

1 Towards Enduring Autonomous Robots via Embodied Energy

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14 15 Preface:

16
17 Autonomous robots are comprised of actuation, energy, sensory, and control systems built from
18 materials and structures that are not necessarily designed and integrated for multifunctionality.
19 Yet, animals and other organisms that robots strive to emulate contain highly sophisticated and
20 interconnected systems at all organizational levels, which allow multiple functions to be performed
21 simultaneously. Herein, we examine how system integration and multifunctionality in nature
22 inspires a new paradigm for autonomous robots that we call *Embodied Energy*. Currently, most
23 untethered robots use batteries to store energy and power their operation. To extend operating
24 times, additional battery blocks and supporting structures must be added, which increases weight
25 and reduces efficiency. Recent advancements in energy storage techniques enable chemical or
26 electrical energy sources to be embodied directly within the structures, materials, and mechanical
27 systems used to create robots. This perspective highlights emerging examples of Embodied
28 Energy, focusing on the design and fabrication principles of enduring autonomous robots.

29 30 31 Manuscript Body:

32 33 Embodied Energy: a new paradigm for robotics

34
35 Power and control remain major barriers to the realization of untethered autonomous robots that
36 can move and adapt on demand for long duration missions. A close synergy between active
37 systems is needed to optimally use the, often limited, onboard energy supply. Recent examples
38 highlight a pathway towards improved operational lifetimes through the co-integration of chemical
39 and electrical energy sources with mechanical systems to imbue robots with high energy and power
40 density¹⁻⁵. By housing the energy supply directly within the robot's architecture and materials, it
41 is readily available for use, can be efficiently converted into useful work and, ideally, can be
42 replenished through onboard energy harvesting mechanisms. We call this design philosophy
43 *Embodied Energy*, where the same mass that normally provides a vital mechanical or structural
44 function also contains stored energy that powers at least a portion of the robot or device.

45
46 The potential of Embodied Energy systems can be evaluated through biological analogy. In
47 humans and other animals, energy is primarily stored in the body as fat. However, the
48 functionalities of adipose tissue extend far beyond energy storage to include insulation, the

49 protection of vital organs, waterproofing, and the regulation and production of hormones.
50 Embodied Energy can similarly imbue robotic systems with multifunctionality. For example,
51 batteries can be configured to serve load-bearing or architectural functions. Compliant materials
52 and actuators can provide structure while storing and reusing elastic energy.

53
54 In many ways the underlying principles of Embodied Energy parallel those currently employed in
55 robotic artificial intelligence systems. AI-driven robots interact with their environment based on
56 information previously gathered and processed from their surroundings via onboard sensors. This
57 closed sense-decide-response loop is reliant on a continuous synergy between the sensors,
58 processors, actuators, and collected data. The same should be true for the energy harvesting-
59 storage-delivery loop in robots with Embodied Energy. If these systems can fulfill energy and
60 power needs as well as actuation and control functions, we can create robots that more seamlessly
61 interface with their own environments.

62
63 Over the past two decades, there has been a small, but growing, effort to improve machine
64 autonomy by developing multifunctional, Embodied Energy systems^{4,5}. Most robots, however, still
65 contain isolated power, actuation, sensory, and control *blocks*, each optimized for an individual
66 task (Fig. 1)^{1,3,6-8}. In Honda's ASIMO robot, for example, there is a clear division between the
67 actuators in the joints, the control module in the torso, and the batteries in the backpack unit⁶. Such
68 isolated building blocks lack the synergy and efficiency observed in living organisms (e.g., the
69 pictured octopus), which are capable of harvesting, storing, and generating energy either
70 continuously or on demand. By distributing energy sources throughout multifunctional system
71 configurations, as illustrated by the progression of innovative robots and their corresponding block
72 diagrams in Fig. 1, we can expand their range of complex functions while increasing their
73 operational efficiency.

74 75 **Energy storage and conversion**

76
77 An important aspect of Embodied Energy design is precisely how this energy is harvested, stored,
78 applied, and recovered throughout the robotic system. Most untethered robot designs are guided
79 by a simple tradeoff between size, weight, and power. However, by broadening the range of
80 functionalities concurrent in a material or subsystem and distributing the mass budgets between
81 them, we can upend the conventional energy budget and design methodology. Power, sensing,
82 computation, and control will be largely native to the mechanical system.

83
84 Fig. 2 details concepts that are important to consider when designing for Embodied Energy.
85 Several robotic Embodied Energy systems, each representing a specific energy storage and
86 transduction methodology, are exemplified here. Though energy storage can take many forms in
87 mechanical systems, we limit our depiction here to five of the most common types that can be
88 harnessed by autonomous robots: electrical, mechanical, chemical, magnetic, and thermal. Several
89 of these categories overlap in conventional systems (e.g., electrochemical batteries,
90 thermochemical heat storage), a property that can be leveraged when merging different energy
91 storage and transduction technologies. Systems that store energy can vary wildly in their efficiency
92 (see Extended Data Table 1), material composition, and even the states of matter they interface
93 with (e.g., solid state batteries, liquid redox flow batteries, and gaseous hydrogen fuel cells).
94 Similarly, the landscape of energy transduction mechanisms (e.g., electromagnetic motors,
95 combustion engines, hydraulic pistons, etc.) is vast, complicating design decision making.

96

97 The intersection of energy storage and transduction will form the framework of our discussion, as
98 Embodied Energy seeks to accomplish these tasks collectively. Generally speaking, Embodied
99 Energy is best discussed in the context of robotics by examining its conversion to mechanical work
100 (i.e., actuation and locomotion). In the sections that follow, we will present existing technologies
101 that can transduce different types of stored energy into mechanical actuation in robots. We will
102 describe how these technologies can be implemented in multifunctional Embodied Energy
103 systems, citing existing examples, and discuss future developments for each energy transduction
104 category, concluding with an examination of nine Embodied Energy design principles.

