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ABSTRACT

A detailed temporal analysis of the spectral diffusion phenomenon in single photon emitting InGaN/GaN quantum dots (QDs) is performed via measurements of both time-varying emission spectra and single photon emission intensity autocorrelation times. Excitation dependent phenomena are investigated via the optical excitation of carriers into the GaN barrier material and also directly into InGaN. Excitation into InGaN reveals that the fastest environmental fluctuations occur on timescales as long as a few hundreds of nanoseconds: an order of magnitude longer than previously measured in GaN QDs. Such long time scales may in future allow for the generation of indistinguishable photons in spite of the fact that the experimentally measured linewidths are broad.

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Quantum dots (QDs) are promising structures for the development of single photon emitting devices^{1–4} and therefore are expected to find applications in several future quantum information processing applications such as teleportation,⁵ computation,⁶ sensing,⁷ and quantum key distribution.⁸ As a subset of thus-far investigated QD-based single photon emitters, III-nitride structures are of interest due to their widely tunable emission wavelength range,^{9–12} the possibility of operation at comparatively high temperatures,^{13–20} the possibility of high purity single photon emission,²¹ and also the large scale industrial infrastructure available for manufacturing and processing such materials. However, III-nitride QDs are currently known to suffer from severe spectral diffusion caused by strong Coulomb interactions between QD-confined charges and itinerant charges in the surrounding environment.^{22–27} This spectral diffusion will severely limit (and possibly negate) the possibility of indistinguishable photon generation^{28–31} from these structures, and thus demands a detailed investigation, particularly with regard to the time scales on which it occurs.

In this work, we report excitation dependent measurements of the long-term (occurring on time scales of seconds) and fast temporal scale ($\sim$ nanosecond) spectral diffusion phenomena in an isolated self-assembled InGaN/GaN QD. The QDs were grown on c-plane GaN/sapphire pseudo-substrates using a modified droplet

epitaxy method^{32–34} by Metal Organic Chemical Vapour Deposition on a 6×2 in. Thomas Swan close-coupled showerhead reactor and are situated in an etched micro-pillar structure containing porous DBRs (formed by electrochemical etching) for enhanced emission extraction efficiency.^{35,36} Due to the modified droplet epitaxy growth of the QDs, they form as part of a fragmented quantum well.^{32,37} Characterization of the QDs is performed optically using microphotoluminescence spectroscopy at a temperature of 7 K in a closed cycle cryostat under continuous wave (CW) laser excitation. Low temperature operation is required to suppress environmental fluctuations as much as possible. We excite the sample through a $50\times$ objective lens ($NA = 0.42$) to a spot size of $\sim 2 \mu\text{m}$, and the resulting photoluminescence is then collected with the same objective and collimated before being directed for measurement in a 30 cm spectrometer with a 1200 mm^{-1} diffraction grating. The spectrometer has two exit ports: One equipped with a nitrogen cooled CCD for the standard spectral measurement, and the other connected to a Hanbury Brown and Twiss (HBT) type autocorrelation setup, consisting of a beam splitter and two photomultiplier tube (PMT) detectors, for measuring temporal variations of the emission via the second order intensity autocorrelation function

FIG. 1. Microphotoluminescence spectrum and autocorrelation measurement of an isolated InGaN/GaN QD. The measurement of $g^{(2)}(0) < 0.5$ confirms the single photon nature of the emission. For these measurements, the emitter was excited with a 400 nm laser at a power of 255 W cm^{-2} , and emission from the whole peak (excluding the low energy acoustic phonon sideband) was measured for autocorrelation.

$$g^{(2)}(\tau) = \frac{\langle I(t+\tau) \cdot I(t) \rangle}{\langle I(t) \rangle^2}.$$

The exit slit of the spectrometer for this second port is used for spectral selection (i.e.: the spectrometer is used as a monochromator for filtering with a tunable bandwidth).

