? To address this,  
275 repeat indentation tests were performed on bilayer plates in the edge-clamped condition, with the  
276 2 layers bonded by the epoxy adhesive, Redux 810<sup>®</sup>. The results are summarised in Figures 10a  
277 and 10b. Although the indentation load  $F$  required to cause a given degree of damage  $f$  (i.e.  
278 fraction of plies for which fibre tensile failure was observed) is, in general, higher for the  
279 adhesively bonded bilayer, the overall indentation responses (in terms of load  $F$  versus  
280 displacement  $u_z$ ) is relatively insensitive to the presence of the adhesive layer. Furthermore, the  
281 cross-sectional microscopy images of the tested bilayer plates (B) and (C) with adhesive present  
282 showed signs of shear plugging (along with adhesive debonding at the metal/CFRP interface), see  
283 Figures 10c and 10d. Note that multiple researchers [14,16,20,27,28] have reported such  
284 debonding in fibre metal laminates when tested under impact loading and this issue is currently an  
285 ongoing research challenge in the manufacture of fibre metal laminates [29–32].

286 It is concluded that the presence of the adhesive leads to a detectable increase in perforation  
287 resistance, but has no influence on the failure mechanism of the bilayer materials in the edge-  
288 clamped indentation tests. Within the scope of the current study, the presence of adhesive does not  
289 promote the activation of the indirect tension mechanism. Consequently, the remaining  
290 experiments in this study were conducted in the configuration with the adhesive absent.

291

#### 292 **4.7 Ballistic Impact**

293 The level of damage in the CFRP layer following ballistic impact, represented by the  
294 fraction of plies that exhibited fibre failure  $f$ , is plotted as a function of impact velocity  $v_0$  in  
295 Figure 11. For all tests, the fraction of failed plies increased progressively with impact velocity.  
296 Two critical velocities can be defined:  $v_{init}$  is the velocity at initiation of failure (defined to be the  
297 highest tested impact velocity at  $f = 0$ ), and  $v_p$  is the penetration velocity (defined to be the  
298 lowest tested impact velocity at  $f = 1$ ). Under both edge-clamped and back-supported boundary

299 conditions, the ballistic resistance in terms of  $v_{init}$  and  $v_p$  increased in the following order:  
300 monolithic material (A), bilayer composite plates (B), and bilayer composite plates (C). The higher  
301 ballistic resistance of material (C) was pronounced under the edge-clamped condition, where  $v_p$   
302 exceeded the launch velocity limit of the test set-up (380 m/s) and was estimated to be  
303  $v_p \sim 400$  m/s based upon extrapolation of the data.

## 304 **5 Discussion**

### 305 **5.1 Failure Mechanisms**

306 In both the quasi-static and the ballistic tests, the failure mechanisms of the CFRP layers  
307 in the monolithic and bilayer plates were sensitive to the boundary condition but were not affected  
308 by the presence or absence of the metallic layers.

309 In the edge-clamped state, transverse matrix cracks form in the CFRP when the local shear  
310 stress reached the matrix shear strength. As the indentation force or impact velocity increased, the  
311 matrix crack formation was followed by ply delamination and fibre fracture. Fibre fracture  
312 provided a failure path that connected the above-mentioned matrix cracks. This failure mode is  
313 often referred to as the shear plugging mechanism, and is commonly observed in the impact failure  
314 of conventional CFRP [6,7,33–35]. In the current study, the presence of a metallic front face did  
315 not suppress this shear plugging mode in the CFRP layer under both quasi-static and ballistic  
316 loading. Measurements of the contact area during the interrupted quasi-static indentation test  
317 confirmed that first failure in the bilayer composite plates occurred when the out-of-plane shear  
318 stress of the CFRP reached its matrix shear strength. However, the contact area measurement  
319 revealed that the plastic deformation of the metallic layer spread the indentation load over a larger  
320 area. This increased the quasi-static indentation load required for shear plug formation. In similar  
321 fashion, this load spreading effect of the metallic protection occurs under ballistic loading, thus  
322 increasing the energy required for shear plug formation and enhancing the ballistic resistance.

323 In the back-supported state, the CFRP cross-ply laminates fail by an indirect tension  
324 mechanism facilitated by ply tensile failure directly beneath the indenter/projectile. This failure  
325 mode is in agreement with that observed by Poe Jr. [36]. In the current study, the presence of the  
326 metallic protection did not alter the failure mode of the underlying CFRP. Nevertheless, the above-

327 mentioned load spreading effect was also observed in the back-supported tests and increased the  
328 indentation load.

329

## 330 **5.2 A Comparison of the Quasi-static and Ballistic Responses**

331 The above observations indicate that the failure mechanisms of a CFRP layer are the same  
332 under both quasi-static and ballistic loading. The level of damage under different loading  
333 conditions can be compared by plotting the cut fraction of plies  $f$  in the CFRP layer as a function  
334 of energy dissipation  $W$ . The energy absorption  $W$  in the quasi-static experiments was calculated  
335 by integrating the indentation load  $F$  over the displacement  $u_z$ :

$$336 \quad W = -\int_0^{u_0} F du_z \quad (4)$$

337 where  $u_0$  is the maximum displacement before unloading in each interrupted test. The energy  
338 dissipation  $W$  in the ballistic tests was calculated from the different kinetic energies of the  
339 projectile before impact and after rebound:

$$340 \quad W = \frac{m_p}{2} (v_0^2 - v_r^2) \quad (5)$$

341 where  $m_p$  is the projectile mass ( $7.2 \times 10^{-4}$  kg),  $v_0$  is the impact velocity, and  $v_r$  is the rebound  
342 velocity. Overall, the energy dissipation in the CFRP layer under quasi-static loading is  
343 comparable to the values from the ballistic test, see Figure 12. The disparity of the energy  
344 dissipation was larger in the edge-clamped condition; this can be attributed to the presence of stress  
345 wave propagation in the ballistic test as opposed to in the quasi-static test. In general, we expect  
346 the agreement between degree of damage and dissipated energy to break down when wave  
347 propagation and other inertial effects become significant, for example when the impact velocity is  
348 on the order of elastic (or plastic) wave speeds.

349 The bilayer composite plates tested in this study have a higher areal density than that of the  
350 monolithic CFRP layer. To account for the effect of additional mass on the energy absorption  
351 capability, the cut fraction of plies  $f$  in the CFRP layer is plotted as a function of specific energy  
352 absorption ( $W / \rho_A$ ) in Figure 13; here, the monolithic plates (A) have  $\rho_A = 6.28 \text{ kg/m}^2$  and the  
353 bilayer plates (B) and (C) have  $\rho_A = 9.73 \text{ kg/m}^2$ . We find that the presence of a metallic front

354 face increases the static and dynamic penetration resistance on the basis of specific energy  
355 dissipation.

356

## 357 **6 Concluding remarks**

358 The current study explores the protection against perforation by adding a protective  
359 metallic layer to cured CFRP cross-ply laminates. The aim is to determine whether the presence  
360 of an aluminium alloy layer can suppress the commonly observed brittle shear plugging  
361 mechanism in CFRP under ballistic and quasi-static loading. For this purpose, two types of  
362 aluminium alloy-CFRP bilayers were considered: a layer of either AA1050A-T6 or AA6082-T6  
363 was placed in front of a CFRP layer. The performance of bilayer plates was compared against that  
364 of monolithic CFRP plates without metallic protection. The composite plates were then subjected  
365 to quasi-static indentation and ballistic impact by a spherical indenter or projectile under back  
366 support or edge support. In total, four types of test were conducted: (i) quasi-static indentation test  
367 with rigid back support, (ii) quasi-static indentation test with an edge-clamped condition,  
368 (iii) ballistic test with rigid back support, and (iv) ballistic test with an edge-clamped condition.

