

# Cambridge-INET Institute

Cambridge-INET Working Paper Series No: 2015/23

Cambridge Working Paper in Economics: 1566

## INFORMATION ACQUISITION AND EXCHANGE IN SOCIAL NETWORKS

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# Information Acquisition and Exchange in Social Networks

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September 6, 2015

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We are grateful to the Editor, Martin Cripps, and three anonymous referees for comments that have significantly improved the paper. We also thank Nicolas Carayol, Syngjoo Choi, Matthew Elliott, Edoardo Gallo, Ben Golub, Friederike Mengel, Francesco Nava, Romans Pancs, Pauline Rutsaert, Vessela Daskalova and seminar participants at ASSET 2012, Stockholm, ESA 2012, Cologne, Bordeaux, Cambridge, Rotterdam and Cape Town for helpful comments. The paper was circulated as a working paper in 2012 with the title "Individual search and social communication".

# 1 Introduction

Individuals (and organizations) acquire information privately and by forming communication links with others. Private acquisition of information is costly; similarly, creating and maintaining personal contacts takes time and resources. The development of modern information technology creates a platform for extensive on-line social engagement: it has a major impact on the relative cost of these two ways of accessing information. The goal of this paper is to empirically study the economic effects of this change.<sup>1</sup>

We use laboratory experiments to study this trade-off as they allow us to control the main variables directly: the costs and benefits of linking and of individual public good provision. We can study causal determinants of the processes at work. Moreover, we can measure the provision of the public good and the welfare implications explicitly.

The theoretical framework for our experiment is taken from Galeotti and Goyal (2010). In their model, individuals choose a level of investment given by  $x_i$ , and the number of links with others, given by  $\eta_i$ . Investments take on a general form and are naturally interpreted as a local public good.<sup>2</sup> Individual investment is costly: each unit of investment costs  $c > 0$ . Similarly, linking activity is costly: each link costs  $k > 0$ . Furthermore, investment activity of different individuals is substitutable: the marginal utility of own investment is falling in the investment level of connected others. Define  $\hat{y}$  as the investment an isolated individual would make.

Galeotti and Goyal (2010) show that every (strict) Nash equilibrium of this game is characterized by investment sharing. The theory yields sharp predictions on some dimensions: every individual must access  $\hat{y}$  investment (own investment and investment from others) and total investment by society must also be equal to  $\hat{y}$ , independently of the linking costs. The theory is permissive on other dimensions: a variety of networks and distribution of individual investments levels can be sustained in equilibrium. For instance, at low costs of linking, there exists an equilibrium with a single hub player acquiring  $\hat{y}$  and all other players forming links to him/her. But there is

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<sup>1</sup>For a wide ranging overview of the economics of modern information technology, see Peitz and Waldfogel (2012). For a study of the information flows and their impact on interfirm collaboration links, see Frankort et al (2012).

<sup>2</sup>This framework combines an approach to network formation introduced in Goyal (1993) and Bala and Goyal (2000) with a model of local public good provision in fixed networks taken from Bramoullé and Kranton (2007).

another equilibrium in which all players make investments and are fully connected with each other. On the other hand, at high costs of linking, only the single hub outcome is sustainable in equilibrium. One of the main questions of interest is the impact of changing linkage costs on welfare. It is easy to see that welfare impact depends crucially on which equilibrium is played at low costs. Roughly speaking, the welfare improvements are larger if the single hub equilibrium is played across the different linkage costs, but are muted if the multiple hub equilibrium is played at low costs.<sup>3</sup> This multiplicity in equilibrium outcomes is thus an important motivation for our experimental work.

We conduct a range of experiments with groups of four subjects. To accommodate the complexity of the strategic structure of the game and to give players ample opportunities for learning we run the experiment in continuous time. Subjects can make choices and revise them over time and we have a random termination time.

We start with homogenous costs of investment,  $c$ , and low costs for links,  $k$ . We then compute the level of  $\hat{y}$ . In the experiment, we find that all subjects indeed have access to  $\hat{y}$  units of investment. Total investment in society is much lower than  $4 \times \hat{y}$ : so there is extensive sharing of investments. In line with theory, individual investments and the number of in-coming links are positively correlated.

We then turn to the effects of changing costs of linking. As we raise linking costs, the theory predicts that  $\hat{y}$  remains unchanged. However, at a higher linking cost, a person must obtain more investment for the link to be justified. Given that total investment is constant (across linkage costs), this implies that there will be fewer hubs and also fewer links. In the experiment, we find that subjects act very much in line with each of these predictions: the number of hubs and links fall as we raise linking costs, while hubs raise their investment. Individuals access  $\hat{y}$  units of investment on average, at all cost levels.

Next we consider a setting with heterogeneity in costs of investment. The low-cost player  $i$ 's stand-alone optimal investment is  $\hat{y}_1 > \hat{y}$ . The unique equilibrium network has the star architecture with the low-cost player as the hub, independently of the linking costs. In the experiment we randomly

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<sup>3</sup>We note that equilibrium total investment is constant across linkage costs, but that the number of links vary from  $n - 1$  (in the hub-spoke (star) network) all the way to  $n(n - 1)/2$  (in the fully connected (complete) network).

determined one player in each group to have lower costs. We see indeed that this low-cost player is more likely to be the hub and that individuals access  $\hat{y}_1$  units of investment on average, at all cost levels. The macroscopic patterns with regard to linking costs exhibit the same pattern as in the homogenous treatments: the number of hubs and links fall as we raise linking costs, while average investment by hubs rises.

One important prediction of the theory, in both the homogenous and the heterogeneous cost treatments, is that total investment acquired is invariant with respect to linking costs. In the experiment, we find that aggregate investment is higher than predicted and that it increases with linking costs. We develop an explanation for these two departures from the theory. The first point to note is that in the original model of Galeotti and Goyal (2010), players make their choices simultaneously. By contrast, in the experiment, players make choices sequentially and repeatedly, and there is an uncertain end point. We focus on this difference: the main idea we explore is that, toward the end of the game, players explore small and local moves to improve their payoffs. A strategy profile is said to be *stable* if there exists no small and local deviation that is profitable, in this sense.

An important feature of the equilibrium outcome in the static game is that the hub player makes large investments while the peripheral nodes make zero investments and form links with the hub. In a dynamic setting, the hub can shade his investment downward, in anticipation of a potential upward shift in the investment by the peripheral player. The extent of downward shading is constrained by the threat of a link deletion by peripheral player. Our analysis explores the bounds on the shading and the level of investments by the peripheral players. We note that in this situation, the peripheral player will choose an investment level that is optimal given the hub's investment choice (so investment accessed by the peripheral player must be  $\hat{y}$ ). On the other hand, as the hub potentially has access to multiple peripheral players, he/she accesses investment in excess of the static equilibrium level  $\hat{y}$ . This provides an account for higher than static equilibrium investments in the experiment. Building on these considerations, we also show that higher costs of linking imply higher aggregate investments.