We begin by investigating the spectrum of a selected emitter at $\sim 2.74 \text{ eV}$ (450 nm) from which we confirm single photon emission (see Fig. 1) via a $g^{(2)}(0)$ measurement of 0.36 (below the 2-photon threshold of 0.5). In order to study the spectral stability of this emitter, we first measure and analyze temporal variations in the emission spectrum over a period of 1 h under excitation at 355 nm, 375 nm, and 400 nm (all experiments are performed at the same excitation power of $\sim 193 \text{ W cm}^{-2}$). These excitation wavelengths are chosen as they enable us to excite carriers into the surrounding GaN material (355 nm) and also directly into the InGaN layer (375 nm and 400 nm). In Fig. 2(a), we plot 2D color maps of the emission spectra as they vary with time. In all cases, we observe a clear fluctuation in the emission energy of the dot, occurring on time scales on the order of a few

seconds, as is typically observed in III-nitride QDs.^{26,38,39} We integrate these spectra to acquire averaged emission spectra for each excitation wavelength, which we present in Fig. 2(b). We extract an average linewidth at each excitation wavelength [see Fig. 2(c): the error bars come from the standard deviation of the fitting results from each spectra] and also perform a Fourier analysis of time varying emission energies [see Fig. 2(d)]. From the figures, it is clear that tuning the excitation wavelength from 355 nm to 400 nm results in a significant suppression of the spectral diffusion effects, i.e., we observe a suppression of the total 1-h averaged linewidth (from $\sim 4.5 \text{ meV}$ down to $\sim 1.7 \text{ meV}$) and also a suppression of all measured frequencies of oscillation in the Fourier Transform.

This suppression of spectral diffusion on the measured time scales provides a route for optically improving the quality of the emission and can be understood in the framework of a standard model of a series of charge traps in the vicinity of the dot which cause shifts in the emission energy of the dot when they change their charge status.^{22,40} By tuning the excitation energy much lower than the GaN bandgap, we selectively excite carriers in only the InGaN layer, and the excited carriers can therefore access traps that exist only within the InGaN. This reduced number of accessible traps leads to a suppression of the spectral diffusion. The relatively large emission peak jumps that appear under excitation at 355 nm are likely due to the existence of a charge trap in the GaN region that is in close proximity to the dot.

The charge traps likely consist of a mix of crystal point defects, dislocations, and other potential fluctuations such as indium composition fluctuations. It is also possible that other non-optically active quantum dots also contribute to the fluctuating electronic environment as they become charged and discharged. Indeed, we estimate that for every optically active QD there may be up to a few tens of non-optically active structures.^{27,34}

While measuring such spectral diffusion on these large time scales is important to understand the dynamics that play a role in the emission properties of the dots, it is actually the environmental fluctuations that occur on the fastest time scale that are the most important. This is because it is the fastest time scale of the spectral jumps that will determine how many photons can be generated before the emission energy shifts. Unfortunately, the measurement described above cannot

FIG. 2. Microphotoluminescence from the studied single InGaN/GaN QD. (a) Temporal variation of the emission spectra of a single emitter measured over a period of 1 h at excitation wavelengths of 355 nm, 375 nm, and 400 nm (all the same excitation power of 193 W cm^{-2}). (b) Integrated emission spectra from the data in (a). (c) Excitation wavelength dependence of the emission linewidth [extracted from the data in (b)]. (d) Fourier transforms of the fluctuations in the peak energies, showing a suppression of the magnitude of the spectral diffusion at all time scales for excitation below the GaN bandgap.