105

106 *1. Electrical to mechanical transduction:*

107

108 Untethered robots and their mechanical actuators are predominantly powered by rigid rechargeable
109 batteries (e.g., lithium-ion, lithium-polymer, nickel-metal hydride, etc.). Some of the earliest
110 notable cases of multifunctional energy storage involve structural power sources^{5,9,10}, where static,
111 load-bearing components of machinery also supply electrical energy. A simple example is the use
112 of lead-acid batteries in forklifts as counterbalance for lifting heavy loads¹¹. More sophisticated
113 Embodied Energy examples include structural batteries in satellites¹², spacecraft¹³ and electric
114 vehicles^{4,14}, lithium-polymer batteries that function as wings in unmanned aerial vehicles
115 (UAVs)⁹, pliable, biomorphic zinc-air batteries that can serve as protective covers for robots¹⁵, and
116 flexible galvanic thin-film batteries in flapping wing aerial vehicles (FWAVs)¹⁶. In the latter
117 example, the use of embodied electrical energy sources increased the operating time of an FWAV
118 by 250% relative to designs using standard batteries and conventional wing materials.

119

120 The conversion of electrical energy to mechanical actuation is most commonly accomplished in
121 robots by electric motors, though they do not store their own onboard energy. Electroactive
122 polymers (EAPs), so-called because they change size or shape in response to electric stimulus, are
123 a class of materials that are capable of multifunctional energy storage. They have the capacity to
124 quickly ($t \sim 10^{-3}$ – 10^{-4} s) undergo large reversible strains ($\epsilon_{ult} > 300\%$)^{17,18} making them an attractive
125 option for robots with muscle-like actuators^{17–19} and sensing capabilities^{20,21}. EAPs can broadly be
126 classified as either electronic (e.g., electrostatic, electrostrictive, and ferroelectric polymers) or
127 ionic (e.g., gels and ionic polymer-based composites) depending on their mode of action¹⁸.

128

129 Dielectric elastomer actuators (DEAs), a class of soft electrostatic transducers belonging to the
130 electronic group, have been performing multifunctional electrical to mechanical energy conversion
131 for decades²². During operation, DEAs store energy throughout their structure, with elastomer
132 layers functioning as deformable capacitors. Consequently, DEAs can serve simultaneously as
133 actuators, sensors, and energy harvesters²³. DEAs have been implemented in crawling^{24,25},
134 gripping²⁶, swimming^{27–29}, and even flying robots³⁰, while more recently introduced soft
135 electrostatic transducers (e.g., hydraulically amplified self-healing electrostatic (HASEL)
136 actuators^{31,32}) have combined solid and liquid dielectrics to produce additional functionalities,
137 including hydraulic and pneumatic³³ actuation modes. Unlike conventional electric motors, soft
138 electrostatic transducers inherently store electrical energy and can assume “catch states”, where
139 negligible power is consumed while holding a position. When used in a multifunctional manner,
140 soft electrostatic transducers provide a rich opportunity for Embodied Energy in robots, and have
141 already been used for high frequency, high amplitude actuators^{32,34,35}

142

143 Ionic polymer-metal composites (IPMCs) have also been used in the creation of mobile robots^{36–}
144 ³⁸. Composed of a thin conductive polymeric material placed between two metal electrodes, IPMCs
145 use the transport of ions into and out of the polymer for actuation. Though they generally produce
146 lower actuation forces compared to soft electrostatic transducers, their ability to operate at low
147 voltage ($V_{in} \sim 1\text{-}5\text{ V}$, vs $V_{in} > 100\text{ V}$ for DEAs) and also generate a small voltage in response to
148 deformation has made IPMCs both useful actuators and sensors in biomedical and engineering
149 applications^{21,39–41}.

150
151 We anticipate future improvements not just in the energy density of batteries, but also in the
152 materials used in their composition⁴². Batteries with tunable mechanical properties could serve a
153 variety of functions outside of traditional energy storage, expanding the benefits of Embodied
154 Energy to a wider array of robot designs. As exemplified in Fig. 2, a stretchable battery can
155 theoretically be used as an extensible tendon in a walking robot or a wearable exosuit, thus
156 combining electrical and elastic energy storage into a structural element that connects different
157 system components. Fluidic energy storage using flow battery technologies is also a key
158 innovation in this domain. For example, in 2019, a soft robotic fish was created with an embedded
159 “electrolytic vascular system¹.” This design was inspired by redox flow batteries and consisted of
160 a distributed liquid electrolyte that also served as a hydraulic fluid. This multifunctional use of
161 electrochemical energy storage enabled simultaneous power generation and fluidic actuation,
162 which allowed the fish to swim for long durations (>36 h).

163 164 2. Mechanical to mechanical transduction: 165

166 There are many methods for converting stored mechanical energy into motion, including springs,
167 linkages, gear trains, cams and followers, etc. However, multifunctional and embodied
168 applications are far less common in modern machinery. One use case that has been explored is the
169 inclusion of flywheels in spacecraft to both store energy and provide torque for attitude and
170 control^{43–45}.

171
172 For robots, one pathway towards improved mechanical energy management involves
173 advancements in high energy density materials, composites, and interfacial chemistry that can
174 replace or supplement existing mechanisms. The field of soft robotics has provided such a platform
175 for the latest innovations in Embodied Energy due to the vast design space offered by the high
176 strain capabilities ($\epsilon_{ult} > 1,000\%$), range of stiffnesses ($E \approx 1 - 10^5\text{ kPa}$), and durability of soft
177 matter, such as silicone elastomers, hydrogels, and polyurethane rubbers⁴⁶. Other characteristics
178 of soft robots, including their ability to be fabricated via additive manufacturing methods (e.g., 3D
179 printing and soft lithography)⁴⁷, the existence of well-established actuation techniques (e.g.,
180 fluidic, electrostatic)^{46–48}, adaptability, and human compatibility, all motivate synergistic
181 applications for multifunctional and efficient power conversion technologies.