The final major finding concerns the welfare implications of changes in costs of links. In the homogenous cost case (when all players have the same costs of investment), at high linking costs, there is a unique equilibrium with a single hub. However, at lower linking costs in addition to the single hub outcome, there also exist other equilibrium outcomes, with multiple hubs

and more links. So the theoretical predictions on individual and aggregate welfare are *a priori* ambiguous. The data from the experiment yields two clear cut findings. Aggregate earnings are below the (least efficient) Nash equilibrium prediction in all cases. However, they are falling significantly in linking costs.<sup>4</sup>

To summarize, our experimental subjects behave in line with the predictions of the theory with regard to total investment accessed by an individual player and on the presence of significant linking and investment sharing. The experiment, however, goes beyond the theory in one important dimension: it shows that as linking costs fall, investment is more dispersed and it is accompanied by denser social networks. This has interesting and large effects on welfare. Finally, the experiment also yields an important departure from the theory: aggregate investment is sensitive to costs of linking.

Our paper is a contribution to the literature on public goods and networks. In the literature on public goods experiments, an important general finding is that individuals contribute more than what theory predicts though they contribute less than the first best; for surveys, see Ledyard (1995), Croson (2010), and Holt and Laury (2012). Thus individual utility is generally higher than the Nash equilibrium level. The principal novelty in the present paper is that individual choices determine whether their actions and others' actions become public goods or remain 'private'. This is accomplished through the formation of links. The experiment reveals that this 'endogeneity' of public goods has important implications for behavior and welfare. With increasing linking costs the aggregate investment in the 'public' good rises, but due to lower linking, every individual has access to the same amount of it. Moreover, in all treatments, endogeneity of links leads to outcomes that are worse than the worst Nash equilibrium (in terms of aggregate welfare).

Our paper is also a contribution to the study of social networks. There is now a large theoretical literature on social networks but the empirical assessment of networks in economic activity remains a challenge. This motivates the recent experiments on networks (Charness, Corominas-Bosch and Frechette (2007), Cassar (2007), Callander and Plott (2005), Burger and Buskens (2009), Goeree et al. (2009), Falk and Kosfeld (2012), Rosenkranz and Weitzel (2012), Charness, Feri, Melendez-Jimenez, Sutter (2014), and Van Dolder and Buskens (2014)). This work considers either games on fixed

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<sup>4</sup>We observe very similar patterns with regard to welfare in the heterogenous cost treatments.

networks or pure network formation games. The novelty in the present paper is that we combine both activities and focus on the trade-off between private investments and linking activity. Two recent papers, Rong and Houser (2012) and Leeuwen, Offerman and Schram (2013) also report experiments on the Galeotti and Goyal (2010) paper. The distinctive feature of our paper is the focus on the relative costs of social linking and the empirical findings relating to the large economic effects of such changes. The rest of the paper is organized as follows: Section 2 describes the theoretical model. Section 3 presents the experimental design. Section 4 presents and discusses the experimental findings. Section 5 concludes.

## 2 The network game

The following model is taken from Galeotti and Goyal (2010). Suppose there is a set of agents  $N = \{1, 2, \dots, n\}$  with  $n \geq 3$  and let  $i$  and  $j$  be members of this set. Let each player  $i$  choose  $x_i \in X$  with  $X \in [0, \bar{X}]$  (denoting agent  $i$ 's effort level on the production of a local public good, and a set of links represented as a vector  $g_i = (g_{i1}, \dots, g_{ii-1}, g_{ii+1}, \dots, g_{in})$ , where  $g_{ij} \in \{0, 1\}$ , for each  $j \in N \setminus \{i\}$ . If  $g_{ij} = 1$ , agent  $j$  has a link with player  $i$  and benefits directly from agent  $i$ 's effort, and  $g_{ij} = 0$  otherwise. Suppose that  $g_i \in G_i = \{0, 1\}^{n-1}$ .

The set of strategies of player  $i$  is denoted by  $S_i = X \times G_i$ . Let  $S = S_1 \times \dots \times S_n$  to be the set of strategies of all players. A strategy profile  $s = (x, g) \in S$  specifies the investment made by each player,  $x = (x_1, x_2, \dots, x_n)$ , and the network of links  $g = (g_1, g_2, \dots, g_n)$ . The network of links  $g$  is a directed graph; let  $G$  be the set of all possible directed graphs on  $n$  vertices.

Define  $N_i(g) = \{j \in N : g_{ij} = 1\}$  as the set of players with whom  $i$  has formed a link, and let  $\eta_i(g) = |N_i(g)|$ , the number of links formed by  $i$ . The closure of  $g$  is an undirected network denoted  $\bar{g} = cl(g)$  where  $\bar{g}_{ij} = \max\{g_{ij}, g_{ji}\}$  for each  $i$  and  $j$  in  $N$ , reflecting the bilateral nature of exchange between two players. Define  $N_i(\bar{g}) = \{j \in N : \bar{g}_{ij} = 1\}$  as the set of players directly connected to  $i$ .

The *core-periphery* network plays a prominent role in our analysis. We now define it formally: There are two groups of players,  $\hat{N}_1(\bar{\mathbf{g}})$  and  $\hat{N}_2(\bar{\mathbf{g}})$ , with the feature that  $N_i(\bar{\mathbf{g}}) = \hat{N}_2(\bar{\mathbf{g}})$  for all  $i \in \hat{N}_1(\bar{\mathbf{g}})$ , and  $N_j(\bar{\mathbf{g}}) = N \setminus \{j\}$  for all  $j \in \hat{N}_2(\bar{\mathbf{g}})$ . We will refer to nodes which have  $n - 1$  links as hubs, while we will refer to the complementary set of nodes as peripheral nodes or

as spokes.

The payoff to player  $i$  under strategy profile  $s = (x, g)$  is:

$$\Pi_i(s, g) = f(x_i + \sum_{j \in N_i(\bar{g})} x_j) - cx_i - \eta_i(g)k \quad (1)$$

Costs of investment are represented by  $c > 0$ , while linking costs are represented by  $k > 0$ . The payoff function represents the tradeoff described in the introduction and the local public good character of private investment. The benefit  $f(y)$  of a player depends on the aggregate investment by her direct neighbors, which is not necessarily identical to the aggregate investment available in the network.

For the experiment we assume that  $f(y)$  is twice continuously differentiable, increasing, and strictly concave in  $y$ , and that  $f(0) = 0$ ,  $f'(0) > c$  and  $f'(\bar{X}) = z < c$ . Under these assumptions there exists a number  $\hat{y} \in (0, \bar{X})$ , such that  $\hat{y} = \arg \max_{y \in X} f(y) - cy$ .