369 In both quasi-static and ballistic tests, the qualitative perforation mechanism in the CFRP  
370 layers was sensitive to the boundary condition but was not affected by the presence of the metallic  
371 layers. Furthermore, bonding of the metal/CFRP interface did not alter the overall failure  
372 mechanism, but it did improve the perforation resistance of the underlying CFRP. When the  
373 specimens were tested under the edge-clamped condition, back face deflection was permitted. This  
374 caused the CFRP layers to fail by shear plugging with transverse matrix cracks, ply delamination,  
375 and fibre fracture concentrated at the circumference of the contact area.

376 In contrast, when the specimens were tested with back-support, the material underneath the  
377 indenter/projectile was subjected to compression. As a result, the CFRP layers failed by an indirect  
378 tension mode consisting of ply tensile failure directly beneath the indenter or the projectile, similar  
379 to the failure mode observed for CFRP cross-ply laminates when subjected to uniaxial out-of-plane  
380 compression.

381 The presence of the metallic layer did not alter the failure mechanism in the underlying  
382 CFRP layer, but reduced the magnitude of the indentation on the CFRP layer. Consequently, under  
383 both edge-clamped and back-supported conditions, the quasi-static strength and impact resistance  
384 of the CFRP layers increased due to the presence of the metallic layers. A greater benefit was

385 derived by a metallic layers of higher yield strength. The impact resistance (in terms of absorbed  
386 energy per areal density) measured from all the tests generally increased in the following order:  
387 monolithic CFRP, AA1050A-H6-CFRP bilayer, and AA6082-T6-CFRP bilayer. These data  
388 suggest that the use of metallic layers of high yield strength can potentially suppress shear plugging  
389 in the CFRP laminates.

390

### 391 **Acknowledgements**

392 The research work was sponsored by the Office of Naval Research (ONR), U.S. (Prime  
393 Award No. N62909-14-1-N232). The raw composite materials and the autoclave manufacturing  
394 process were generously provided by Hexcel Ltd. Finally, the doctoral study of one of the authors  
395 (B. Yu) was sponsored by the Croucher Foundation and the Cambridge Commonwealth, European  
396 & International Trust.

397 **REFERENCES**

- 398 [1] Karthikeyan K, Russell BP, Fleck NA, Wadley HNG, Deshpande VS. The effect of shear  
399 strength on the ballistic response of laminated composite plates. *Eur J Mech A/Solids*  
400 2013;42:35–53.
- 401 [2] Attwood JP, Khaderi SN, Karthikeyan K, Fleck NA, Omasta MR, Wadley HNG, et al. The  
402 out-of-plane compressive response of Dyneema® composites. *J Mech Phys Solids*  
403 2014;70:200–26.
- 404 [3] Karthikeyan K, Russell BP. Polyethylene ballistic laminates: Failure mechanics and  
405 interface effect. *Mater Des* 2014;63:115–25.
- 406 [4] O’Masta MR, Crayton DH, Deshpande VS, Wadley HNG. Mechanisms of penetration in  
407 polyethylene reinforced cross-ply laminates. *Int J Impact Eng* 2015;86:249–64.
- 408 [5] Attwood JP, Russell BP, Wadley HNG, Deshpande VS. Mechanisms of the penetration of  
409 ultra-high molecular weight polyethylene composite beams. *Int J Impact Eng* 2016;93:153–  
410 65.
- 411 [6] Cantwell WJ, Morton J. Comparison of the low and high velocity impact response of CFRP.  
412 *Composites* 1989;20:545–51.
- 413 [7] Cantwell WJ, Morton J. Geometrical effects in the low velocity impact response of CFRP.  
414 *Compos Struct* 1989;12:39–59.
- 415 [8] Cantwell WJ, Morton J. Impact perforation of carbon fibre reinforced plastic. *Compos Sci*  
416 *Technol* 1990;38:119–41.
- 417 [9] Yu B, Kaderi SN, Deshpande VS, Fleck NA. The Effect of Matrix Shear Strength on the  
418 out-of-plane Compressive Strength of CFRP Cross-ply Laminates. *Int J Solids*  
419 *Struct:Submitted*.
- 420 [10] Yu B, Karthikeyan K, Deshpande VS, Fleck NA. Perforation resistance of CFRP beams to  
421 quasi-static and ballistic loading: The role of matrix strength. *Int J Impact Eng*  
422 2017;108:389–401.
- 423 [11] Krull M, Vlot A, Krull M. Impact damage resistance of various fibre metal laminates. *J*  
424 *Phys Iv* 1997;7:1045–50.
- 425 [12] Lawcock G, Ye L. Effects of fibre\_matrix adhesion on CARBON/FIBRE/REINFORCED  
426 METAL LAMINATES- II. Impact behaviour. *Compos Sci Technol* 1998;3538:1621–8.
- 427 [13] Song SH, Byun YS, Ku TW, Song WJ, Kim J, Kang BS. Experimental and numerical



- 428 investigation on impact performance of carbon reinforced aluminum laminates. *J Mater Sci*  
429 *Technol* 2010;26:327–32.
- 430 [14] Bieniaś J, Jakubczak P, Surowska B, Dragan K. Low-energy impact behaviour and damage  
431 characterization of carbon fibre reinforced polymer and aluminium hybrid laminates. *Arch*  
432 *Civ Mech Eng* 2015;15:925–32.
- 433 [15] Yu G-C, Wu L-Z, Ma L, Xiong J. Low Velocity Impact of Carbon Fiber Aluminum  
434 Laminates. *Compos Struct* 2015;119:757–66.
- 435 [16] Jaroslaw B, Barbara S, Patryk J. The Comparison of Low-Velocity Impact Resistance of  
436 Aluminum/Carbon and Glass Fiber Metal Laminates. *Polym Compos* 2016;37:1056–63.
- 437 [17] Sadighi M, Alderliesten RC, Benedictus R. Impact resistance of fiber-metal laminates: A  
438 review. *Int J Impact Eng* 2012;49:77–90.
- 439 [18] Vlot A. Impact properties of Fibre Metal Laminates. *Compos Eng* 1993;3:911–27.
- 440 [19] Vlot A, Kroon E, La Rocca G. Impact Response of Fiber Metal Laminates. *Key Eng Mater*  
441 1998;141–143:235–76.
- 442 [20] Compston P, Cantwell WJ, Jones C, Jones N. Impact perforation resistance and fracture  
443 mechanisms of a thermoplastic based fiber-metal laminate. *J Mater Sci Lett* 2001;20:597–  
444 9.
- 445 [21] Hoo Fatt MS, Lin C, Revilock DM, Hopkins DA. Ballistic impact of GLARE fiber-metal  
446 laminates. *Compos Struct* 2003;61:73–88.
- 447 [22] Caprino G, Spataro G, Del Luongo S. Low-velocity impact behaviour of fibreglass-  
448 aluminium laminates. *Compos Part A Appl Sci Manuf* 2004;35:605–16.
- 449 [23] Johnson VVS. Impact and Residual Fatigue Behavior of ARALL and AS6/ 5245 Composite  
450 Materials October 1986. 1986.
- 451 [24] Sun CT, Dicken A, Wu HF. Characterization of impact damage in ARALL laminates.  
452 *Compos Sci Technol* 1993;49:139–44.
- 453 [25] Vlot A. Impact loading on fibre metal laminates. *Int J Impact Eng* 1996;18:291–307.
- 454 [26] Hexcel Composites. HexPly® 8552 epoxy matrix (180°C/356F curing matrix), product  
455 data. 2013.
- 456 [27] Atas C. An Experimental Investigation on the Impact Response of Fiberglass/Aluminum  
457 Composites. *J Reinf Plast Compos* 2007;26:1479–91.
- 458 [28] Wu G, Yang JM, Hahn HT. The impact properties and damage tolerance and of bi-