182
183 Soft robotics has historically embraced the storage or tuning of elastic energy in elastomeric
184 structures for improved efficiencies and high-power actuation. Recent work has pushed this further
185 by harnessing materials and geometric nonlinearities to discretize the actuator response. Some
186 nonlinear soft actuators, for example, are characterized by instabilities that cause the actuator to
187 undergo a snap-through response, where a fast motion with a large stroke follows from a small
188 external input. During the snapping phase, the elastic energy stored in the actuator structure is
189 suddenly released and can be redirected towards the external world. This principle was recently

190 exploited in the fabrication of bistable hybrid soft actuators inspired by the spinal flexion of
191 mammalian quadrupeds⁴⁹. In another example, stored pressure-volume mechanical work was
192 harnessed to create a jumping robot consisting of spherical caps that leveraged a volumetric
193 instability⁵⁰. Embedded actuator sequencing has been achieved by connecting multiple nonlinear
194 balloon actuators, adding passive control to the energy conversion process^{8,51}. We see this snap-
195 through behavior in nature as well; a classic example is that of the venus flytrap⁵².

196
197 As robots continue to emulate biology and evolve towards hybrid hard-soft structures, there will
198 be additional opportunities to generate unified musculoskeletal systems that provide energy
199 storage, power, and structural functionality. Series elastic actuators (SEA), where a spring-like
200 element is placed between an actuator and the end effector, is perhaps the simplest example of this
201 concept. Fig. 2 highlights how this approach to Embodied Energy can be used to improve the
202 adaptability and durability of terrestrial robots. Integrating compliant elements like SEAs into
203 robot architectures could lead to greater shock tolerance, more accurate and stable force control,
204 lower reflected inertia, and decrease inadvertent damage to the environment, all while storing
205 energy⁵³. Advancements in manufacturing techniques will also inform future designs for hybrid
206 hard-soft robots that can structurally store mechanical energy. Multi-material additive
207 manufacturing represents a clear step towards this approach. An idealized process would be able
208 to dynamically tune the chemical and mechanical properties of a part during synthesis to produce
209 functionally graded composites and monolithic robots. Just as humans capture and reuse elastic
210 energy with their muscles and tendons, we also expect future robots to more commonly harvest,
211 store, and reuse energy from inertial forces⁵⁴.

212 213 *3. Chemical to mechanical transduction:*

214
215 Humans and other animals rely on chemical fuels like glucose and fat to serve as their primary
216 energy source for mechanical work. Similarly, combustion engines convert energy-dense
217 hydrocarbons into power for transportation, but the high temperatures required necessitate the use
218 of rigid and dense metal bodies (or frameworks) in most applications. Compressed, gaseous
219 hydrocarbon fuels have now been used for both variable compliance⁵⁵, as well as, when
220 combusted, high power density actuation in soft elastomeric robots². While the efficiency is not
221 yet high, the large energy density of these hydrocarbon fuels, along with their multifunctional
222 capabilities, can increase the high power performance and adaptability of these robots compared
223 to inert gases^{55,56}. More recently, liquid fuels have been implemented in multifunctional power-
224 structure-actuation systems to achieve cyclic movement in untethered robots⁵⁷. The “octobot”,
225 unveiled in 2016, employed a distributed chemical energy system (platinum-catalyzed H₂O₂
226 decomposition) coupled with a microfluidic logic circuit to autonomously achieve mechanical
227 actuation of the tentacles of a 3D printed octopus³.

228
229 We anticipate further advances by storing convertible fuel sources within intelligent structural and
230 machine elements. Autophagous systems are one such approach, wherein physical loads are borne
231 by structural components that also provide energy in a “self-consuming” process. Prior work in
232 this area has been explored for use in aerospace applications^{5,58}. The structural requirements for
233 launching vehicles into space greatly exceed those needed for normal operation; with the
234 components consequently sized for launch, the lifetime and efficiency of these vehicles would
235 increase by breaking down and harvesting energy from their excess materials. This same strategy
236 could be implemented in robots, and is supported by research involving autophagous metal-air

237 batteries⁵⁹, structural beams pressurized with gaseous fuels⁵⁸, and thermoplastic matrix composites
238 that can be converted to fuel and burned with liquid oxidizers⁶⁰.

239
240 Naturally, end-use applications must be carefully considered when designing autophagous
241 structure-power systems. The large energy density of solid fuels comes at the expense of ease-of-
242 servicing and long-term durability as the structure is depleted. Recyclable, biodegradable, and
243 single-use devices do show promise in applications including surveillance, exploration, and
244 medicine, but more traditional robots will need to prioritize refueling capabilities, possibly through
245 the use of modular designs, energy harvesting, and secondary or emergency means of power
246 generation to ensure perpetual functionality. One difficult challenge that can be envisioned is the
247 nonhomogeneous consumption of materials in autophagous systems. Using the autophagous
248 metal-air battery as an example, a localized catastrophic failure could incapacitate the system,
249 leaving a fraction of the remaining energy inaccessible. A solution to this problem is the use of
250 materials and configurations that leave behind residual structures that can still function in their
251 intended roles. Bimetallic shells could be used in configurations where only one of the two
252 compounds is consumed. Porous structures containing internalized liquid or adsorbed gaseous
253 fuels are another promising solution, as shown in Fig 2. A recent report described an ultraporous
254 ($7,310 \text{ m}^2 \text{ g}^{-1}$) metal-organic framework that can store large volumes of methane and hydrogen
255 gases that could be used to power vehicles, aircraft, and even robots⁶¹.

256 257 4. Magnetic to mechanical transduction: 258

259 The coupling of electricity and magnetism leads to a fair degree of overlap when discussing
260 magnetic energy storage applications. Energy can be stored in the magnetic field of an inductor or
261 a superconducting coil (a process called superconducting magnetic energy storage, or SMES), for
262 example, but current flow is required. Many robotic components and actuators, including motors,
263 valves, pumps, solenoids, switches, and relays all leverage this same basic electromagnetic
264 principle: a conducting coil produces a magnetic field when energized by an electric current, which
265 in turn induces movement in a magnetic body.