Define  $I(s) = \{i \in N | x_i > 0\}$  as the set of players who make positive investments. Galeotti and Goyal (2010) prove:

**Proposition 1** *Suppose payoffs are given by (1) and  $k < c\hat{y}$ . In every strict equilibrium  $s = (x, g)$ : (1.)  $\sum_{i \in N} x_i = \hat{y}$ , and (2.) the network has a core-periphery architecture. Hubs make positive investments and peripheral players make no investments.*

They show that as the relative linking costs  $k/c$  grow, the number of hubs decreases, each hub player makes larger investments, and the total number of links decreases. In particular, if  $k/c \in (\hat{y}/2, \hat{y})$ , then there is only one hub, and the communication structure takes the form of a periphery sponsored star. Note that in every strict equilibrium aggregate investment will be equal to  $\hat{y}$  and is thus independent of the level of linking costs.

Suppose that there exists a small heterogeneity in costs of investment. Let  $c_i = c$  for all  $i \neq 1$  and  $c_1 = c - \epsilon$ , where  $\epsilon > 0$ . Define  $\hat{y}_1 = \arg \max_{y_1 \in X} f(y_1) - c_1 y_1$ . Proposition 3 of Galeotti and Goyal (2010) establish:

**Proposition 2** *Suppose that  $k < f(\hat{y}_1) - f(\hat{y}) + c\hat{y}$ .<sup>5</sup> In every strict equilibrium  $s^* = (g^*, x^*)$ , (i)  $\sum_{i \in N} x_i^* = \hat{y}_1$  (ii) the network is a periphery-sponsored*

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<sup>5</sup>The inequality gives us the upper bound on the cost of a link for a high cost player to link with a low cost hub player.



star with player 1 as hub, and (iii) either  $x_1^* = \hat{y}_1$  and  $x_i^* = 0$ , for all  $i \neq 1$ , OR  $x_1^* = ((n-1)\hat{y} - \hat{y}_1)/(n-2)$ , and  $x_i = (\hat{y}_1 - \hat{y})(n-2)$ , for all,  $i \neq 1$ .

Observe that a slight cost heterogeneity leads to the low-cost player becoming the unique hub player; this illustrates the power of strategic reasoning in shaping networks and behavior.

### 3 The experimental design and hypotheses

In the experiment, subjects faced the decision problem characterized above: groups of  $N = 4$  subjects chose a level of investment and, simultaneously, they chose to which other players they wanted to be connected. The payoff is given by the following function (with  $\bar{X} = 29$ ):

$$\pi_i = (x_i + \sum_{j \in N(i;\bar{g})} x_j)(29 - (x_i + \sum_{j \in N(i;\bar{g})} x_j)) - c_i x_i - \eta_i(g)k.$$

This implies that (given the network) the optimal effort level  $x_i$  for a player  $i$  is:

$$x_i = (29 - c_i) / 2 - \sum_{j \in N(i;\bar{g})} x_j.$$

Our design consists of two treatment variables: the linking costs  $k$ , and the costs  $c_i$  for investment. In the experiment, investments were constrained to integers. Table 1 presents our treatments, which we label by roman numbers in the following.

— Insert Table 1 here —

#### The baseline treatment

In the baseline treatment, we set  $c = 5$  and  $k = 10$ . For these values  $\hat{y} = 12$ , and the parameters satisfy  $k < c\hat{y}$ . We refer to this as Treatment I.

Appendix I provides a proof that in every equilibrium the sum of total investments is equal to 12.<sup>6</sup> With this result on aggregate investment being

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<sup>6</sup>The original results of Galeotti and Goyal (2010) apply to strict Nash equilibrium. In our experimental treatments we assume that investments take on integer values only and this restriction allows us to draw stronger implications and show that aggregate investment is equal to  $\hat{y} = 12$  in every equilibrium (and not just in the strict equilibrium).

equal to  $\hat{y} = 12$ , we then apply Proposition 1 in Galeotti and Goyal (2010) to provide a complete characterization of equilibria. Figure 1 presents the key features of equilibrium outcomes.

— Insert Figure 1 here —

There are multiple equilibria possible but they share some key macroscopic properties: there is investment sharing in all of them, every individual accesses 12 units of investment, and aggregate investment in society is also 12. There is positive correlation between level of individual investment and the number of others who link with this person (her in-degree). Theory also predicts individual earnings to vary greatly within an equilibrium and also across equilibria. Finally, aggregate earnings are predicted to also vary greatly across equilibria (see Table 3). Due to the rather high level of complexity in our experiment (groups of 4, two strategic variables, multiple equilibria) we do not expect subjects to easily coordinate on equilibria. This leads us to focus on the impact of relative cost of investments and linking on individual investments and the macroscopic features of the network (the number of links and the welfare).

### Linking costs

A key aspect of the model is the comparison of linking costs and the costs of investment. To explore the role of this comparison we vary the linking costs. We raise the costs from  $k = 10$  to  $k = 24$  and then to  $k = 36$ ; we refer to these as Treatments II and III. Figure 1 provides a characterization of equilibrium outcomes. In Treatment II, with  $k = 24$ , an equilibrium contains either 1 hub with 3 links or 2 hubs with 4 links. Investment by a hub must be at least 4.8 to justify linking by peripheral players. In Treatment III, with  $k = 36$ , an equilibrium contains 1 hub and 3 links. Investment by the hub must exceed 7.2. Across these cost levels, individuals access exactly  $\hat{y} = 12$  units of investment and aggregate investment remains at 12. For easy reference all equilibrium values including earnings are presented in Table 3.

These observations yield our first hypothesis on the comparisons across Treatment I, II and III.

**Hypothesis 1:** *With homogenous costs of investment an increase in linking costs (a) reduces the number of hubs, (b) raises investments by hubs,*

and (c) reduces the number of links, while (d) aggregate investment remains unchanged and (e) aggregate earnings fall.

### Heterogeneity in costs of investment

To understand the importance of heterogeneity among players for the emergence of core-periphery structures, we consider the role of heterogeneity in costs for investment across individuals. Suppose  $c_i = 5$  for all  $i \neq 1$  and  $c_1 = c - \epsilon$ , where  $\epsilon = 2$ . We allow for the same three levels of linking costs as in the homogeneous treatments, i.e.  $k = \{10, 24, 36\}$ . We refer to these heterogeneous treatments as Treatments IV-VI. It follows that the low-cost player's stand-alone optimal investment is  $\hat{y}_1 = 13$ . Moreover,  $k < f(\hat{y}_1) - f(\hat{y}) + c\hat{y}$ , which in combination with the discrete action space implies that the unique equilibrium network is a periphery-sponsored star and the low-cost player is the hub, investing  $\hat{y}_1$ , irrespective of the linking costs. The proof of this property is presented in Appendix I. Figure 1 provides a characterization of equilibrium outcomes. Our second hypothesis operationalizes Proposition 2 and refers to a comparison between Treatment I and IV ( $k = 10$ ).<sup>7</sup>

**Hypothesis 2:** *If linking costs are low ( $k = 10$ ), heterogeneity with respect to costs of investment specialization: (a) the low-cost player is the hub. Moreover, heterogeneity (b) reduces the number of hubs, (c) raises investment by hubs, and (d) lowers the number of links, and (e) raises aggregate investment.*

Note that part (e) is a direct consequence of the fact that with heterogeneous players the low-cost player is the unique hub whose optimal investment, which is identical to aggregate investment, is larger due to his lower costs.