- 459 directionally reinforced fiber metal laminates. *J Mater Sci* 2007;42:948–57.
- 460 [29] Kim WS, Yun IH, Lee JJ, Jung HT. Evaluation of mechanical interlock effect on adhesion  
461 strength of polymermetal interfaces using micro-patterned surface topography. *Int J Adhes*  
462 *Adhes* 2010;30:408–17.
- 463 [30] Yun IH, Kim WS, Kim K, Jung JM, Lee JJ, Jung HT. Highly enhanced interfacial adhesion  
464 properties of steel-polymer composites by dot-shaped surface patterning. *J Appl Phys*  
465 2011;109.
- 466 [31] Ning H, Li Y. Improvement of interlaminar mechanical properties of CARALL based on  
467 nanofiller interface reinforcement and other fabrication techniques. 13th Int. Conf. Fract.  
468 Vol 5, Beijing, China: 2013, p. 3465–75.
- 469 [32] Pärnänen T, Kanerva M, Sarlin E, Saarela O. Debonding and impact damage in stainless  
470 steel fibre metal laminates prior to metal fracture. *Compos Struct* 2015;119:777–86.
- 471 [33] Cristescu N, Malvern LE, Sierakowski RL. Failure Mechanisms in Composite Rates  
472 Impacted by Blunt-Ended Penetrators. *Foreign Object Impact Damage to Compos A Symp*  
473 1975;No. 568 p. 159.
- 474 [34] Cantwell, W.J.; Morton J. The impact resistance of composite materials - a review.  
475 *Composites* 1991;22(5):347–62.
- 476 [35] Zhou G. Damage mechanisms in composite laminates impacted by a flat-ended impactor.  
477 *Compos Sci Technol* 1995;54:267–73.
- 478 [36] Poe Jr. CC. Simulated Impact Damage in a Thick Graphite/epoxy Laminate Using Spherical  
479 Indenters. *J Reinf Plast Compos* 1991;10:293–307.
- 480

481 **FIGURE CAPTIONS**

482 Fig. 1 An aluminium alloy-CFRP bilayer struck by a spherical indenter/projectile. All dimensions  
483 are in mm.

484 Fig. 2 Uniaxial tensile curves of aluminium alloy AA1050A-H6 and AA6082-T6.

485 Fig. 3 Sketches of (a) edge-clamped and (b) back-supported aluminium alloy-CFRP bilayer plates  
486 for impact by a spherical projectile. All dimensions are in mm.

487 Fig. 4 Cross-sectional images indicating that, regardless of the loading conditions, monolithic  
488 CFRP plate material (A) failed by shear plugging in the edge-clamped test and failed by indirect  
489 tension in the back-supported test.

490 Fig. 5 Cross-sectional images indicating that, regardless of the loading conditions, the CFRP layer  
491 of bi-material (C) failed by shear plugging in the edge-clamped test and failed by indirect tension  
492 in the back-supported test.

493 Fig. 6 Quasi-static indentation responses of edge-clamped plates (A) to (C). (a) load  $F$  versus  
494 displacement  $u_z$ , (b) normalised contact radius  $a/R$  versus displacement  $u_z$ , and (c) normalised  
495 average shear stress  $\bar{\tau}/\tau_y$  versus displacement  $u_z$ . First failure, labelled as (i), is associated with  
496 matrix cracking whereas the second failure, labelled as (ii), denotes fibre fracture beneath the edge  
497 of contact.

498 Fig. 7 Quasi-static indentation responses of back-supported plates (A) to (C). (a) load  $F$  versus  
499 displacement  $u_z$ , (b) normalised contact radius  $a/R$  versus displacement  $u_z$ , and (c) normalised  
500 average pressure  $\bar{p}/p_f$  versus displacement  $u_z$ . First failure, labelled (i), is associated with fibre  
501 tensile failure directly beneath the indenter.

502 Fig. 8 Quasi-static indentation load-displacement responses of materials (A) and (C) under edge-  
503 clamped and back-supported conditions in terms of normalised average pressure  $\bar{p}/p_f$  versus  
504 displacement  $u_z$ .

505 Fig. 9 The indentation cut fraction  $f$  in materials (A) to (C) versus indentation load  $F$  under  
506 (a) edge-clamped and (b) back-supported conditions.

507 Fig. 10 Edge-clamped indentation response of bilayer material (B) and (C) with and without  
508 bonding between layers. (a) indentation load  $F$  versus  $u_z$  and (b) indentation cut fraction  $f$

509 versus load  $F$  . (c)-(d) Cross-sectional micrographs of the bonded bilayer plates (B) and (C), after  
510 testing to the indentation load  $F$  levels as labeled (i) and (ii) in Figure 11b.

511 Fig. 11 The cut fraction  $f$  in materials (A) to (C) versus impact velocity  $v_0$  under (a) edge-  
512 clamped and (b) back-supported conditions.

513 Fig. 12 Cut fraction  $f$  in materials (A) to (C) from quasi-static and dynamic tests versus energy  
514 dissipation  $W$  under (a) edge-clamped and (b) back-supported conditions.

515 Fig. 13 Cut fraction  $f$  in materials (A) to (C) from quasi-static and dynamic tests versus specific  
516 energy dissipation  $W / \rho_A$  under (a) edge-clamped and (b) back-supported conditions.

517

518 **TABLE CAPTIONS**

519 Table 1 Layer thickness and areal density of monolithic CFRP and the aluminium alloy-CFRP  
 520 bilayer plates.

521

522

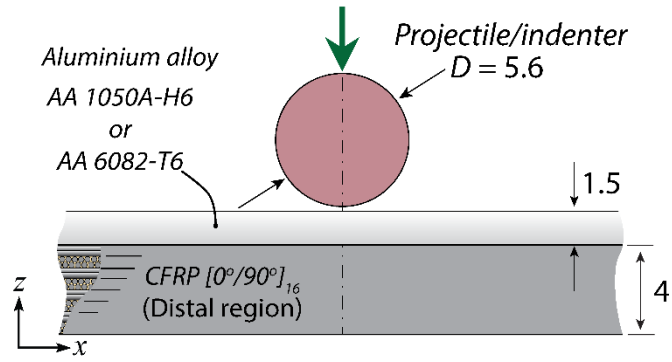
523

524

525 Table 1 Layer thickness and areal density of monolithic CFRP and the aluminium alloy-CFRP  
 526 bilayer plates.

Material	Metal layer thickness $h$ (mm)	CFRP layer thickness $H$ (mm)	Total plate thickness $H + h$ (mm)	Total areal density $\rho_A$ (kg/m <sup>2</sup> )
A	--	4	4	6.28
B	1.5	4	5.5	9.73
C	1.5	4	5.5	9.73

