

# Anomalous $tqV$ couplings and FCNC top quark production<sup>1</sup>

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## Abstract

We discuss FCNC top quark production via anomalous  $tqV$  couplings at the Tevatron and HERA colliders. We calculate higher-order soft-gluon corrections to such processes and demonstrate the stabilization of the cross section when these corrections are included.

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# 1 Introduction

Flavor-changing neutral-current (FCNC) processes involving the top quark appear in several models of physics beyond the Standard Model. The effective Lagrangian involving anomalous  $tqV$  couplings can be written as  $\Delta\mathcal{L}^{eff} = \frac{1}{\Lambda} \kappa_{tqV} e \bar{t} \sigma_{\mu\nu} q F_V^{\mu\nu} + h.c.$  where  $\kappa_{tqV}$  is the anomalous coupling, with  $q$  denoting an up or charm quark and  $V$  a photon or  $Z$ -boson with field tensor  $F_V^{\mu\nu}$ ;  $\sigma_{\mu\nu} = (i/2)(\gamma_\mu\gamma_\nu - \gamma_\nu\gamma_\mu)$  with  $\gamma^\mu$  the Dirac matrices; and  $\Lambda$  is an effective scale which we set equal to the top quark mass,  $m$ .

The present TeV energy scale colliders – Tevatron and HERA – can probe FCNC interactions in the top-quark sector and set limits on  $\kappa_{tq\gamma}$  and  $\kappa_{tqZ}$ . However, there are large uncertainties in the lowest-order results from variation of the factorization/renormalization scales,  $\mu$ . Therefore the stabilization of the cross section for these FCNC processes is timely and important. We have calculated next-to-leading order (NLO) and next-to-next-to-leading order (NNLO) soft-gluon corrections for the following processes:  $gu \rightarrow tZ$ ,  $gu \rightarrow t\gamma$ , and  $uu \rightarrow tt$  at the Tevatron [1]; and  $eu \rightarrow et$  at HERA [1, 2]. As a result, we show that inclusion of QCD corrections significantly stabilizes the cross sections.

## 2 FCNC top quark cross sections

We define  $s_4 = s + t + u - \sum m^2$ , with  $s, t, u$  standard kinematical invariants, and where the sum is over the masses squared of the particles in the scattering. At threshold  $s_4 \rightarrow 0$ . The soft-gluon corrections [3, 4] are of the form  $[(\ln^l(s_4/m^2))/s_4]_+$ , where  $l \leq 2n - 1$  for the order  $\alpha_s^n$  corrections. These corrections are expected to dominate the cross section in the near-threshold region, which is relevant for the processes studied here. The leading logarithms (LL) are those with  $l = 2n - 1$  while the next-to-leading logarithms (NLL) are those with  $l = 2n - 2$ . Here we calculate NLO and NNLO corrections in  $\alpha_s$  at NLL accuracy, i.e. keeping LL and NLL at each order in  $\alpha_s$ . We denote them as NLO-NLL and NNLO-NLL, respectively, and calculate them using the master formulas in Ref. [5].

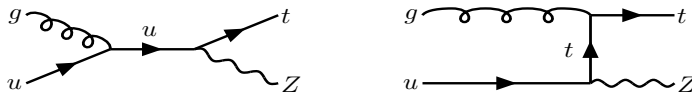


Figure 1: Tree-level diagrams for  $gu \rightarrow tZ$ .

First we study the process  $gu \rightarrow tZ$  in  $p\bar{p}$  collisions at the Tevatron. In Fig. 1 we show the lowest-order Feynman diagrams.

In Fig. 2 we show plots versus top quark mass of the Born, NLO-NLL, and NNLO-NLL cross sections and of various  $K$ -factors, which are defined as ratios of cross sections at different orders. Note that  $K$ -factors are independent of the notation/specification for the anomalous couplings. We have set the scale  $\mu$  equal to the top quark mass and set  $\kappa_{tuZ} = 0.1$ .