### 3.1 Experimental procedures

The computerized experiment was designed using the software program z-tree (Fischbacher, 2007) and conducted in the Experimental Laboratory for Sociology and Economics (ELSE) at Utrecht University. In total, eight experimental sessions of approximately one-and-a-half hours were scheduled and

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<sup>7</sup>For Hypothesis 2, we focus on the benchmark cost  $k = 10$ ; in other words, we compare treatment I and IV. This comparison that offers the greatest contrast: with homogenous costs networks with 1-4 hubs may arise in equilibrium while there is a network with a unique hub in the heterogeneous costs case. For higher links costs, the impact of cost heterogeneity is much smaller.

completed. Before the start of every experiment, general written instructions were given, which were kept identical across sessions (see Appendix II).

Using the ORSEE recruitment system (Greiner, 2004), over 1000 potential subjects were approached by e-mail to participate in the experiment. A total of 152 subjects (either 16 or 20 per session) participated. Each subject played 24 rounds of a local public goods game with linking decisions. Subjects were informed about the fact that at the beginning of each round, they were randomly allocated to a group together with three other participants. This resulted in  $152/4 = 38$  observations at the group level per round. Subjects were indicated as circles on the screen and could identify themselves by color: each subject saw him- or herself as a blue circle while all other members of the same group were represented as black circles (see screen shots in Appendix II). In the heterogeneous treatments the low-cost player was determined randomly at the beginning of each round and on the screen this player was marked with an additional square. Subjects could see investment levels and links as well as profits of all other players all the time. The identity of the subjects was not identifiable between different rounds or at the end of the experiment.<sup>8</sup>

In each session we ran every treatment. The order of the treatments was balanced across sessions.<sup>9</sup> Each of the six treatments I - VI described in the previous section was played for 4 rounds: 1 trial round and 3 payment rounds. As we did not use the data of the trial round in our analysis, this ultimately led to 114 ( $= 38 \text{ groups} \times 3 \text{ rounds}$ ) observations at the group level per treatment. Moreover, we obtained 456 ( $= 38 \text{ groups} \times 3 \text{ payment rounds} \times 4 \text{ players}$ ) observations at an individual level.

Every round had the same structure and lasted between 105 and 135 seconds (on average 120.5 seconds). This was communicated to subjects at the start of the experiment and again at the point of 105 seconds. Starting from a situation with no investments and no links, subjects indicated simultaneously on their computer terminals (by clicking on one of two buttons at the bottom of the screen) how much (expressed in "points") they wished to invest. By clicking on one of the circles on the screen representing another participant, subjects could link to this other participant. A one-headed arrow appeared to indicate the link and its direction. By clicking again on

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<sup>8</sup>The aim of this allocation mechanism is to minimize the dependence across observations (Falk and Kosfeld, 2012).

<sup>9</sup>See Table 9 in Appendix II for the sequence of the treatments.

the other participant the arrow and, thus, the link was removed again. The participant who initiated this link had to pay some points for this link. If both participants had clicked for a specific link a two-headed arrow appeared and both participants needed to pay points for this link.

We note that, during the experiment, full information about the investments and linking decisions of all other subjects was continuously provided. Also, resulting payoffs of all participants could continuously be observed on the screen. At the end of each round, subjects were informed about the number of points earned with the investments and links as were on the screen at the end of that round. In other words, subject earnings only depended on the situation at the (random) end of every round.

It is important to clarify some aspects of the experimental design.

Our *first* remark concerns the complexity of the game and the need for trial time: Experience with previous experiments on network formation suggests that individuals find the decision problem to be very complex and this inhibits behavior (Goeree et al., 2009; Falk and Kosfeld, 2012). Subjects appear to need time to understand the game and to coordinate their actions. We address this issue in our design by having a trial round (non-payoff relevant) at the beginning of each treatment, and, in addition, by starting each round with a trial period of 105 seconds where actions do not have payoff implications. Moreover, to facilitate activity, we allowed subjects to choose links and investment levels in continuous time.

Our *second* remark concerns the end of the time interval between 105 and 135 seconds: while a random end may induce players in a disadvantageous equilibrium position to try to move play towards a more advantageous equilibrium if the interval is still long enough, a fixed end may turn the game into an unpredictable waiting game in which players are likely to mis-coordinate during the final stage. After an internal test session we considered the second effect to be more severe.

The *third* set of remarks is about the relation between the theoretical model discussed in Section 2, and the experimental design.

A general observation is that design departs in many ways from the static model studied by Galeotti and Goyal (2010). This departure was in some cases motivated by considerations of complexity of the game, as discussed above. But it is important to emphasize a more general methodological point: our goal in this paper is to examine the economic implications of the trade-off between costs of linking and the costs of personal investment as alternative routes to being well informed. Our view is that if the trade-

offs identified in the theoretical paper are robust then they should also be reflected in an experimental design that departs in some dimensions from the static model. With this general observation in place, we now take up some more specific points.

We may consider our experimental design as a sequence of simultaneous move games, with a stochastic end stage, and only the last stage behavior to be payoff relevant. In such an interpretation, it follows from standard arguments that any equilibrium of the stage game can be implemented in the stage game of our experiment.

Players know that activity in the first 105 seconds has no (direct) payoff relevance: actions in this period may therefore be viewed as ‘cheap talk’. This raises the question of whether this cheap talk can select between different equilibria of the stage game. There is a large literature on this subject: a general message is that cheap talk is more likely to be effective in equilibrium selection if equilibria are Pareto ranked (see e.g., Farrell and Rabin (1996)). In our setting, equilibria are not Pareto ranked. So we believe that cheap talk is not helpful in selecting equilibria in our analysis.

The final remark is about the potential repeated game effects. The period from 105 seconds until the end of the game may be viewed as a type of ‘repeated game’, with an ending that is stochastic with a well defined finite end point (at 135 seconds). From the work of Benoît and Krishna (1985), we know that repetition may be used to select among different stage game equilibrium and indeed even go beyond stage game equilibrium – to Pareto improving profiles of actions. This is certainly a possibility in our experimental design. We come back to this issue in section 4.3. below.<sup>10</sup>

At the end of the experiment, points were converted to Euros at a rate of 200 points = Euro 1. The total was then rounded upwards to Euro 0.5. On average, the experiment lasted 80 minutes and subjects earned Euro 14.40. At the end of the experiment, subjects were asked to fill in a short questionnaire about their demographic profiles.

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<sup>10</sup>There is also the possibility that once play settles on a stage game equilibrium a player who is disadvantaged (such as the hub) may choose to signal a move to a different stage game equilibrium though a deviation in personal investment. This sort of dynamic can probably be accommodated within an equilibrium but would require a much richer model. While this dynamic might be at work we believe that our main results – which pertain to the effects of falling linking costs –are robust to this dynamic as it is common across all our treatments.