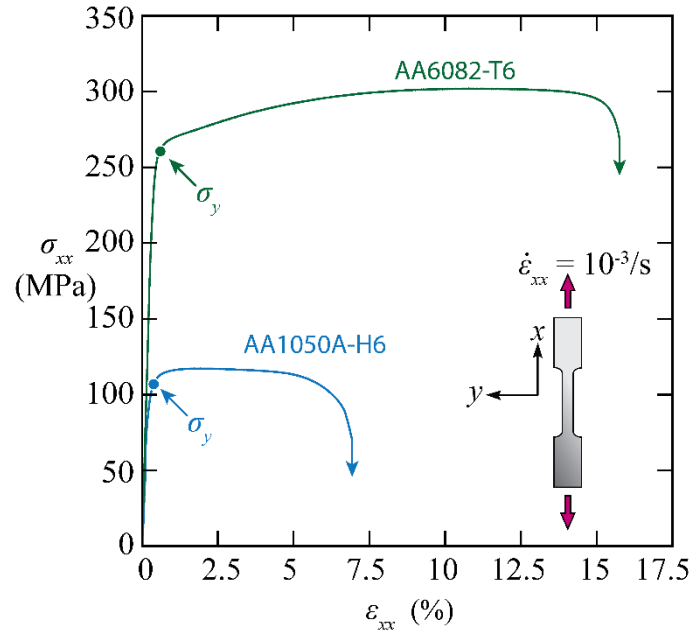
527



528

529 Fig. 1 An aluminium alloy-CFRP bilayer struck by a spherical indenter/projectile. All dimensions

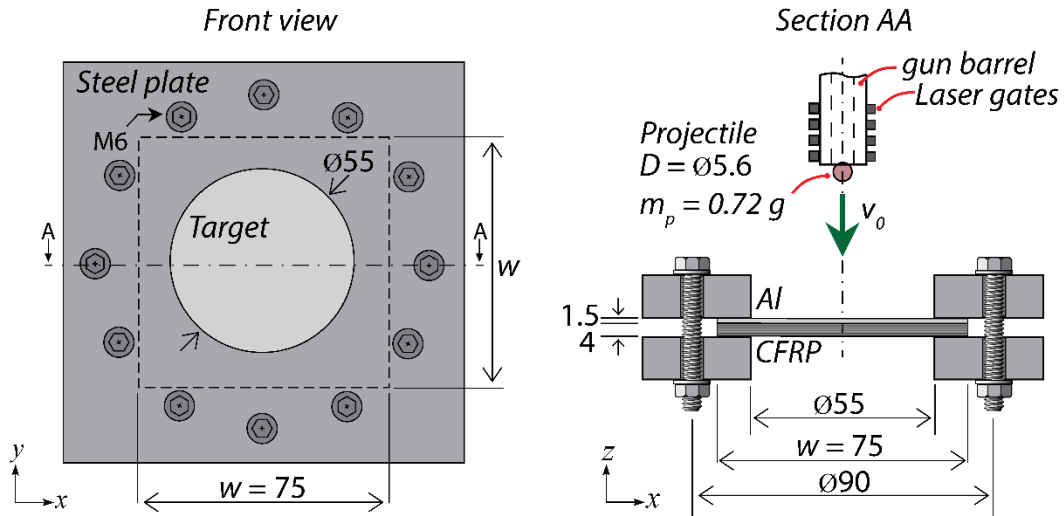
530 are in mm.



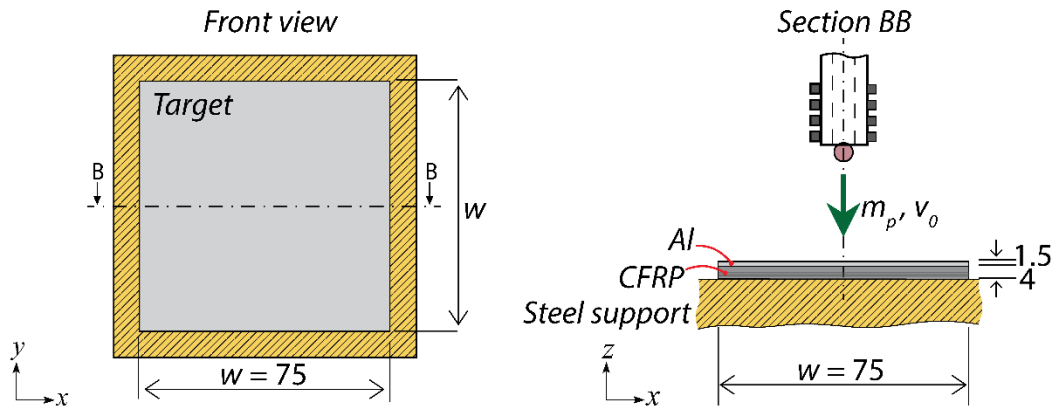
531

532 Fig. 2 Uniaxial tensile curves of aluminium alloy AA1050A-H6 and AA6082-T6.

a) *Edge-clamped condition*



b) *Back-supported condition*



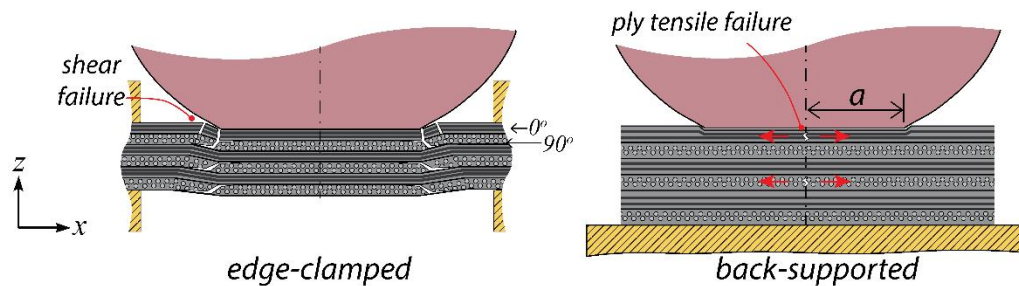
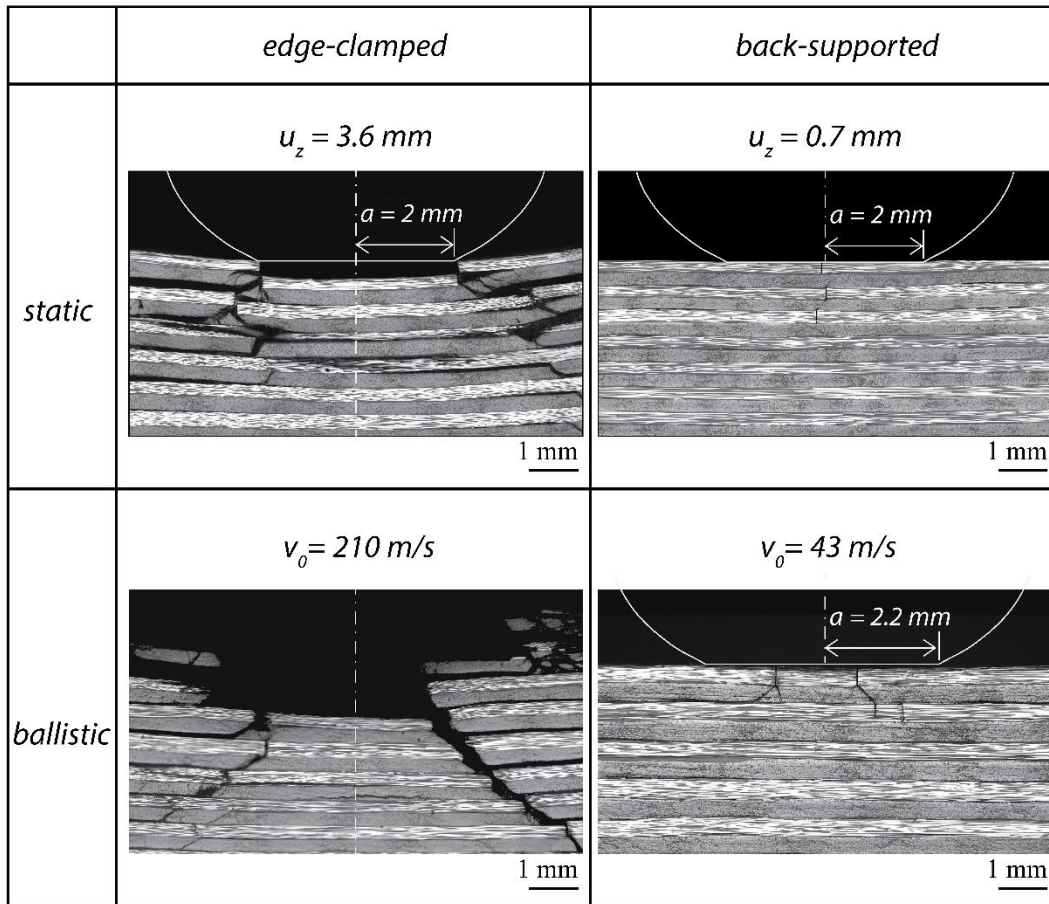
533

534 Fig. 3 Sketches of (a) edge-clamped and (b) back-supported aluminium alloy-CFRP bilayer plates

535 for impact by a spherical projectile. All dimensions are in mm.