give access to such fast time scales because the experiment is limited by the data acquisition times of the CCD to time scales greater than several milliseconds. The most important time scales of spectral diffusion in InGaN QDs have therefore not been measured to date. In the following, we investigate the spectral diffusion effects on nano-second time scales for this dot using autocorrelation measurements typically used for single photon characterization. More specifically, we perform photon autocorrelation measurements whilst spectrally selecting only a small part of the emission peak,⁴¹ as illustrated in Fig. 3. The temporal resolution of this experiment is determined by the combined response functions of our PMTs to be ~ 370 ps. By selectively measuring a narrower region of the peak for measurement, we are able to change the spectral fluctuations of the peak into intensity fluctuations due to the fluctuation of the emission in and out of the measurement window. Figure 3(a) shows the emission spectrum from our studied quantum dot along with a series of measurement windows (full peak, 1/4 width, and 1/8 width). The corresponding autocorrelation traces are presented in Fig. 3(b). These measurements were all performed under 375 nm excitation at a power of 72 W cm^{-2} . The data are fitted with a typical model of an antibunched correlation with a single exponential bunching envelope.²³

As we become more spectrally selective with our filter, a pronounced bunching can be seen in the autocorrelation, characterized by $g^{(2)}(\tau) > 1$. The bunching appears because the data points for the autocorrelation histograms are acquired by the measurement of time differences between detected photons, and we are less likely to measure two photons with longer time differences because of an increasing chance that the spectral diffusion may have shifted the emission out of the measurement window at longer times. A measurement of the decay time in the bunching profile is thus a measurement of the characteristic time scale of the spectral diffusion⁴¹ or a measurement of how quickly the environment itself is fluctuating. In terms of the experiment, the bunching peak becomes increasingly visible for narrower spectral windows, with the requirement of longer data acquisition times (the time required to measure a given signal grows with the inverse square of the measured emission intensity). The widths of the

selected spectral windows have no influence on the measured fast spectral diffusion time scales but only on the degree of bunching.⁴¹

It is important to note that the bunching appears only when we selectively measure a fraction of the peak and is therefore not due to the presence of a real 3-level system⁴² in this case. However, we note that the results are in fact compatible with such an analysis: For example, we could artificially assign 3 levels to the system [(1) QD is occupied and emission energy is within the filter window, (2) QD is occupied and emission energy is blocked by the spectral filter, and (3) QD is empty]. In this picture, the spectral diffusion process shifts the emitter between states 1 and 2.

Analysis of the data in Fig. 3(b) reveals typical characteristic time scales of the bunching effect of ~ 260 ns, providing an upper limit of the time scale in within which indistinguishable photons could in principle be generated using these InGaN QDs (other sources of decoherence such as phonon interactions are likely to reduce this further). For time scales longer than this, environmental fluctuations will cause a change in the emission energy such that the emitted photons could in principle be distinguished by use of an optical system with a dispersive element. However, even though the energetic extent of the diffusion is large ($\sim \text{meV}$ levels—likely due to the large permanent dipole moment of the confined exciton²²), the time scale of the fluctuations is slow enough that the successive emission of several photons should be possible between fluctuations in the environment (the emission lifetime of the dot is measured to be ~ 1 ns). We note that this spectral diffusion time scale of 260 ns is longer than values reported in the literature for some other typical semiconductor QDs, such as ~ 10 – 20 ns in GaN/AlGaIn,²³ ~ 5 ns in CdSe/ZnSe,^{41,43} and comparable to some InGaAs/GaAs QDs which exhibit time scales of 90–1900 ns.⁴⁴ Although a direct comparison between different materials can be difficult, we note that the spectral diffusion times measured from these InGaIn quantum dots are an order of magnitude longer than those measured in GaN QDs,²³ despite the fact that the excitation power density is over an order of magnitude greater in this case.^{21,23} The relatively long spectral diffusion times measured here could be due to the existence of fairly deep charge traps (such that carrier escape and subsequent migration

FIG. 3. Spectral diffusion measurements using autocorrelation under 375 nm excitation with a power of 72 W cm^{-2} (a) Photoluminescence spectrum with a series of chosen measurement regions. (b) Corresponding 2nd order autocorrelations of the measurement windows in (a). The apparent bunching is due to spectral diffusion in and out of the measurement windows.

occur on long time scales). This may be somehow linked to the fragmentation of the quantum well that forms along with the QDs during the growth process or due to compositional fluctuations in the ternary material.