## 4 Experimental findings

### 4.1 Description of sample and variables

Table 2 describes the sample across all sessions and treatments.<sup>11</sup> On average, a subject contributed 4.4 units, invested in 1.03 links to other players (out-degree) and had 1.03 other players linking to her (in-degree). On average, a period lasted 120.5 seconds during which a subject took 24.7 linking decisions and 52 investment decisions. Thus, the experiment was characterized by high level of activity in both investment and linking decisions.

— Insert Table 2 here —

Table 3 provides a summary of investments and linking per treatment, and reports profits at the individual and at the group level. In the following subsection, we use these variables and the differences between treatments, and report the relevant statistical analyses to test our hypotheses.<sup>12</sup>

— Insert Table 3 here —

With respect to individual investment, Table 3 shows that in line with theory the median player accesses exactly 12 units of investment, while the average access is 12.693 units. Although this average access is statistically different from  $\hat{y} = 12$  (two-tailed  $t$ -test,  $p < 0.01$ ), its deviation is less than 1 unit from the predicted value, which was the minimum increment in the experiment. Also for the heterogeneous treatments, in line with theory we observe that individuals, in the median, access 13 units of investment regardless of the level of linking costs.<sup>13</sup> For the average we also find that it is statistically not different from the theoretically predicted value of  $\hat{y}_1 = 13$  (two-tailed  $t$ -test,  $p = 0.229$ , in Treatment IV). In Table 3, we observe for the baseline Treatment I, a mean total investment per group of 15.175 units,

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<sup>11</sup>Approximately 65% of the 152 subjects participating in the experiment were female and 62% were Dutch. On average, a subject knew 0.7 other people in the lab by first name ('friends'), and was 21.3 years old.

<sup>12</sup>Treatments V and VI are robustness checks for Treatment IV.

<sup>13</sup>Wilcoxon rank-sum tests for the equality of medians show that the accessed levels of investment for  $k = 24$  and  $k = 36$  do not differ significantly ( $z = 0.455$ ) and only at  $z = 0.093$  for  $k = 10$  and  $k = 24$ . Two-sample  $t$ -tests for a comparison of the averages show a similar pattern with a  $p = 0.438$  for  $k = 24$  versus  $k = 36$ , and  $p = 0.002$  for  $k = 10$  versus  $k = 24$ .

which is significantly higher than the theoretically predicted level of  $\hat{y} = 12$ .<sup>14</sup> Figure 2 presents the distribution of investments accessed in Treatments I and IV.

— Insert Figure 2 here —

While total investment in society is larger than predicted, it still is much lower than 48 units, the level that would prevail if every individual would choose its optimal level independently. As each individual, on average, has access to approximately 12 units of investment, this means that there is considerable sharing of investment among individuals.

This insight is confirmed by an analysis of the relation between an individual’s investment and her in-degree, i.e. the number of directed, incoming links from other individuals. Figure 3 presents a box plot on this relation, i.e. the average node investment (for  $x_i < 19$ , corresponding to 99% of all observations) per node in-degree (x-axis). Non-parametric and parametric tests of pairwise correlation show that investment is indeed significantly higher for players with a higher in-degree.<sup>15</sup>

— Insert Figure 3 here —

To get more insight into investment sharing we next analyze the network structure. A direct examination of linking patterns reveals that the network is connected in over 90% of the cases, see Table 4. Table 2 shows that there is significant linking activity (in all treatments).<sup>16</sup>

— Insert Table 4 here —

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<sup>14</sup>Our statistical tests (a two-tailed  $t$ -test, a Wilcoxon rank-sum (Mann-Whitney) test for the equality of medians, and a Kolmogorov-Smirnov test for the equality of distribution functions) confirm that aggregate investment is statistically significantly higher than 12 at a 99% level of confidence.

<sup>15</sup>The Pearson correlation coefficient between in-degree and investment at a 1% level of statistical significance (99% CI) is 0.4196 for the homogeneous Treatments I-III, and 0.4409 for the heterogeneous Treatments IV-VI. The positive correlation between in-degree and investment is also confirmed in an OLS regression, with investment as the dependent variable, and in-degree and all levels of linking costs  $k$  as independent variables. This is reported in Table 10, in Appendix II, where Model 1 in the first column presents the data from the baseline Treatment I ( $k = 10$ ,  $c = 5$ ).

<sup>16</sup>Although equilibrium outcomes arise very rarely in the laboratory, 25.4% of all groups are in a network structure as described by equilibrium (for evidence on this refer to Table 11 in Appendix II).



Taken together, these observations offer strong support for investment sharing in the laboratory. Finally, from Table 3 we note that aggregate earnings of subjects are typically lower than the lowest equilibrium payoffs. However, we do observe a significant fall in aggregate earnings as we raise the costs of linking from  $k = 10$  to  $k = 36$ .

## 4.2 Hypotheses testing

We now turn to the central question regarding the impact of changing linking costs. Hypothesis 1 predicts (for the homogeneous treatments) that *an increase in linking costs (a) reduces the number of hubs, (b) raises investments by hubs, and (c) reduces the number of links, while (d) aggregate investment remains unchanged and (e) aggregate earnings fall.*

The theory defines a hub as a player who invests  $x_i > k/c$ , such that other players find it worthwhile to link to this player. For  $k = 10, 24, 36$  and  $c = 5$ , these critical investment levels are 2, 4.8, and 7.2, respectively. Note that, to test whether the investment by hubs increases with rising linking costs, we should not use a definition that is based on rising investment thresholds, as this would bias our estimates. We therefore use a definition that is based on a player's incoming links (in-degree). We define someone as 'Hub2' if she has an in-degree larger than or equal to 2, and someone as 'Hub3' if she has an in-degree larger than or equal to 3. While the first definition is in line with the equilibrium predictions for the treatments  $k = \{10, 24\}$ , it is too lenient for  $k = 36$ . The second definition is in line with the theoretical predictions for treatment  $k = 36$ . It also allows for a conservative test of our theory when applied to the other two treatments.