266
267 Many improvements to magnetic actuators have been realized over the past few decades, most
268 recently with regard to smaller size scales and the adoption of different substrate materials⁶²⁻⁶⁵.
269 Magnetic microrobots, in which the body and magnet are mostly one and the same, represent an
270 exciting new set of capabilities, especially in the biomedical or *in vivo* realms⁶⁶⁻⁶⁸. Constructing
271 the robot from magnetic materials allows the transduction of magnetic energy into mechanical
272 motion to be embodied at the structural level. While remote power generation eliminates the need
273 for an integrated energy storage system, external control via bulky, stationary magnetic coils
274 restricts the scope of these robots to some degree.

275
276 Though examples are limited, magnetic actuation presents an excellent opportunity for Embodied
277 Energy technologies, as the coil and magnet configurations used for actuation can also be used for
278 energy harvesting (a magnet traveling through a coil will induce an electromotive force, while
279 electrically powered actuators can in turn move magnetic elements). One example is the use of
280 electromagnetic dampers^{54,69} within end effectors for proprioceptive force control, energy
281 generation, and locomotion, as demonstrated in Figure 2. Another example is the “Moball” robot,
282 which contains moveable, permanent magnets that can provide steering and enable rolling
283 movements by changing the device’s center of mass, in addition to generating energy by passively

284 oscillating within solenoids⁷⁰. Magnetic actuator technologies are also being expanded to non-rigid
285 materials; stretchable inductors for compliant power electronics^{71,72} are one interesting emerging
286 application.

287
288 Improvements in offboard magnetic control will be required for future robots to maximize the
289 potential of Embodied Energy in this domain. We can also envision coupling magnetic actuation
290 and energy harvesting/delivery with the existing electrical systems in larger robots to achieve
291 higher efficiencies and a wider range of functionalities.

292
293 *5. Thermal to Mechanical transduction:*
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295 Thermal to mechanical energy conversion is commonly accomplished by combustion engines,
296 which are ubiquitous in modern machinery. However, the mechanical complexity, weight, size,
297 and scaling limitations of heat engines complicate integration into other energy-power systems
298 and typically restrict them to larger applications in industry and transportation. Heat engines make
299 up for their lower efficiencies (efficiency $\eta \sim 25\text{--}40\%$)⁷³ relative to other energy transducers by
300 consuming high energy density reactants. One established technique for improving the efficiency
301 and expanding the utility of combustion engines is the capture and reuse of waste heat (e.g.,
302 through the use of exhaust gas heat recovery, organic Rankine cycle units, or thermoelectric
303 devices)^{73,74}. Another approach is to leverage an alternative fuel source shared by another onboard,
304 power-generating device. Hybrid electric vehicles represent a simple example where an electric
305 and thermal system can operate synergistically through the addition of an optimizing control
306 element. A related technology is combined heat and power (CHP), wherein fuel is used in the
307 concurrent production of electricity and thermal energy, the latter of which is efficiency captured
308 and used in processes like heating and cooling. The energy systems of future robots could all stand
309 to benefit through the incorporation of similar processes.

310
311 At smaller size scales, bimetallic strips are among the simplest technologies used for thermal
312 actuation. Heating a pair of thin, bonded metal parts with different coefficients of thermal
313 expansion will cause the strip to bend. Recently, this technique of coupling materials with different
314 thermal properties has been extended to soft matter to create fiber-based, muscle-like actuators
315 capable of producing large stroke cycles and withstanding high strain (in some cases $>1,000\%$)^{75,76}.

316
317 Thermophoresis, a phenomenon where temperature gradients cause particles to experience a net
318 force that may induce flow, represents another instance of thermal to mechanical energy
319 transduction. Over the past few decades there has been growing interest in using thermal gradients
320 to manipulate and propel micro/nano scale objects. Recent achievements in the medical field
321 include the creation of thermophoretic nanomotors that can target and penetrate cancer cells⁷⁷, and
322 the development of a micro-rocket robot that can be optically actuated through a bloodstream⁷⁸.

323
324 Shape memory polymers (SMPs) are another promising class of materials/actuators that can be
325 engineered to react to both thermal and magnetic stimuli. As their name suggests, SMPs are
326 capable of undergoing a shape transformation—the entropy-driven restoration of a prior
327 mechanical deformation—that is fast, reversible ($t_{\text{recovery}} < 1$ sec to minutes), and
328 reprogrammable⁷⁹. The favorable mechanical properties of SMPs, including high ultimate strains
329 ($\epsilon_{\text{ult}} < 800\%$), tunable stiffnesses ($E = 10^4\text{--}3$ GPa), and a wide range of transition temperatures
330 ($T_{\text{crit}} = -10\text{--}100$ °C)⁸⁰ have seen them used in medical devices^{81,82}, fabrics and wearables⁸³,

331 sensors⁸⁴, robots^{85,86}, and aerospace technologies⁸⁷. Additionally, the multifunctionality associated
332 with storing several different shape configurations within a single or composite material^{79,88,89},
333 which can serve as both a structure and an actuator⁸⁶, makes SMPs an attractive option for
334 Embodied Energy technologies. Shape memory alloys (SMAs) comprise a similar group of smart
335 materials that can return to their original forms when subjected to changes in temperature or
336 magnetic field strength. SMAs are typically stiffer than SMPs ($E \sim 28\text{--}83$ GPa, with generally
337 similar moments of inertia)⁸⁰ and while they possess limited strain capabilities ($\epsilon_{ult} < 8\%$)⁹⁰ their
338 high power densities ($\Gamma = 10^3\text{--}10^5$ kW m⁻³)⁴⁸ have contributed to their use in a wide array of robots
339 and actuators⁹⁰⁻⁹⁵.