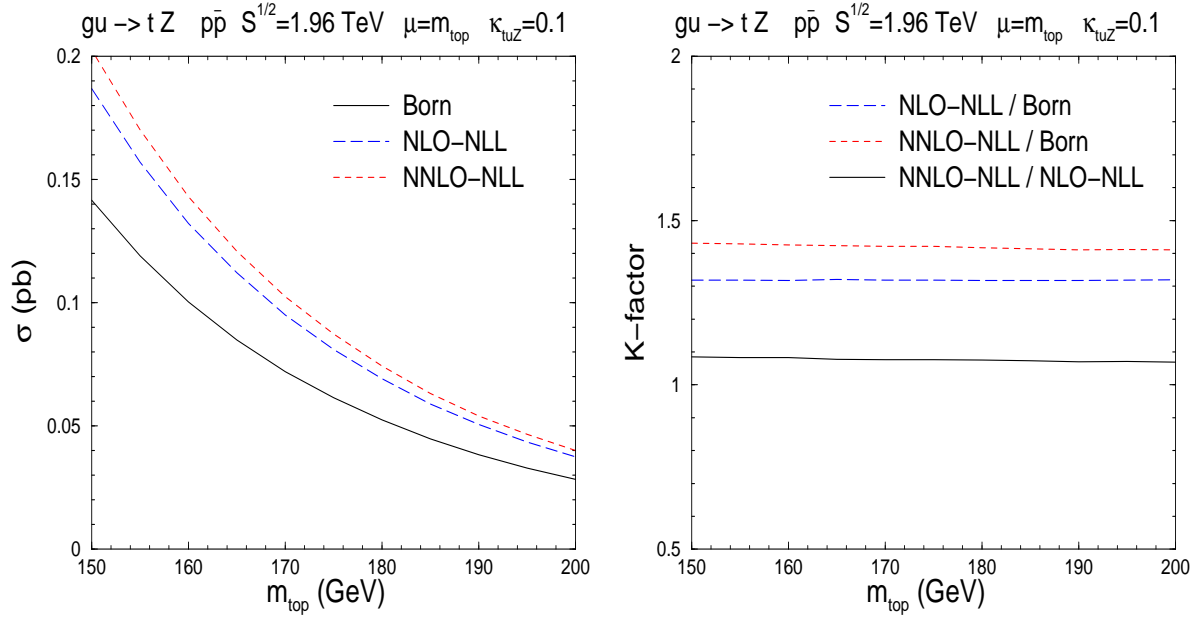


Figure 2: Cross sections (left) and  $K$ -factors (right) for  $gu \rightarrow tZ$  at the Tevatron.

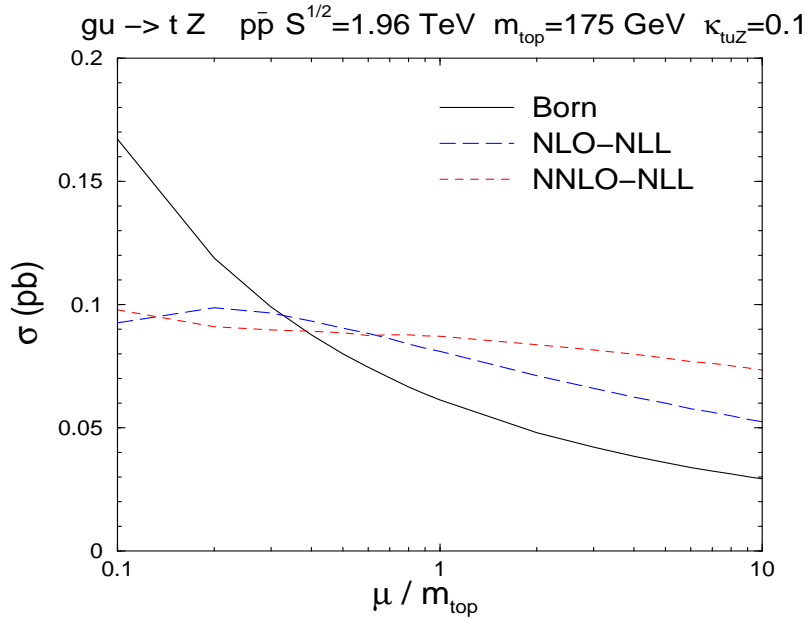


Figure 3: The scale dependence of the  $gu \rightarrow tZ$  cross section at the Tevatron.

In Fig. 3 we plot the scale dependence of the cross section for a top mass  $m = 175$  GeV. It's clear that the dependence of the cross section on scale is significantly decreased when we add the NLO-NLL and NNLO-NLL corrections. For  $\mu = m = 175$  GeV,  $\kappa_{tuz} = 0.1$  and  $\sqrt{S} = 1.96$  TeV we find  $\sigma_{NNLO-NLL}^{gu \rightarrow tZ} = 87_{-3}^{+2}$  fb where the uncertainty comes from scale variation between  $m/2$  and  $2m$ . We note that the cross section for the process

$gc \rightarrow tZ$ , involving the charm quark, is negligible by comparison. We also note that the cross section for anti-top production,  $g\bar{u} \rightarrow \bar{t}Z$ , is the same as for top production.