In Table 5, the columns 'Hub2' and 'Hub3' show the number of players qualifying as a hub, as well as the average number of hubs per group. Overall, we find clear evidence for a decline in the number of hubs when linking costs increase from  $k = 10$  to  $k = 24$  or  $k = 36$  (Hub2) and from  $k = 10$  or  $k = 24$  to  $k = 36$  (Hub3), largely supporting Hypothesis 1(a).<sup>17</sup>

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<sup>17</sup>Kolmogorov-Smirnov tests comparing the number of hubs in one treatment with the remaining two levels of  $k$ , show that there are significantly more subjects with an in-degree of at least 2 (Hub2) when  $k = 10$  compared with  $k = 24$  or  $k = 36$  (statistically significant with a 99% CI). There is, however, no significant difference between the treatments with  $k = 24$  and  $k = 36$ . At the same time we find that significantly fewer subjects had an in-degree of 3 (Hub3) when  $k = 36$  compared with  $k = 24$  or  $k = 10$  (differences are significant with a 99% CI). We do not find a significant difference between the treatments

Table 5 shows investment subjects that qualify as a Hub2 or as a Hub3: for both hub definitions investment levels for  $k = 24$  and for  $k = 36$  are significantly higher than for  $k = 10$  (99% CI), while the investment levels for  $k = 24$  and  $k = 36$  do not differ statistically.<sup>18</sup> Thus, we interpret this as support for Hypothesis 1(b).<sup>19</sup>

— Insert Table 5 here —

We next turn to the number of links. Table 3 on group descriptives reports the mean (and median) number of directed ties per group. We see that there are 5, 4 and 3 links as we vary costs of linking from  $k = 10$  to  $k = 36$ . Confirming Hypothesis 1(c), we find that higher levels of linking costs are associated with lower levels of linking.<sup>20</sup>

We next consider aggregate investment. Table 3 reveals that it is growing with cost of linking: in the homogeneous treatments, it is, on average, 15.175 at  $k = 10$ , rises to 17.588 at  $k = 24$  and then rises further to 19.465 at  $k = 36$ . This rise of aggregate investment is statistically significant at a 95% level of confidence (for  $t$ -tests, the Wilcoxon rank-sum tests as well as a Kolmogorov-Smirnov tests across levels of  $k$ ). With the same tests we also confirm statistically that aggregate investment is higher than 12 at a 99% level of confidence. This is a clear departure from the theoretical prediction in Hypothesis 1(d). However, note that, as theoretically predicted (see Proposition 1 and Figure 1), the mean and median individually accessed investment does not change in the level of linking costs  $k$ .<sup>21</sup> We provide an

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with  $k = 10$  and  $k = 24$ .

<sup>18</sup>Table 10 in Appendix II shows a positive correlation between in-degree and investment in general. Model 2 shows the estimations for the data from the heterogeneous Treatment IV with  $k = 10$ , Model 3 for all data from the homogeneous Treatments I-III pooled, Model 4 for all data from the heterogeneous Treatments IV-VI, and Model 5 for all data of the full sample (Treatments I-VI) pooled. In Models 3 to 5, dummies for the treatments with linking costs  $k = 10$  and  $k = 36$  are added. The results show that with lower linking costs,  $k = 10$ , individual investment is lower. The dummy for  $k = 36$  in Model 3 is close to statistical significance with a  $t$ -value ( $p$ -value) of 1.565 (0.118) when compared to  $k = 24$ .

<sup>19</sup>Note that theory does not predict a specific slope for the increase of investments by hubs. According to Table 5 such a slope is likely to be concave: we find a significant increase in hub investments as costs of linking move from  $k = 10$  to  $k = 24$ , which then levels out between  $k = 24$  and  $k = 36$ .

<sup>20</sup>A Wilcoxon rank-sum test (and also the Kolmogorov-Smirnov test) shows that the respective differences are significant for  $k = 24$  ( $k = 36$ ) and  $k = 10$  (99% CI), and for  $k = 24$  and  $k = 36$  (95% CI).

<sup>21</sup> $T$ -tests show  $p$ -values of 0.187 and 0.631 for a comparison of averages across levels of

explanation for the deviation concerning aggregate investment in Section 4.3 below.

Finally, we consider aggregate earnings. Recall that at  $k = 10$  and at  $k = 24$  there are multiple equilibria (with possibly 1-4 hubs and 1-2 hubs, respectively), while at  $k = 36$  there exists a unique equilibrium (with a single hub). As aggregate investment is constant at 12 in all cases aggregate earnings are falling in the number of links in an equilibrium: the equilibrium with a single hub is efficient. If we focus on the efficient equilibrium then it is easy to check that aggregate earnings will fall by 78 as the costs of linking increase from  $k = 10$  all the way to  $k = 36$ . This is the maximum decline in equilibrium earnings possible as we raise costs of linking. On the other hand, the minimum fall in earnings is 48 and corresponds to the case when players choose the 4-Star equilibrium when  $k = 10$ . Table 3 reports the movement in aggregate earnings across different linking cost treatments. We find a significant drop in median earnings – from 680 to 611 – as we raise costs from  $k = 10$  to  $k = 36$ .<sup>22</sup> Thus the experiment supports Hypothesis 1(e), aggregate welfare are falling sharply in costs of linking.

We next turn to effects of heterogeneity in the costs of investment. Hypothesis 2 predicts that, *if linking costs are low ( $k = 10$ ), heterogeneity with respect to costs of investment increases specialization: (a) the low-cost player is the hub. Moreover, heterogeneity (b) reduces the number of hubs, (c) raises investment by hubs, and (d) lowers the number of links when compared to the homogeneous case, while (e) aggregate investment rises.*

First we test whether the low-cost player is a hub player. Here we follow the theoretical prediction for the heterogeneous treatments and focus on Hub3 (someone who has an in-degree equal to 3), because the definition of Hub2 would be too lenient and bias our results in favour of the theory. Table 6 presents logistic estimations for Treatment IV and for all heterogeneous Treatments IV-VI with a dummy for Hub3 as the dependent variable (Columns 1 and 3). As our most important variable of interest we include a dummy for the low-cost player as explanatory variable.<sup>23</sup> For robustness,

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$k = 10$  and  $k = 24$ , and of  $k = 24$  and  $k = 36$ , respectively. The corresponding  $z$ -values of Wilcoxon rank-sum tests for the equality of medians are  $z = 0.328$  and  $z = 0.861$ , respectively.

<sup>22</sup>This fall of aggregate earnings is statistically significant at a 99% level of confidence across all levels of  $k$  (Wilcoxon rank-sum test as well as a Kolmogorov-Smirnov test).

<sup>23</sup>All control variables of the econometric specification in Table 10 are also included in

Table 6 also reports all estimations for Hub2 (Columns 2 and 4). The results of all econometric specifications clearly confirm Hypothesis 2(a): for a low-cost player the odds of being a Hub3 (or Hub2) are 5.692 (or 4.152) times larger than for high-cost players.

— Insert Table 6 here —

We further examine the effect of cost heterogeneity on the number of hubs. Table 5 shows that the average number of players per group that qualify as a Hub3 in the heterogeneous Treatment IV is 0.693, but not significantly lower than the corresponding average in the homogeneous baseline treatment (0.684). This also applies to Hub3-comparisons between heterogeneous and homogeneous treatments for  $k = 24$  (0.623 vs 0.614).<sup>24</sup> Thus, Hypothesis 2(b) is not confirmed.

Despite the fact that investment by Hub3 players is lower than the theoretically predicted level of 13, it is higher in the heterogeneous treatment than in the homogeneous treatment.<sup>25</sup> Moreover, the subgroup of Hub3 players that are also low-cost players in Treatments IV, V and VI invest significantly more than the Hub3 players in Treatments I, II and II respectively.<sup>26</sup> Hence, overall, we find some support for Hypothesis 2(c).