340
341 With waste heat being a significant byproduct of many mechanical systems, it is easy to visualize
342 how SMAs and SMPs could be integrated and embodied within existing machine architectures to
343 improve energy efficiency, weight, or device performance. Both materials, for example, could be
344 used as structural or skin-like elements that actuate to allow thermoregulation in different
345 machines. Shape memory actuators could also be configured to respond to the waste heat of solar
346 energy harvesters or heat engines, or used in concert with thermoelectric or pyroelectric
347 devices^{96,97} (Fig. 2). A recent report detailed the creation of an insect-scale, autonomous crawling
348 robot containing a platinum-coated SMA artificial muscle that was powered via catalytic
349 combustion with an onboard methanol fuel supply⁹⁸. Another publication demonstrated how low-
350 grade waste thermal energy could be converted into electrical energy through the use of artificial
351 polymer muscles.⁹⁹ More than 120 W of electrical energy per kilogram of muscle were
352 successfully produced, which could be used in powering autonomous sensors.

353

354 *Embodied Energy design principles:*

355
356 Creating robots that effectively embody energy can be accomplished by optimizing for endurance
357 and operating time, while overcoming key design contradictions (e.g., increasing the energy
358 content of a robot while maintaining its volume.). To that end, we have identified several key
359 design principles that can be applied during robot development and production. Fig. 2 depicts how
360 these design principles can be used in both existing and hypothetical Embodied Energy
361 technologies.

362

363 1. *Design with size, weight, and power tradeoffs in mind.* While power density is inversely
364 proportional to weight and volume, operating time scales proportionally with size in
365 untethered robots. Using embedded, energy dense fuels is one approach to optimizing for
366 high power at smaller sizes. The prospect of integrated versus modular assembly represents
367 another aspect of this tradeoff. Modular designs can be easier to assemble, service, and
368 reuse. A complex and heavily integrated design can likely achieve higher performance and
369 should execute an array of self-sustaining functions, at the cost of simplicity in
370 maintenance.

371

372 2. *Integrate energy storage into structural elements.* Using batteries as structural elements
373 can eliminate the need for certain load bearing components. Mass or volume elements that
374 would normally bear loads can be reassigned to perform functions unrelated to energy
375 storage.

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3. *Make a system serve itself by performing auxiliary helpful functions.* Synergistic systems can improve machine autonomy while limiting the need for human intervention. Halogen lamps represent a simple example—they regenerate their own filament when in use through the redeposition of evaporated metal¹⁰⁰. Similarly, in the RFB-inspired electrolytic vascular system¹ the same liquid used for hydraulic actuation is also used for energy storage, and the pumping of this liquid recirculates the soluble ions to improve the rate of charge transfer.
 4. *Use hybrid hard-soft structures to create adaptable designs.* Using compliant, muscle-like materials can lead to durable robots that can dampen or even absorb and redistribute forces, traverse difficult terrains, and operate with many degrees of freedom.
 5. *Use composite or porous materials to store energy.* Composites can contain both structural and energy storing domains. Similarly, porous materials, as in the example of gas adsorbent metal lattices⁶¹, can form lightweight structures that house fuel or energy in their pores.
 6. *Harvest energy from the environment.* To achieve fully autonomous robots, we must equip them with the technology to extract energy from their surroundings. Motion-driven microgenerators and photovoltaic cells are among the most mature energy harvesting technologies¹⁰¹, though efficiency and power density limitations exist (see Supplementary Information for a discussion of energy harvesting).
 7. *Reuse waste energy.* Recovered energy can be reconverted into onboard power, as in exhaust gas heat recovery systems, or repurposed for a secondary function, such as heating and cooling in CHP systems.
 8. *Leverage resonance.* Robot efficiency and longevity can be increased by driving systems with parameters that lead to high amplitude outputs. Further, operating actuators at resonance will require less energy input (e.g., a pneumatically powered actuator may need to be inflated fewer times and endure less stress for an equivalent distance traversed).
 9. *Compensate for weight through interaction with the environment.* Machine morphology should be adapted to derive advantages from their surroundings. Hydrofoils are used to lift ships out of the water to reduce drag, and vortex strips are implemented in aircraft wing designs to improve lift¹⁰⁰. In nature, many aquatic animals achieve buoyancy due to their energy storing fat reserves.

Challenges and future advancements

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A universal methodology for characterizing and evaluating Embodied Energy systems in a design context has yet to be established. However, techniques for characterizing the advantages of multifunctional systems, in general, have been proposed. Johannisson et al. introduced a “residual performance methodology,” that involves comparing the specific properties (e.g., mass, shear strength, specific energy) of a multifunctional block with those of two or more monofunctional systems (e.g., structure, energy storage)¹⁰². Other approaches include establishing a multifunctional efficiency metric or directly calculating the change in a value of interest as a function of different design variables, though this relationship may not always be known. Thomas

424 et al. demonstrated this by modeling the flight endurance time of a hypothetical, electrically
425 powered UAV in terms of the relative masses of the onboard batteries, solar cells, and structure to
426 draw conclusions about the most effective multifunctional configurations⁵⁸.

427
428 To envision the potential efficacy of integrated energy storage and transduction systems, we
429 developed a multifunctional version of the classic Ragone plot¹⁰³, as shown in Fig 3. This graph
430 predicts the range of energy and power density values attainable by a theoretical, merged energy
431 storage and actuator system, based on the energy density, power density, and efficiency of the
432 component parts^{4,9,48,104–126} (see Fig. 3 legend for details). It is intended as a tool for exploring
433 different robot designs when energy and power requirements are known.

434
435 The pairs shown in Fig. 3 were selected based on complementary features or their usage in
436 previously reported prototypes (see Extended Data Table 1 for plotted values and their
437 corresponding references). The energy sources in these hypothetical combinations can be thought
438 of as fully embodied within their assigned energy transducer, where they will serve multiple
439 functions. Combinations 1–6, for example, can be thought of as structural battery configurations
440 used in concert with different electromechanical actuators. Combination 13 implies an engine or
441 turbine configuration that takes energy from the burning of its hydrocarbon support structure,
442 rather than a traditional fuel reservoir that serves a single energy storage function.