Material (A) - monolithic CFRP



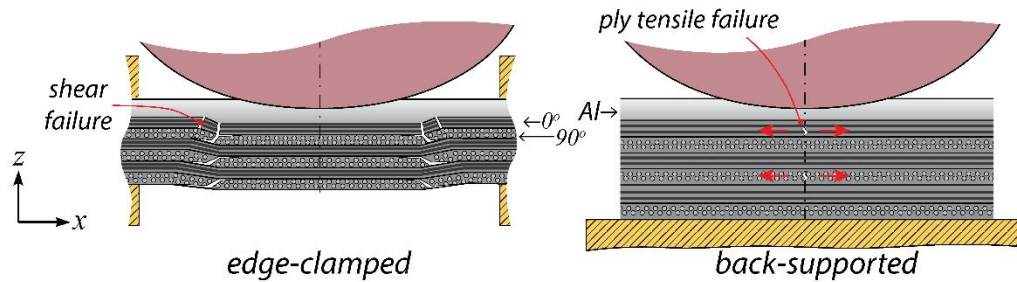
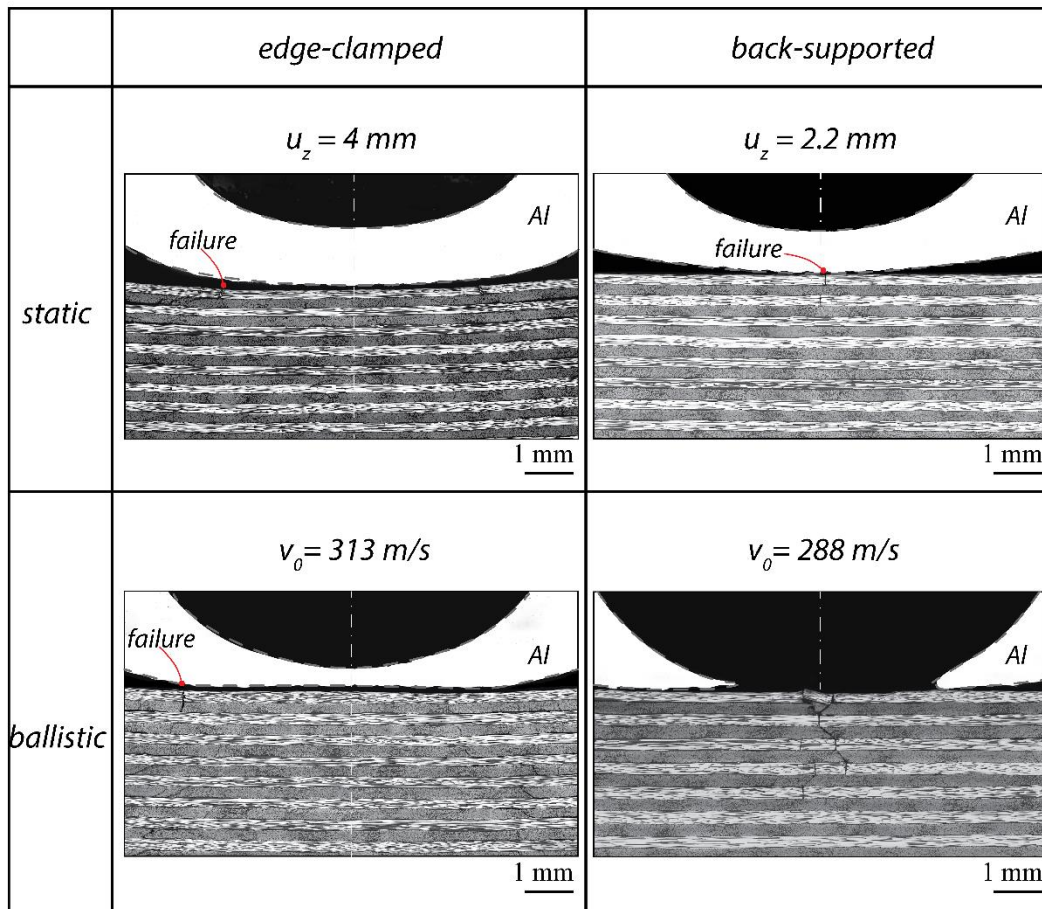
536

537 Fig. 4 Cross-sectional images indicating that, regardless of the loading conditions, monolithic

538 CFRP plate material (A) failed by shear plugging in the edge-clamped test and failed by indirect

539 tension in the back-supported test.