Table 3 shows that networks in the heterogeneous Treatment IV with  $k = 10$  have, on average, 4.965 directed links, which is more than theoretically predicted (3 links, for all heterogeneous treatments) and statistically not different from the average number of links in the corresponding homogenous Treatment I (4.842). Hence, we find no support for Hypothesis 2(d), which predicted a lower number of links in the homogeneous treatment.

Table 3 also reports equal aggregate investments in Treatment IV and Table 6, with the exception of a dummy for  $c$ , as we focus on the heterogeneous sample only.

<sup>24</sup>For  $k = 36$  theory predicts that there should not be a difference, and this is indeed confirmed (0.465 vs 0.412).

<sup>25</sup>A  $t$ -test comparing the mean investments of Hub3 players in the heterogeneous with the homogeneous treatment (see Table 5) is significant with  $p = 0.077$  (one-tailed).

<sup>26</sup>A Wilcoxon rank-sum and two-tailed  $t$ -test (unreported) show that the investment levels of the subgroup of Hub3 players that are also low-cost players in Treatment IV are significantly higher (99% CI) than the investment levels of Hub3 players in the baseline Treatment I. This also applies to respective comparisons of Hub3 investment levels between Treatments II and V (95% CI), and between Treatments III and VI (99% CI).

Treatment I.<sup>27</sup> In addition, the OLS analysis presented in the last column of Table 10 in Appendix II (Model 5) reveals that individual investment is not significantly higher for heterogeneous treatments: the coefficient of a dummy for the homogeneous treatments is not significantly different from zero. This also applies when we rerun Model 5 of Table 10 with Treatments I and IV only (unreported). Overall, we do not find any difference between heterogeneous and homogeneous low-cost treatments, and therefore also no support for Hypothesis 2(e).

Finally, we note that the theory predicts that with heterogeneous costs, the aggregate investment must remain constant with respect to costs of linking. An inspection of Table 3 reveals that aggregate investments are rising in costs of linking, from 14 all the way to 19, as we increase the costs of linking from  $k = 10$  to  $k = 36$ . Thus the experiment with heterogeneous costs clearly violates this prediction of the theory.

Our experiments, both with the homogeneous and the heterogeneous costs, present one consistent violation of the theoretical prediction: aggregate investments are rising in the costs of linking. The next section develops an explanation for this violation.

### 4.3 Findings on aggregate investment

The results in the previous section revealed that, while the median subject accesses the theoretically predicted investment (see Section 4.1), the aggregate investment level is higher than  $\hat{y} = 12$  and is increasing with linking costs. This violates an important prediction of the theory (Hypothesis 1d).

We now propose a simple model to help us understand the patterns in aggregate investment. We start by noting that in the original model of Galeotti and Goyal (2010), players make their choices simultaneously. By contrast, in the experiment, players make choices sequentially and repeatedly, and there is an uncertain end point. Given these significant departures from the model, we interpret the consistency between the theoretical predictions and the data as strong support for key trade-offs faced by individuals in private investments and linking. There is, however, one important dimension – aggregate investment – on which there is clear difference between the theoretical prediction and the experimental data. In what follows, we propose a simple

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<sup>27</sup>Neither the medians (both 14 units) nor the means (15.386 for Treatment IV; 15.175 for Treatment I) are statistically different (Wilcoxon rank-sum and  $t$ -test).

notion of stability to explore the role of strategic posturing in a dynamic setting.

The model we develop is an attempt at bridging the gap between the static theoretical model and the possibilities of strategic posturing created by the dynamic game being played in the experiment. Our model builds on earlier work by Bramoullé and Kranton (2007) on the stability of investment behaviour on fixed networks, and Page and Wooders (2009) and Dutta et al. (2009) on the stability of network formation processes.

The main idea here is that, toward the end of the game, players explore small and local moves to improve their payoffs. In this exploration they take into account the possible response of other players but as time is short they do not believe that it is worth working through the consequences of long sequences of moves and counter moves. More formally, given a profile  $s$ , a player  $i$  asks if she can change her investment or her linking and if that can conceivably improve her payoffs, given that possibly one other player may have a chance to respond. A strategy profile  $s$  is said to be stable if there exists no small and local deviation that may be profitable in this sense.

We start with an analysis of the stability of the equilibrium predictions in the theoretical model. The first observation is that a hub player has an incentive to shade their investments: if the shading is very large peripheral player(s) will best respond by deleting links but if the shading is small then they will best respond by simply raising their investment correspondingly. In this situation, the payoffs of the hub player will definitely increase. We have thus shown that the equilibrium outcomes identified in Treatments I-III are not stable in a dynamic setting

We now turn to the study of stable outcomes. Following on the above argument, the next step is to develop bounds on the level of shading that the hub-player can practice. Our analysis of these bounds is summarized as follows:

**Observation:** *Fix a strategy profile  $s$  in which the network is a core-periphery network with  $m$  hub players and  $n-m$  periphery players. Let  $x_i$  denote investment by a hub-player and  $x_j$  the investment by a periphery player. This profile is stable only if the investments respect the following restrictions:*

$$x_i = \frac{k}{c} + \frac{z^*}{m}; \quad x_j = \hat{y} - \frac{mk}{c} - z^*,$$

with

$$\hat{y} - \frac{(m+1)k}{c} \leq z^* \leq \hat{y} - \frac{mk}{c}.$$

We note an important feature of these investment restrictions: a hub player accesses investments in excess of  $\hat{y}$ , while periphery players access investments exactly equal to  $\hat{y}$ .

The key step is the derivation of the bounds on  $z$  and we present it here; the rest of the derivation is presented in Appendix I. Consider the incentives to reduce investments by the periphery: in the dynamic setting there is the possibility that the hub player responds by raising her investment. We now show that if  $z$  is small then the hub is accessing sufficient investments and will not raise his investment in response. To check this let us take the investment of this one periphery player all the way down to 0. The hub will still access

$$m \left( \frac{k}{c} + \frac{z}{m} \right) + (n - m - 1) \left( \hat{y} - \frac{mk}{c} - z \right)$$

And it may be checked that this is in excess of  $\hat{y}$  if

$$z^* \leq \hat{y} - \frac{mk}{c}$$

(for  $n - m \geq 2$ ).

As periphery players get no incoming links, their investments must be justified (in themselves), and there must be no incentive to form a link with another peripheral player. As aggregate investments accessed by a peripheral player are  $\hat{y}$ , we only need to check the no-new-link constraint, i.e.,  $x_j < k/c$ . This is true if

$$z > \hat{y} - \frac{(m+1)k}{c}$$

Putting together these two conditions gives us the required restrictions on  $z^*$ . We now illustrate the implication of these restrictions, for our different cost treatments. To fix ideas we focus on the case of a single hub.