Next, we discuss the excitation wavelength and the power dependence of the time scale of the bunching. Similar to the long time scale diffusion shown in Fig. 2, we measure enhanced spectral diffusion for excitation into the barrier material. Indeed, as can be seen in Fig. 4(a), in which we present the inverse of the bunching time as a function of the excitation wavelength, we observe an increased spectral diffusion rate for excitation at 355 nm (with a corresponding bunching time of ~ 100 ns). As in the case of the long time scale measurement, the reason for this increase in the spectral diffusion rate here is due to an increased number of charge traps that can be excited by the 355 nm laser. With a larger number of excited electrons and possible trap states in the environment, it is more likely that the environment will change and cause a shift in the emission energy of the dot within a given time period. In Fig. 4(b), we present the power dependence of the spectral diffusion time scales under excitation of 375 nm. The data reveal a more or less linear increase in the spectral diffusion rate with increasing power, in good agreement with studies on other materials,^{23,43,45} and supporting the notion that the spectral diffusion dynamics are governed by single carrier processes (rather than multiple carrier processes such as Auger-assisted carrier escape from traps).

In conclusion, we have performed experimental characterization of the excitation wavelength dependence of the spectral diffusion effects in a spectrally isolated single-photon emitting InGaN/GaN quantum dot. We observe spectral diffusion occurring on timescales of a few seconds and also on timescales of a few hundreds of nanoseconds. Although the underlying physics is the same (interactions with fluctuating charge distributions in the local environment), we believe that different time scales arise due to different distributions of traps with different characteristic trap times. We find that direct excitation into InGaN leads to both a suppression of the spectral extent of the spectral diffusion and also a slowing down of its time scale. The fastest spectral diffusion can occur on time scales larger than 250 ns, which is one order of magnitude longer than that recently measured from GaN quantum dots (albeit with fluctuations that occur over a larger energy range). We have shown that even though the spectral diffusion limited linewidths of these emitters are broad, the time scales on which the

diffusion occurs are slow enough that indistinguishable photon generation should, in principle, be possible, provided that other sources of decoherence could also be sufficiently suppressed. Indeed, the measurements described here reveal that the average time between the environmental fluctuations that give rise to the measured broadened linewidths can be as large as a few hundred nanoseconds, so that in principle (neglecting other sources of decoherence), a few hundred photons could be emitted at the same energy in the time windows between environmental fluctuations. It is likely that the spectral diffusion could be further suppressed by using resonant excitation of carriers directly into the emitting state.