The results for  $gu \rightarrow t\gamma$  are qualitatively the same – we find again stabilization of the cross section versus scale variation, as well as a similar cross section level ( $\sigma_{NNLO-NLL}^{gu \rightarrow t\gamma} = 95_{-11}^{+17}$  fb for  $\mu = m = 175$  GeV and  $\kappa_{tu\gamma} = 0.1$ ). In the case of the process  $uu \rightarrow tt$  the cross section is also stabilized; however, this process is qualitatively different: it has a significantly lower cross section ( $\sigma_{NNLO-NLL}^{uu \rightarrow tt} = 1.74_{-0.02}^{+0.00}$  fb for  $\mu = m = 175$  GeV and  $\kappa_{tuZ} = \kappa_{tu\gamma} = 0.1$ ) but a much cleaner signature [1].



Figure 4: Tree-level diagrams for  $eu \rightarrow et$ .

Next we study the process  $eu \rightarrow et$  in  $ep$  collisions at HERA [6, 7, 8]. In Fig. 4 we show the lowest-order Feynman diagrams. In Fig. 5 we show plots of the Born, NLO-NLL,

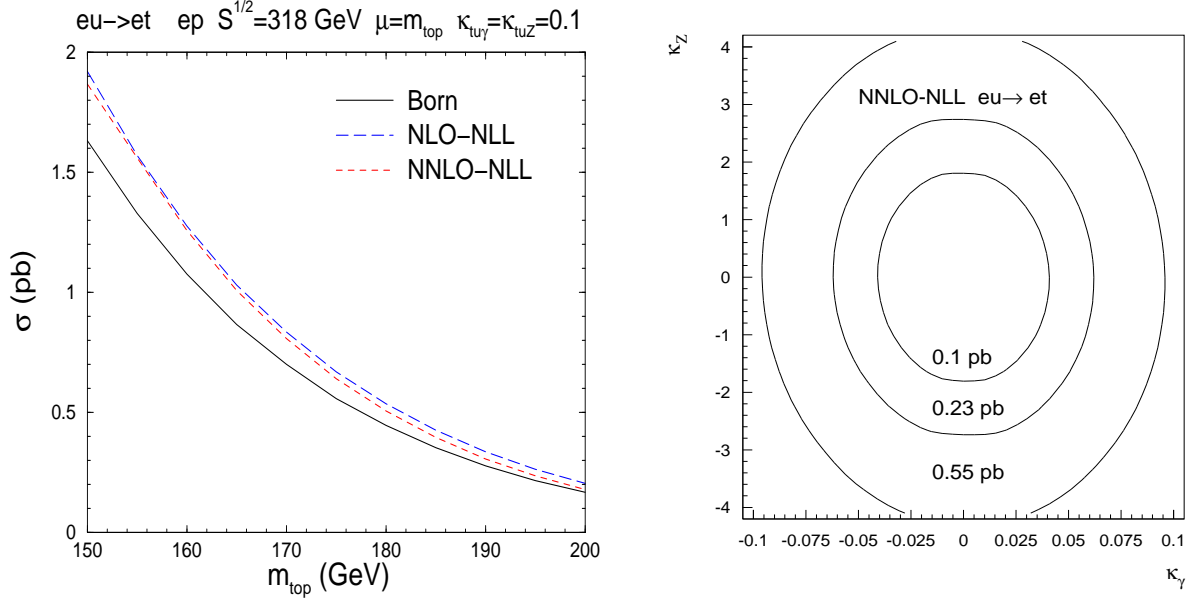


Figure 5: Cross sections (left) and HERA reach (right) for the process  $eu \rightarrow et$ .

and NNLO-NLL cross sections versus top mass, and of contour levels in the  $\kappa_{tu\gamma}, \kappa_{tuZ}$  plane. We have set  $\mu = m$ . It is evident that HERA is much more sensitive to the  $\kappa_{tu\gamma}$  coupling than to  $\kappa_{tuZ}$ . The NNLO-NLL cross section at HERA for  $\mu = m = 175$  GeV,  $\kappa_{tu\gamma} = \kappa_{tuZ} = 0.1$  and  $\sqrt{S} = 318$  GeV is  $\sigma_{NNLO-NLL}^{eu \rightarrow et} = 0.64_{-0.04}^{+0.05}$  pb, where again the uncertainty comes from scale variation between  $m/2$  and  $2m$ . We note that almost all of the cross section comes from the  $\kappa_{\gamma}$  coupling. We also note that contributions from charm

are negligible. In the case of  $e\bar{t}$  production, involving the anti-top, the cross section is quite small  $\sigma_{NNLO-NLL}^{e\bar{u}\rightarrow e\bar{t}} = 0.0079$  pb, and thus assymetrical to  $et$  production.

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