443
444 While the full scope of possible systems and combinations is impossible to sample, this data does
445 allow for a rough comparison of the energy content and output of different hypothetical Embodied
446 Energy arrangements. For example, combinations 10, 11, and 13 store energy as a hydrocarbon
447 fuel and are akin to autophagous power systems; however, despite possessing much greater energy
448 densities than many of the other systems, the upper bound of their power density range is not
449 significantly different from several battery and motor driven designs due to the low efficiencies
450 involved. The graph does not take into account mass budgets and efficiency penalties of
451 supplementary systems that may be necessary for the construction or operation of these
452 hypothetical systems. Similarly, this plot does not capture the additional functionalities or non-
453 energy storage characteristics that may be beneficial in certain designs (e.g., material
454 compatibility, scalability, or cost). All Embodied Energy technologies, along with their inherent
455 characteristics and design tradeoffs, must necessarily be evaluated in the context of their intended
456 environment and applications.

457
458 Embodied Energy both presents and promises to solve future challenges. Size, weight, and power
459 tradeoffs, for example, will always present difficulties to robotics researchers, particularly as
460 smaller robots and personal devices, each possessing significant payload restrictions and energy
461 requirements, are pursued. Microrobots present an extreme case, with many of the latest innovative
462 designs requiring an electric tether to deliver power¹²⁷. Several are limited to specialized
463 environments,¹²⁷ and most also forego conventional actuators (i.e., DC motors) due to fabrication
464 limitations as well as the unfavorable scaling of friction and electromagnetic forces¹²⁸. If the
465 advantages promised by microrobot technologies (e.g., swarm capabilities, exploration, search and
466 rescue, medical intervention) are to be realized, multifunctional design strategies employing
467 Embodied Energy must be pursued.

468

469 Other challenges must be overcome as well, including the need for new, compatible materials that
470 operate synergistically with existing technologies, as well as yet unimagined ones. Examples
471 include conductive and corrosion-resistant materials that could function as battery electrodes and
472 ion exchange membranes, energy-dense solid polymer fuels for autophagous systems, controllable
473 shape-morphing materials¹²⁹, and biocompatible materials that can be assembled into lightweight
474 composites composed of organic, inorganic, and even living matter. Advancements in additive
475 fabrication techniques across multiple scales, coupled with predictive (inverse) design will be
476 necessary to increase both the compositional and structural complexity of robots, and to realize
477 new levels of multifunctionality.

478
479 The tighter integration of sensing, actuation, control, and power towards biological size scales (i.e.,
480 organs and tissue) will realize first order improvements in robot autonomy. While synthetic
481 systems are striving to achieve tissue level autonomy, biohybrid ones already do. Consequently,
482 we expect research in this area to be fervently pursued in the immediate future. 3D printing will
483 also be an increasingly used tool; Direct Ink Writing,¹³⁰ PolyJet,¹³¹ and Digital Light
484 Processing^{132,133} have all been used to create complex robots with intricate internal networks out
485 of soft materials. The use of new, more energy dense materials will also provide new design tools
486 for directly printing robots. Finally, the direct chemical to mechanical conversion of energy, as
487 demonstrated with hydrocarbon fuels, will likely become increasingly used to provide the greater
488 energy densities and efficiencies required for biological magnitudes of endurance and adaptability.

489
490 Finally, the multifunctional energy storage paradigm we are attempting to codify can be further
491 separated into passive and active control. Within these logic mechanisms there is further
492 opportunity for multifunctionality; the structures themselves provide control (e.g., origami¹³⁴,
493 bistable beams^{135,136}, and elastomeric actuators¹³⁷⁻¹⁴⁰). In this context, information processing
494 becomes another material property embodied in the physics of the soft, architected structure,
495 enabling local computations that seamlessly integrate the sense-decide-response chain^{141,142}. For
496 example, networks of elastomeric light guides have demonstrated the information density and
497 sufficient sampling rates to classify deformation states through offboard neural network
498 training¹⁴³. Remarkably, the mechanical nonlinearity of elastomeric materials is even capable of
499 embodying recurrent neural network behavior; as demonstrated in the dynamics of a silicone
500 octopus arm¹⁴⁴. Embedded computation has the added benefit of requiring less energy, as the
501 information processing is inherently coupled to, or a by-product of, the deformation and
502 environmental loading. Embodied Energy and Embedded Computation, therefore, will be
503 intricately linked in the future of advanced robotics research.

504
505 The conjoined aspects of harvesting, storing, transforming, and releasing energy provide a unique
506 lens through which to view the evolution of autonomy and intelligence. Such considerations
507 similarly challenge roboticists to rethink how to design, program, and deploy their creations into
508 the world. The design principles that result from the proposed Embodied Energy paradigm have
509 the potential to yield new multifunctional energy storage systems that improve the multi-objective
510 optimization of robot endurance and adaptability. The frontier of this research lies in integrating
511 advancements in predictive multiscale design, multifunctional materials, digital manufacturing,
512 and robotics.

513
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862

863

864 **Figure Legends:**

865

866 **Fig. 1| Energy, control, and actuating systems in modern robots.** Energy storage elements are

867 highlighted in yellow, control elements are highlighted in green, and actuators are highlighted in

868 red for each robot. **a**, The ASIMO humanoid robot⁶. **b**, A multigait, quadrupedal soft robot

869 powered by a pneumatic tether⁷. **c**, An 8-degree-of-freedom walking robot with embedded

870 actuator sequencing and a single pneumatic input⁸. **d**, An untethered octopus-inspired robot

871 controlled by microfluidic logic and powered by the decomposition of a monopropellant fuel that

872 produces pneumatic actuation³. **e**, An untethered aquatic soft robot with a redox flow battery-

873 inspired vascular system that produces electrical energy and hydraulic actuation¹. **f**, The common

874 octopus. (*To provide a direct comparison with mobile robots **a–e**, we have highlighted the

875 primary actuators of the octopus: the tentacles. Note: There are secondary actuation and

876 sensory/control capabilities not depicted in this simplistic representation.)