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REFERENCES

- P. Michler, A. Kiraz, C. Becher, W. Schoenfeld, P. Petroff, L. Zhang, E. Hu, and A. Imamoglu, *Science* **290**, 2282 (2000).
- J. C. Lored, N. A. Zakaria, N. Somaschi, C. Anton, L. De Santis, V. Giesz, T. Grange, M. A. Broome, O. Gazzano, G. Coppola *et al.*, *Optica* **3**, 433 (2016).
- N. Somaschi, V. Giesz, L. De Santis, J. C. Lored, M. P. Almeida, G. Hornecker, S. L. Portalupi, T. Grange, C. Anton, J. Demory *et al.*, *Nat. Photonics* **10**, 340 (2016).
- T. Miyazawa, K. Takemoto, Y. Nambu, S. Miki, T. Yamashita, H. Terai, M. Fujiwara, M. Sasaki, Y. Sakuma, M. Takatsu, T. Yamamoto, and Y. Arakawa, *Appl. Phys. Lett.* **109**, 132106 (2016).
- X. Wang, X. Cai, Z. Su, M. Chen, D. Wu, L. Li, N. Liu, C. Lu, and J. Pan, *Nature* **518**, 516 (2015).
- M. Kroutvar, Y. Ducommun, D. Heiss, M. Bichler, D. Schuh, G. Abstreiter, and J. Finley, *Nature* **432**, 81 (2004).
- H. Kimble, *Nature* **453**, 1023 (2008).
- E. Waks, K. Inoue, C. Santori, D. Fattal, J. Vuckovic, G. Solomon, and Y. Yamamoto, *Nature* **420**, 762 (2002).
- B. Daudin, *J. Phys. Condens. Matter* **20**, 473201 (2008).
- H. Sekiguchi, K. Kishino, and A. Kikuchi, *Appl. Phys. Lett.* **96**, 231104 (2010).
- S. Tomic, J. Pal, M. Migliorato, R. Young, and N. Vukmirović, *ACS Photonics* **2**, 958 (2015).
- B. Damilano, N. Grandjean, F. Semond, J. Massies, and M. Leroux, *Appl. Phys. Lett.* **75**(7), 962 (1999).
- S. Kako, C. Santori, K. Hoshino, S. Götzinger, Y. Yamamoto, and Y. Arakawa, *Nat. Mater.* **5**, 887 (2006).
- S. Deshpande, T. Frost, A. Hazari, and P. Bhattacharya, *Appl. Phys. Lett.* **105**, 141109 (2014).
- M. Holmes, K. Choi, S. Kako, M. Arita, and Y. Arakawa, *Nano Lett.* **14**, 982 (2014).
- S. Kako, M. Holmes, S. Sargent, M. Burger, D. As, and Y. Arakawa, *Appl. Phys. Lett.* **104**, 011101 (2014).
- M. Holmes, S. Kako, K. Choi, M. Arita, and Y. Arakawa, *ACS Photonics* **3**, 543 (2016).
- F. Le Roux, K. Gao, M. Holmes, S. Kako, M. Arita, and Y. Arakawa, *Sci. Rep.* **7**, 16107 (2017).
- T. Wang, T. J. Puchler, T. Zhu, J. C. Jarman, L. P. Nuttall, R. A. Oliver, and R. A. Taylor, *Nanoscale* **9**, 9421 (2017).
- S. Gong, S. Kim, J. Kim, J. Cho, and Y. Cho, *ACS Photonics* **5**, 711–717 (2018).
- M. Arita, F. Le Roux, M. Holmes, S. Kako, and Y. Arakawa, *Nano Lett.* **17**, 2902 (2017).
- M. Holmes, S. Kako, K. Choi, M. Arita, and Y. Arakawa, *Phys. Rev. B* **92**, 115447 (2015).
- K. Gao, I. Solovev, M. Holmes, M. Arita, and Y. Arakawa, *AIP Adv.* **7**, 125216 (2017).

FIG. 4. (a) Spectral diffusion rates as a function of excitation wavelength (measurements performed at 7 K with an excitation power of 193 W cm^{-2}). (b) Spectral diffusion rates as a function of excitation power (measurements performed at 7 K with an excitation wavelength of 375 nm).