Material (C) - aluminium alloy-CFRP bilayer

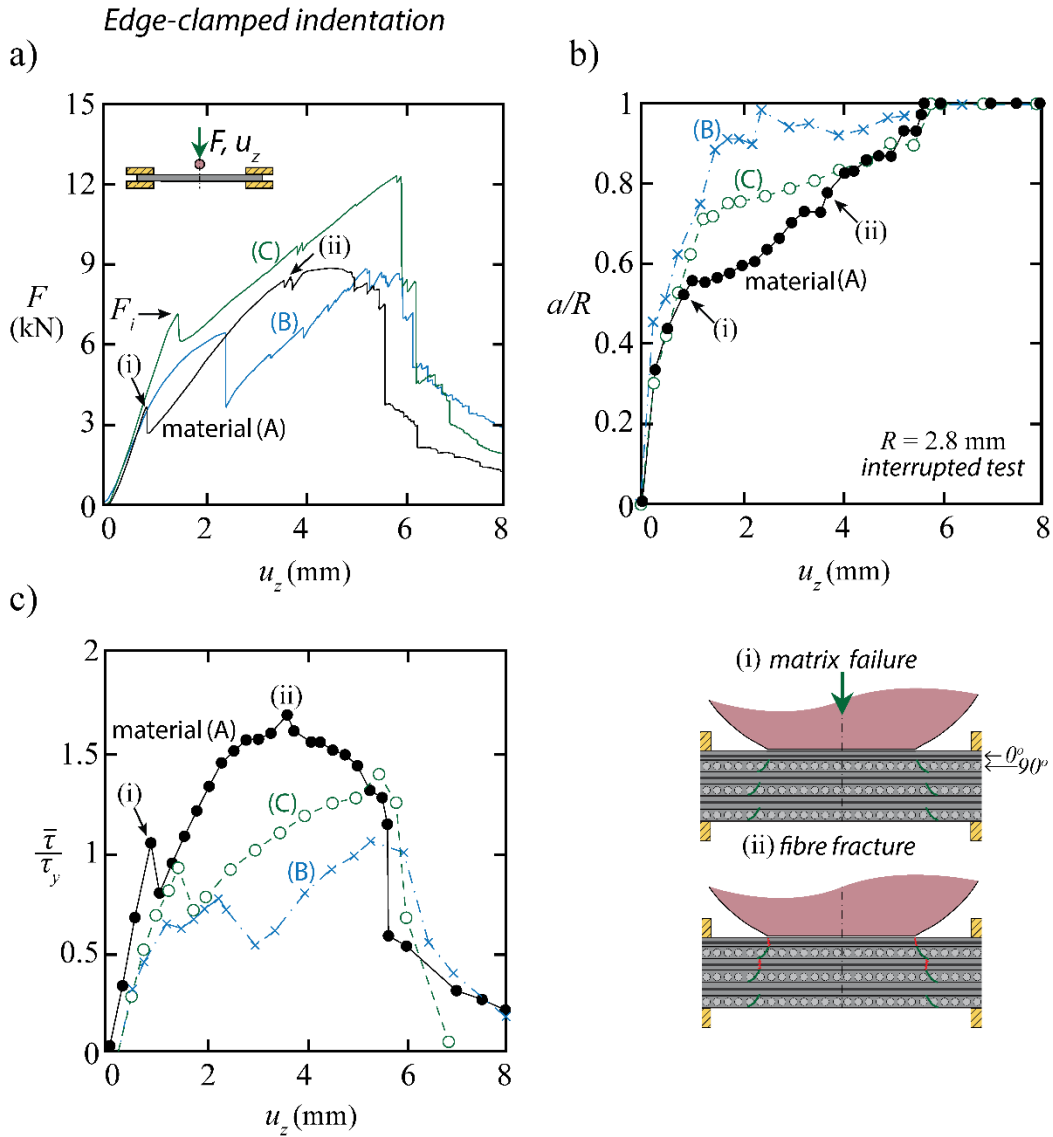


540

541 Fig. 5 Cross-sectional images indicating that, regardless of the loading conditions, the CFRP layer

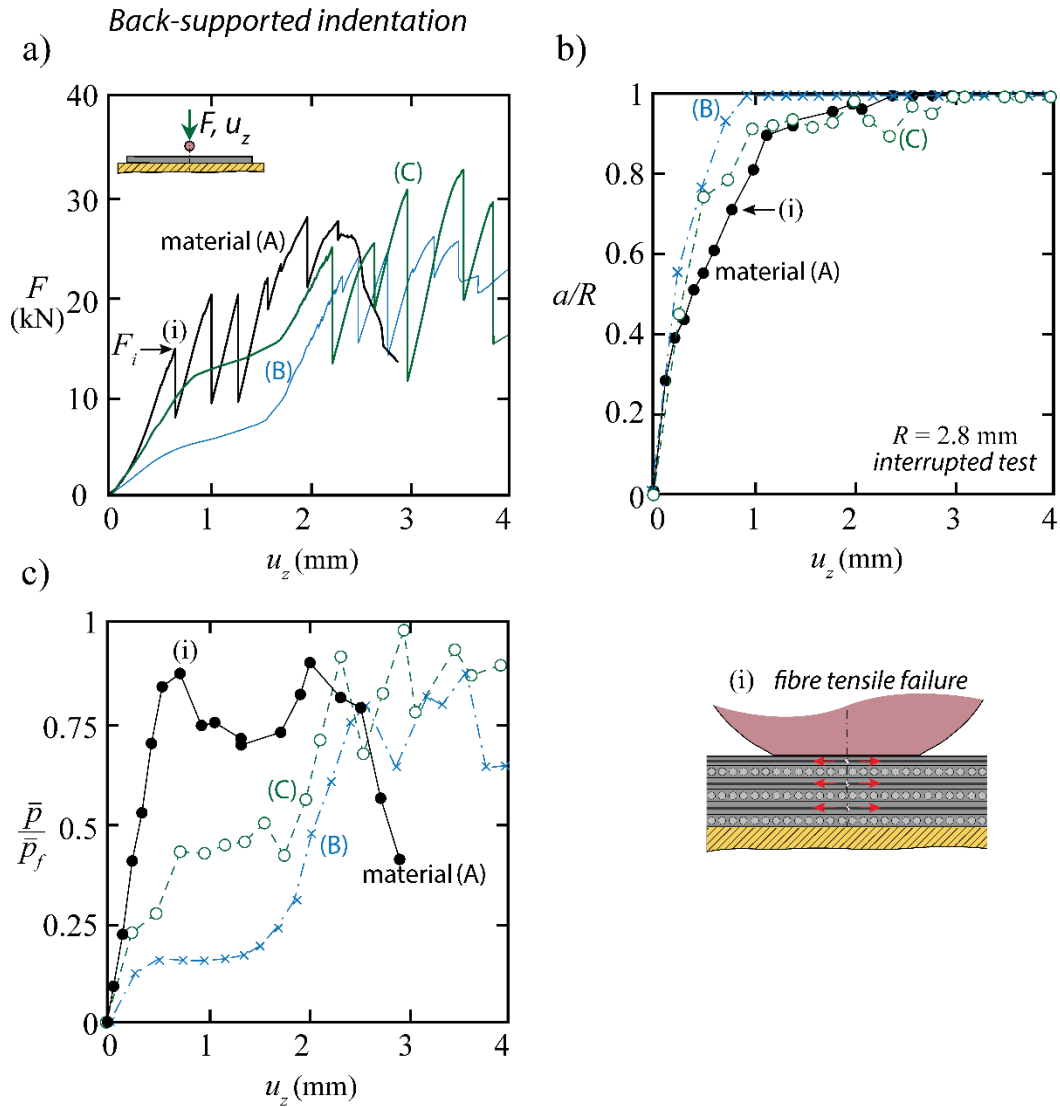
542 of bi-material (C) failed by shear plugging in the edge-clamped test and failed by indirect tension

543 in the back-supported test..



544

545 Fig. 6 Quasi-static indentation responses of edge-clamped plates (A) to (C). (a) load  $F$  versus  
 546 displacement  $u_z$ , (b) normalised contact radius  $a/R$  versus displacement  $u_z$ , and (c) normalised  
 547 average shear stress  $\bar{\tau} / \tau_y$  versus displacement  $u_z$ . First failure, labelled as (i), is associated with  
 548 matrix cracking whereas the second failure, labelled as (ii), denotes fibre fracture beneath the edge  
 549 of contact.



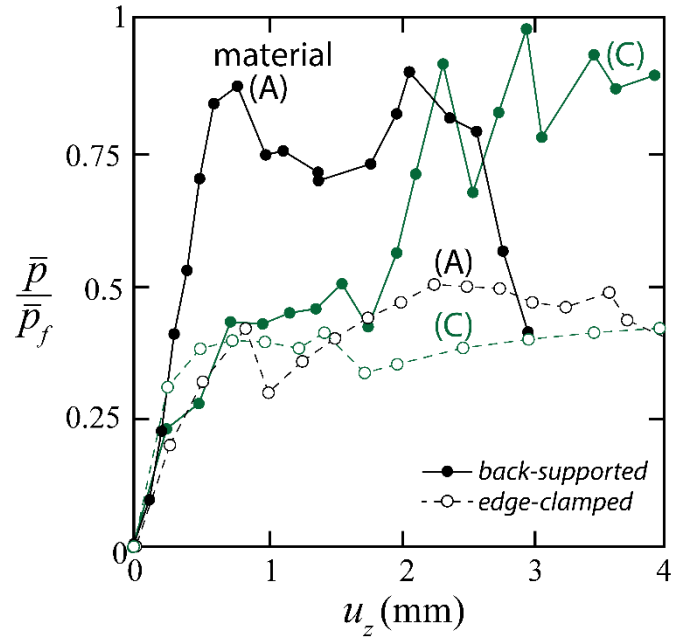
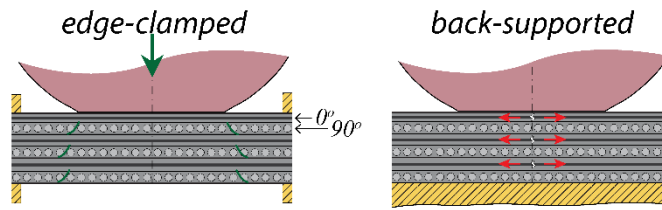
550