877

878 **Fig 2| Energy storage and transduction form the framework of the Embodied Energy design**

879 **process.** The Embodied Energy technologies shown are created by storing a specific type of energy

880 into the structural or energy transduction components of a system. The images in the transduction

881 pathway depict, from left to right, an electric comb drive, a bistable mechanical actuator, a soft

882 combustion actuator, a magnetic solenoid actuator, and a thermally responsive gel. The variable

883 definitions are as follows: U = voltage, q = charge, H = magnetic field strength, B = magnetic flux
884 density, V = volume, S^0 = standard entropy, T = temperature, C = specific heat capacity, m = mass,
885 p = pressure, F = force, x = displacement, σ = mechanical stress, ϵ = strain. The acronyms are:
886 RFBs = redox flow batteries, SMES = superconducting magnetic energy storage, SHES = sensible
887 heat energy storage.

888
889 **Fig 3| Multifunctional Ragone plot of Embodied Energy storage and energy transducer**
890 **combinations.** Each pair of intersecting line segments (corresponding to a specific number and
891 color) represents the range of predicted energy density and predicted power density values for a
892 given energy storage and actuator combination, based on existing products and prototype
893 devices^{4,9,48,104–126}. Predicted energy density is the product of an energy source's energy density Z ,
894 efficiency α , and the efficiency η of the energy transducer where it is embodied. Predicted power
895 density is the product of an energy transducer's power density Γ , efficiency η , and the efficiency
896 α of the energy storage system in which it is embodied. [The intersection points of the line segment
897 pairs are arbitrarily chosen for visibility.]

898
899 **Extended Data Table 1| Energy density and power density of common energy storage and**
900 **actuator technologies**

901

902

903 **Supplementary Information:**

904

905 Supplementary information is available in the online version of this paper

906

907

908 **Acknowledgements:**

909

910 The authors thank the Office of Naval Research, Grant #N00014-20-1-2438, Air Force Office of

911 Scientific Research, Grant #FA9550-20-1-0254, and National Science Foundation, Grant

912 #EFMA-1830924

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914

915 **Author Contributions:**

916

917 R.F.S. and J.A.L. conceived of the concept. C.A.A., J.A.L., and R.F.S. drafted key elements of

918 the manuscript. C.A.A. researched, collected, and analyzed data. C.A.A., B.G., and E.M. drafted

919 figures. P.R.B., N.L., G.A.S., C.K., J.B., and F.I. assisted in editing and refining the vision.

920

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922 **Author Information**

923

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925 declare no competing financial interests. Correspondence and requests for materials should be

926 addressed to R.F.S. (rfs247@cornell.edu).

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ASIMO



Multigait soft robot



Sequenced robot



Octobot



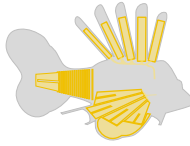
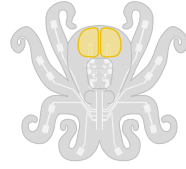
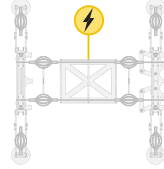
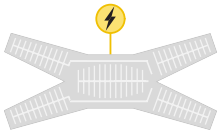
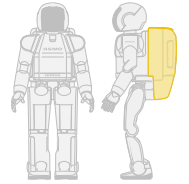
Vascular soft robot



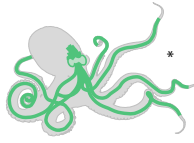
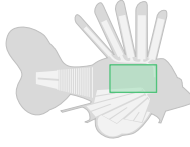
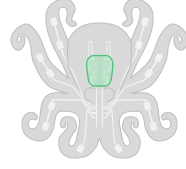
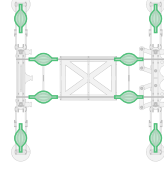
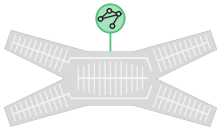
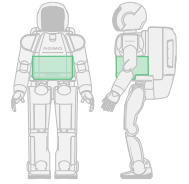
Common octopus



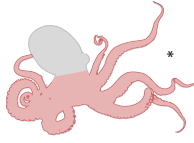
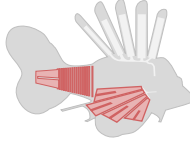
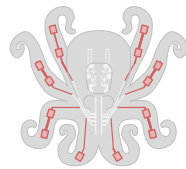
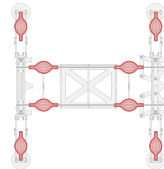
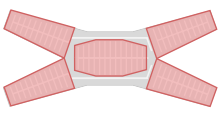
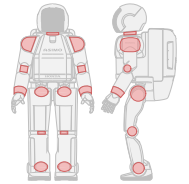
Energy