- ²⁴C. Kindel, G. Callsen, S. Kako, T. Kawano, H. Oishi, G. Honig, A. Schliwa, A. Hoffmann, and Y. Arakawa, *Phys. Status Solidi RRL* **8**(5), 408 (2014).
- ²⁵S. Sergent, S. Kako, M. Burger, T. Schupp, D. As, and Y. Arakawa, *Appl. Phys. Lett.* **105**(14), 141112 (2014).
- ²⁶R. Bardoux, T. Guillet, P. Lefebvre, T. Taliercio, T. Bretagnon, S. Rousset, B. Gil, and F. Semon, *Phys. Rev. B* **74**, 195319 (2006).
- ²⁷B. Reid, T. Zhu, T. Puchtler, L. Fletcher, C. Chan, R. Oliver, and R. Taylor, *Jpn. J. Appl. Phys., Part 1* **52**, 08JE01 (2013).
- ²⁸C. Santori, D. Fattal, J. Vuckovic, G. Solomon, and Y. Yamamoto, *Nature* **419**, 594–597 (2002).
- ²⁹H. Wang, Y. He, Y. Li, Z. Su, B. Li, H. Huang, X. Ding, M. Chen, C. Liu, J. Qin *et al.*, *Nat. Photonics* **11**, 361–365 (2017).
- ³⁰T. Huber, A. Predojević, D. Föger, G. Solomon, and G. Weihs, *New J. Phys.* **17**, 123025 (2015).
- ³¹T. Santana, Y. Ma, R. Malein, F. Bastiman, E. Clarke, and B. Gerardot, *Phys. Rev. B* **95**, 201410(R) (2017).
- ³²R. A. Oliver, G. A. Briggs, M. J. Kappers, C. J. Humphreys, S. Yasin, J. H. Rice, J. D. Smith, and R. A. Taylor, *Appl. Phys. Lett.* **83**, 755 (2003).
- ³³T. Zhu, F. Oehler, B. P. L. Reid, R. M. Emery, R. A. Taylor, M. J. Kappers, and R. A. Oliver, *Appl. Phys. Lett.* **102**, 251905 (2013).
- ³⁴T. Zhu, H. A. R. El-Ella, B. Reid, M. J. Holmes, R. A. Taylor, M. J. Kappers, and R. A. Oliver, *J. Cryst. Growth* **338**, 262 (2012).
- ³⁵H. P. Springbett, K. Gao, J. Jarman, T. Zhu, M. Holmes, Y. Arakawa, and R. A. Oliver, *Appl. Phys. Lett.* **113**, 101107 (2018).
- ³⁶T. Zhu, Y. Liu, T. Ding, W. Y. Fu, J. Jarman, C. X. Ren, R. Vasant Kumar, and R. A. Oliver, *Sci. Rep.* **7**, 45344 (2017).
- ³⁷A. Woolf, T. Puchtler, I. Aharonovich, T. Zhu, N. Niu, D. Wang, R. Oliver, and E. L. Hu, *Proc. Natl. Acad. Sci.* **111**, 14042 (2014).
- ³⁸J. H. Rice, J. W. Robinson, A. Jarjour, R. A. Taylor, R. A. Oliver, G. A. D. Briggs, M. J. Kappers, and C. J. Humphreys, *Appl. Phys. Lett.* **84**, 4110 (2004).
- ³⁹M. J. Holmes, M. Arita, and Y. Arakawa, *Semicond. Sci. Technol.* **34**, 033001 (2019).
- ⁴⁰S. A. Empedocles and M. G. Bawendi, *Science* **278**, 2114 (1997).
- ⁴¹G. Sallen, A. Tribu, T. Aichele, R. André, L. Besombes, C. Bougerol, M. Richard, S. Tatarenko, K. Kheng, and J. Poizat, *Nat. Photonics* **4**, 696 (2010).
- ⁴²T. T. Tran, S. Choi, J. A. Scott, Z.-Q. Xu, C. Zheng, G. Seniutinas, A. Bendavid, M. S. Fuhrer, M. Toth, and I. Aharonovich, *Adv. Opt. Mater.* **5**, 1600939 (2017).
- ⁴³G. Sallen, A. Tribu, T. Aichele, R. André, L. Besombes, C. Bougerol, M. Richard, S. Tatarenko, K. Kheng, and J. Poizat, *Phys. Rev. B* **84**, 041405(R) (2011).
- ⁴⁴M. Abbarchi, T. Kuroda, T. Mano, M. Gurioli, and K. Sakoda, *Phys. Rev. B* **86**, 115330 (2012).
- ⁴⁵J. Wolters, N. Sadzak, A. Schell, T. Schroder, and O. Benson, *Phys. Rev. Lett.* **110**, 027401 (2013).