551 Fig. 7 Quasi-static indentation responses of back-supported plates (A) to (C). (a) load  $F$  versus

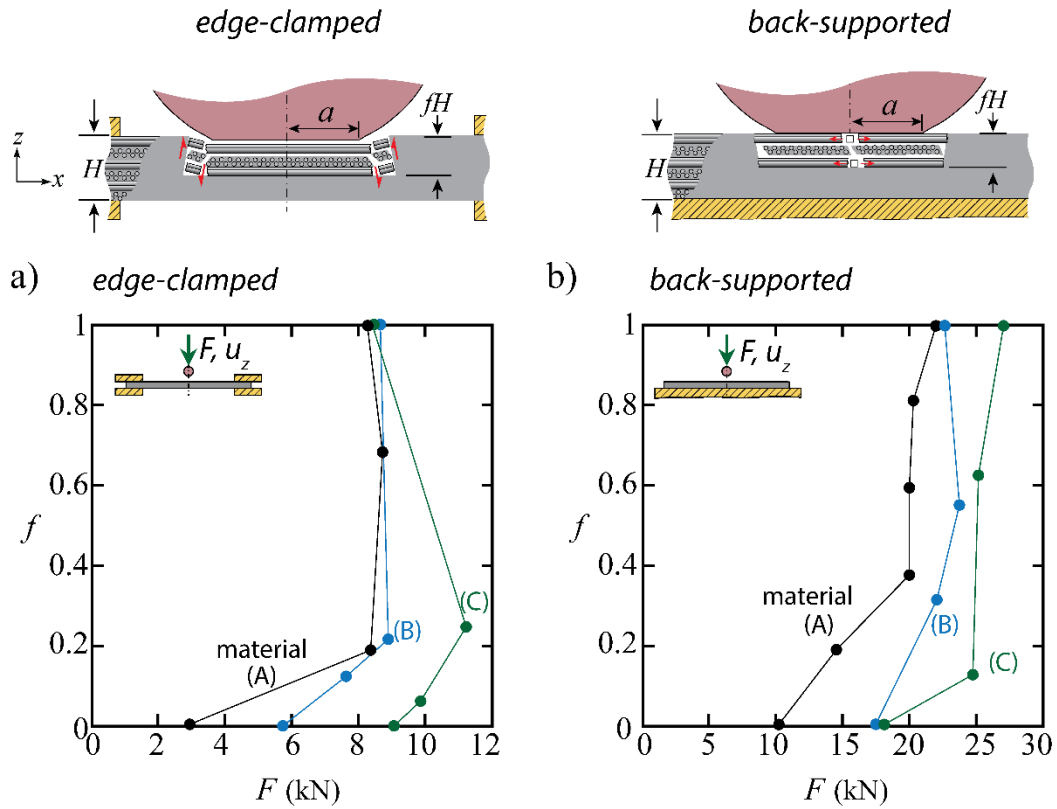
552 displacement  $u_z$ , (b) normalised contact radius  $a/R$  versus displacement  $u_z$ , and (c) normalised

553 average pressure  $\bar{p}/p_f$  versus displacement  $u_z$ . First failure, labelled (i), is associated with fibre

554 tensile failure directly beneath the indenter.

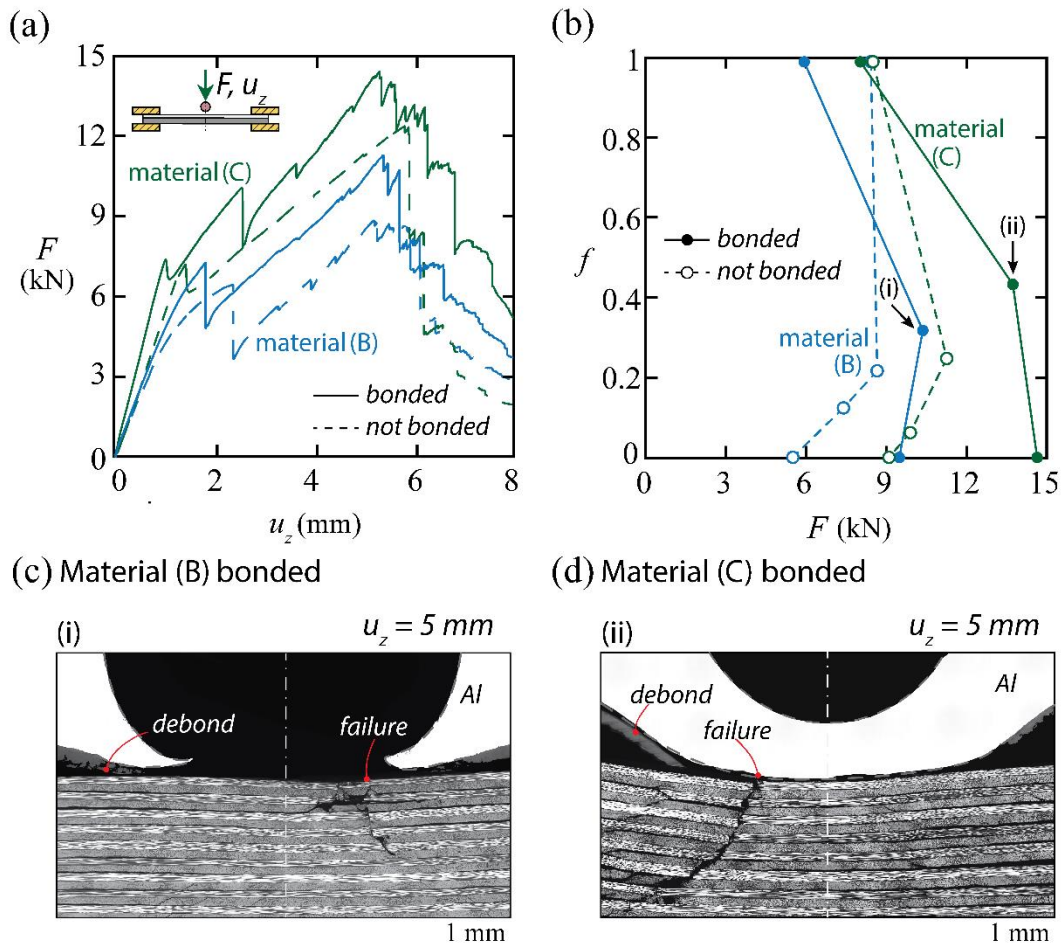


555  
 556 Fig. 8 Quasi-static indentation load-displacement responses of materials (A) and (C) under edge-  
 557 clamped and back-supported conditions in terms of normalised average pressure  $\bar{p}/p_f$  versus  
 558 displacement  $u_z$ .