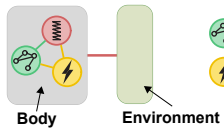
Control



Actuation



Schematic



Body Environment

Design challenge

- Batteries (electrochemical)
- RFBs (electrochemical)
- Supercapacitors

- Compressed air
- Flywheel storage
- Elastic storage

- Combustible fuels
- Fuel cells

- Inductive energy storage
- SMES

- Thermochemical storage
- Latent heat storage
- SHES

Energy storage

Electrical

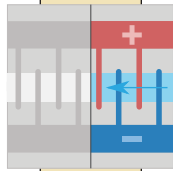
Mechanical

Chemical

Magnetic

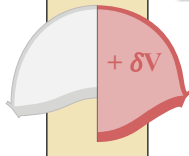
Thermal

$$\int U \cdot dq$$



$$\int F \cdot dx$$

$$\int p \cdot dV$$



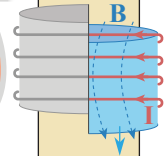
$$\int F \cdot dx$$

$$\int \Delta S^0 \cdot dT$$



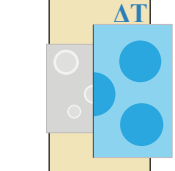
$$\int p \cdot dV$$

$$\frac{1}{2} \int H \cdot B \cdot dV$$



$$\int F \cdot dx$$

$$\int C \cdot m \cdot dT$$



$$\iint \sigma \cdot \epsilon \cdot dV$$

Transduction

Actuation

Motion

Motion

Motion

Motion

Motion

Embodied energy technology

Flexible battery as a tendon

Electrolyte as hydraulic fluid

Flywheel actuators

Autophagous structures

Gas adsorbant materials

Magnetic damping end effector

Phase change material in actuator

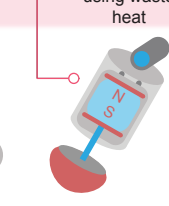
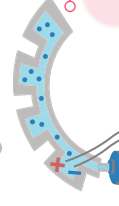
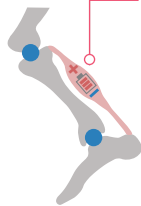
Series elastic actuators

Bistable or snap-through geometries

Pressurized gases for combustion actuation

Solenoid + magnet motion harvester

SMP generator using waste heat



Design concept

Compliance & adaptability

Size & weight

Operating time

Durability & reusability

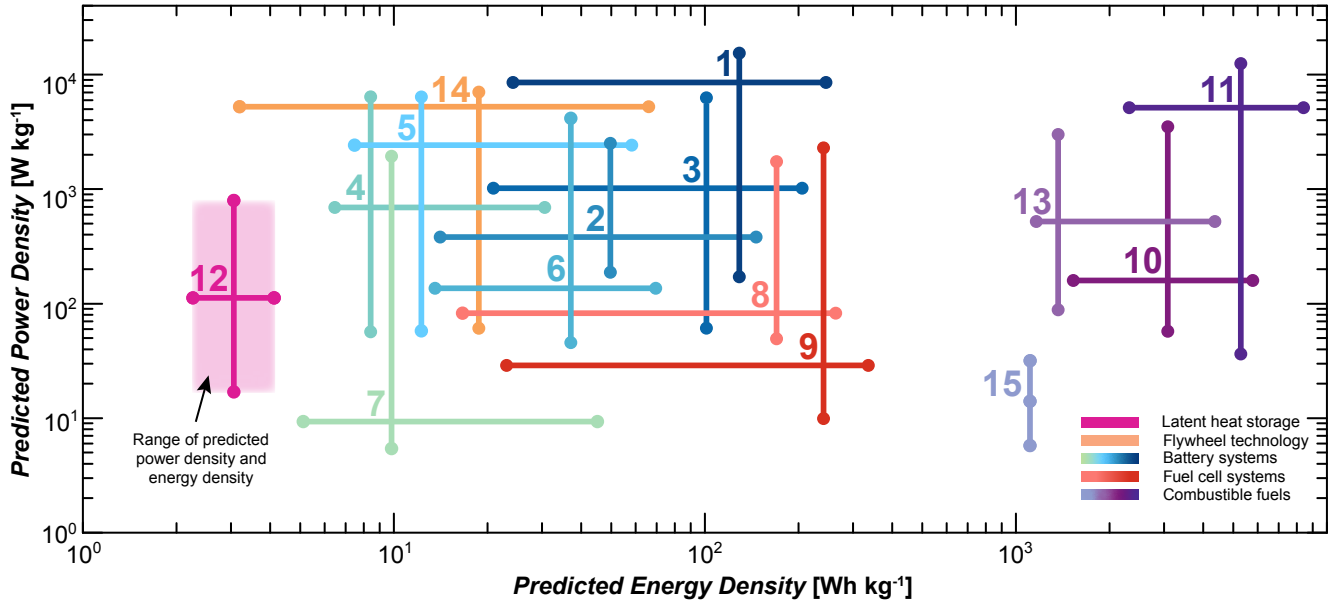
Force & power

Dexterity

Energy storage + structure

Energy storage + actuation

Energy storage + structure + actuation



- | | | |
|--|---|--|
| 1: Lithium Ion Battery - Piezo ($\alpha = 90\%$, $\eta = 90\%$) | 6: Ni Metal Hydride - AC/DC Motor ($\alpha = 65\%$, $\eta = 75\%$) | 11: Hydrocarbons - Hydraulic Actuator ($\alpha = 98\%$, $\eta = 60\%$) |
| 2: Lithium Ion Battery - DEA ($\alpha = 90\%$, $\eta = 57.5\%$) | 7: Redox Flow Battery - Pump ($\alpha = 74\%$, $\eta = 70\%$) | 12: Latent Heat Storage - SMA ($\alpha = 82.5\%$, $\eta = 2\%$) |
| 3: Lithium Ion Battery - AC/DC Motor ($\alpha = 90\%$, $\eta = 75\%$) | 8: Fuel Cell - Comb.Engine/Turbine ($\alpha = 59\%$, $\eta = 30\%$) | 13: Hydrocarbons - Comb.Engine/Turbine ($\alpha = 98\%$, $\eta = 30\%$) |
| 4: Lead Acid Battery - AC/DC Motor ($\alpha = 80\%$, $\eta = 75\%$) | 9: Fuel Cell - Pneumatic Actuator ($\alpha = 59\%$, $\eta = 40\%$) | 14: Flywheel - AC/DC Motor ($\alpha = 87\%$, $\eta = 75\%$) |
| 5: NiCd Battery - AC/DC Motor ($\alpha = 85\%$, $\eta = 75\%$) | 10: Hydrocarbons - Pneumatic Actuator ($\alpha = 98\%$, $\eta = 40\%$) | 15: Body Fat - Human Muscle ($\alpha = 41\%$, $\eta = 25\%$) |