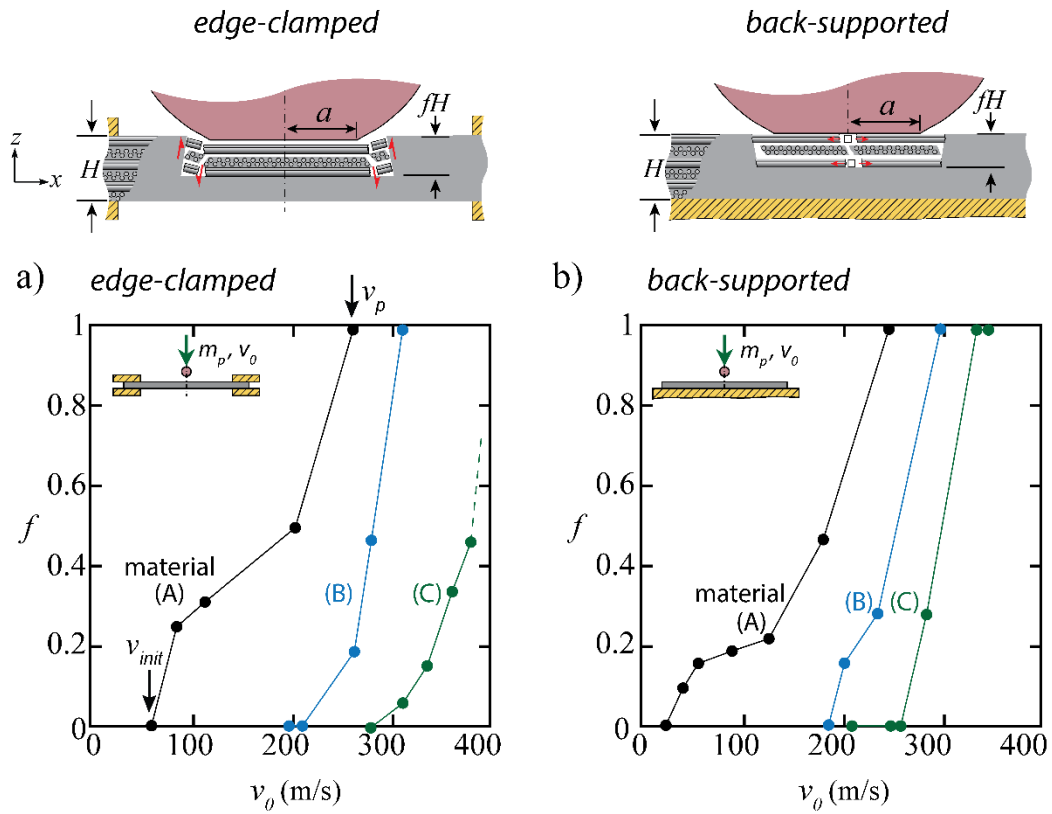
559

560 Fig. 9 The indentation cut fraction  $f$  in materials (A) to (C) versus indentation load  $F$  under  
 561 (a) edge-clamped and (b) back-supported conditions.



564 Fig. 10 Edge-clamped indentation response of bilayer material (B) and (C) with and without  
 565 bonding between layers. (a) indentation load  $F$  versus  $u_z$  and (b) indentation cut fraction  $f$   
 566 versus load  $F$ . (c)-(d) Cross-sectional micrographs of the bonded bilayer plates (B) and (C), after  
 567 testing to the indentation load  $F$  levels as labeled (i) and (ii) in Figure 11b.

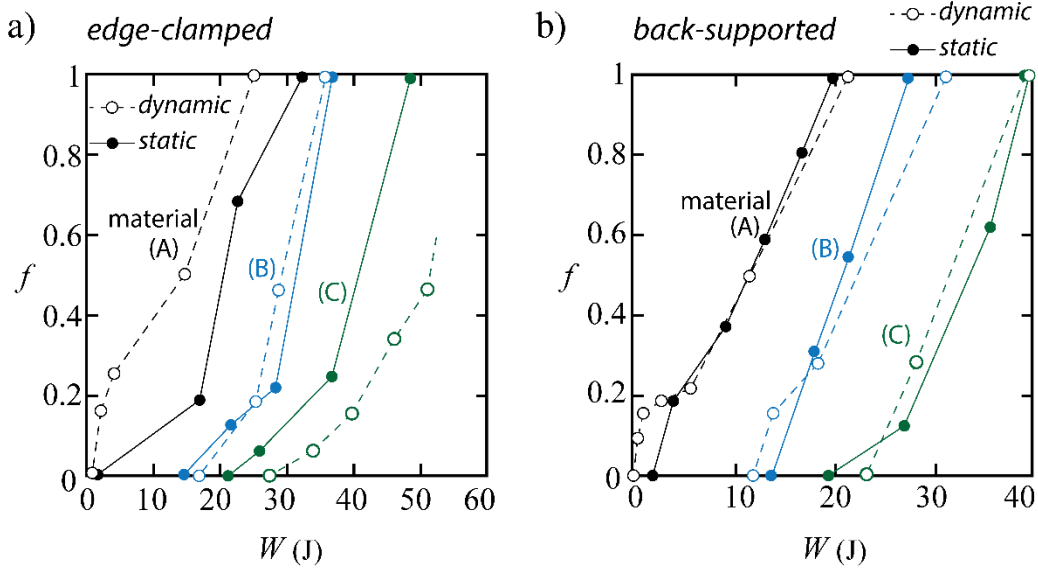




569

570 Fig. 11 The cut fraction  $f$  in materials (A) to (C) versus impact velocity  $v_0$  under (a) edge-  
 571 clamped and (b) back-supported conditions.

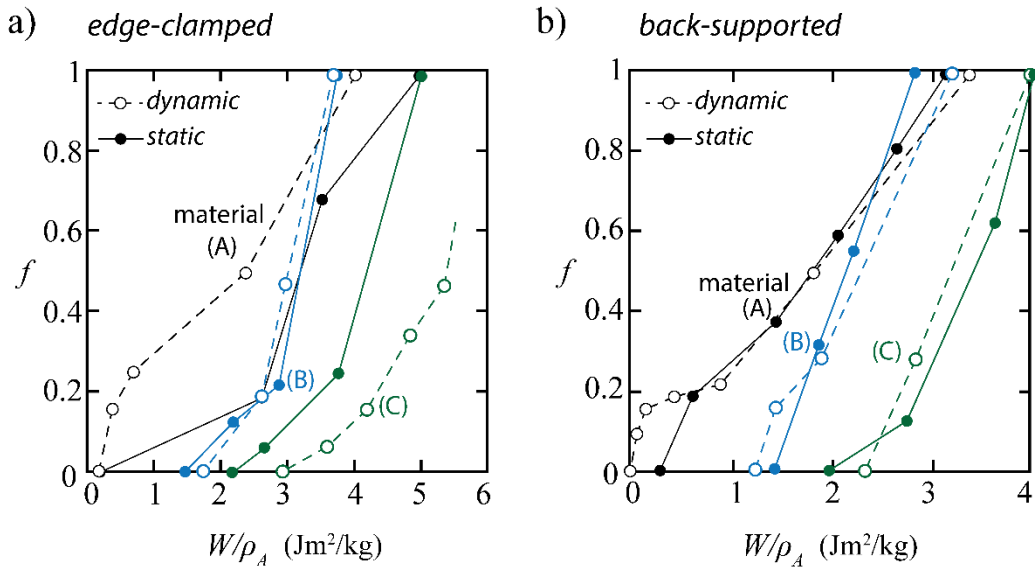




572

573 Fig. 12 Cut fraction  $f$  in materials (A) to (C) from quasi-static and dynamic tests versus energy

574 dissipation  $W$  under (a) edge-clamped and (b) back-supported conditions.



575

576 Fig. 13 Cut fraction  $f$  in materials (A) to (C) from quasi-static and dynamic tests versus specific

577 energy dissipation  $W/\rho_A$  under (a) edge-clamped and (b) back-supported conditions.