Consider the low cost case  $k = 10$ : we can compute the bounds for  $z$  to be  $8 < z < 10$ . The hub player sets minimum possible investment and so we get  $x_i = 10$  and  $x_j = 2$ . So aggregate investment is equal to 16. In

the medium costs case,  $k = 24$ , the bounds for  $z$  are  $2.4 < z < 7.2$ . The hub player sets  $x_i = 7.2$  and  $x_j = 4.8$ . So aggregate investment is equal to 21.6. Finally, consider the high cost case,  $k = 36$ . It is easy to compute that  $-2.4 < z < 4.8$ . The hub player sets minimum possible  $z$ , i.e.,  $z = 0$ . We then get  $x_i = 7.2$  and  $x_j = 4.8$ . So aggregate investment is equal to 21.6. We can use similar methods to compute the bounds on  $z$  for outcomes with multiple hub players. They are presented in the appendix and indicate that aggregate investment will be lower in case there are multiple hubs.

Taken together, our computations demonstrate one, that aggregate investments in a stable outcome in the dynamic model can be larger than the equilibrium investments in the original static model and two, that they are increasing in linking costs. These two predictions are consistent with the patterns observed in our experiment.

To close the circle, we now return to the data from our experiments and show that an important prediction of this new model is also satisfied: hubs typically overinvest relative to the static best response, while periphery players roughly play a best response in investment levels.

Table 4 shows that in the baseline treatment the network is connected in over 92.11% of the cases. Table 7 shows that in Treatments I and II the hub does indeed over-invest relative to the best response given his neighbors' choices, while the non-hubs choose actions roughly in line with their best response.

— Table 7 here —

We conclude by showing that the investment shading practiced by the hubs has large payoff effects. Table 8 presents data on payoffs of hubs and peripheral players. Hubs earn significantly more than peripheral players (99% CI); this order of earnings reverses the ranking of equilibrium payoffs in the static Galeotti-Goyal model!

— Table 8 here —

## 5 Conclusion

Individuals and organizations acquire information privately and also invest in links with others to access information indirectly. This paper presents



an experiment on the economic consequences of changes in the relative cost of these two activities.

The experiment is based on a theoretical model of local public goods and linking. We find that a decline in linking costs can have large effects. Individual investments in local public goods are more dispersed and they are accompanied by greater linking activity and hence, denser social networks. Aggregate investment falls, but investment accessed by individuals remains stable, due to increased networking. The overall effect is a significant increase in individual utility and aggregate welfare.

Our experiment is conducted with 4 subjects. In future work, it would be important to test the scope of the theory by conducting experiments on significantly larger groups.

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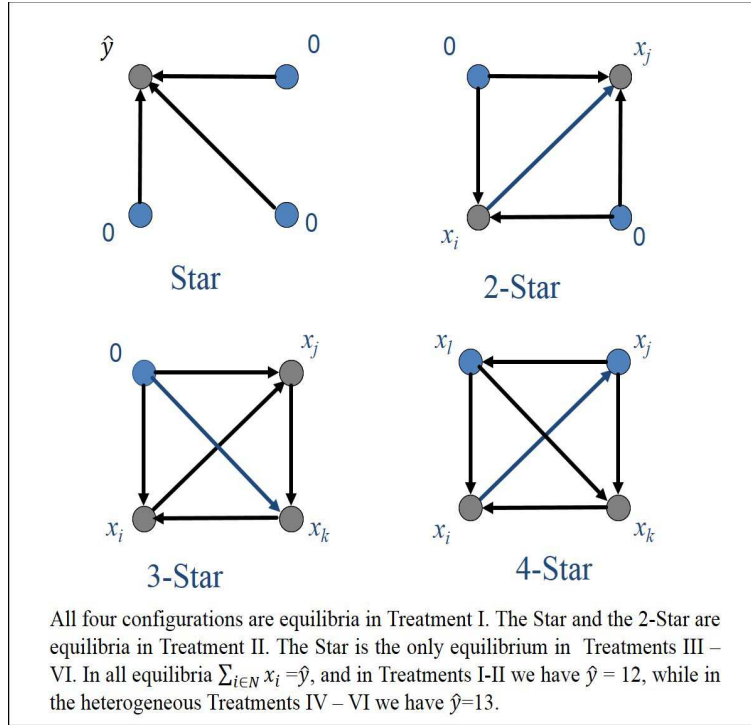


Figure 1: Equilibrium configurations in Treatments I to VI.

	Costs of information acquisition		
	$k = 10$	$k = 24$	$k = 36$
Homogeneous, $c = 5$	I	II	III
Heterogeneous, $c_i = 3$	IV	V	VI

Table 1: Treatments in the experiment

	$N^*$	Mean	SD	Min	Max
Age	152	21.368	2.454	17	31
Friends in the lab	152	0.711	1.183	0	6
Male	152	35.50%	0.48	0	1
Foreign nationality	152	38.20%	0.487	0	1
Investment (final decision)	2736	4.401	3.364	0	30
In-degree (final decision)	2736	1.03	1.09	0	3
Out-degree (final decision)	2736	1.03	0.841	0	3
Linking decisions (per node, round)	38485	24.746	16.387	1	91
Investment decisions (per node, round)	96166	52.015	32.434	1	241

( $N = 152$  subjects multiplied by 18 non-trial rounds).

Table 2: Descriptive statistics of sample

Treatment		Homogeneous, $c = 5$			Heterogeneous, $c_i = 3$		
		I $k = 10$	II $k = 24$	III $k = 36$	IV $k = 10$	V $k = 24$	VI $k = 36$
Number of directed ties per group	theory	5	4	3	3	3	3
	median	5	4	3	5	4	3
	mean	4.842	3.833	3.684	4.965	3.746	3.658
	SD	(1.252)	(3.611)	(1.826)	(1.545)	(0.870)	(1.356)
Total investment per group	theory	12	12	12	13	13	13
	median	14	17	19	14	17.5	19
	mean	15.175	17.588	19.465	15.386	18.491	19.509
	SD	(4.502)	(4.560)	(6.444)	(4.586)	(4.876)	(6.886)
Total profit per group	theory	696-726	636-684	648	763	721	685
	median	680	636	611	698	645	621.5
	mean	658.588	622.526	611.912	669.491	640.956	628.5
	SD	(54.843)	(41.616)	(56.702)	(58.871)	(37.813)	(61.14)
	$N$	114	114	114	114	114	114
Individually accessed investment	theory	12	12	12	13	13	13
	median	12	12	12	13	13	13
	mean	12.693	12.993	12.879	12.833	13.564	13.355
	SD	(2.942)	(3.611)	(3.557)	(2.957)	(3.958)	(4.141)
Individual profit	theory	144-194	130-180	164,198	169,196	169,184	169,172
	median	169	158	156.5	172.5	160	160
	mean	164.647	155.632	152.978	167.373	160.239	157.125
	SD	(20.209)	(21.481)	(23.915)	(20.449)	(20.809)	(23.981)
	$N$	456	456	456	456	456	456

Table 3: Descriptive statistics at the group level

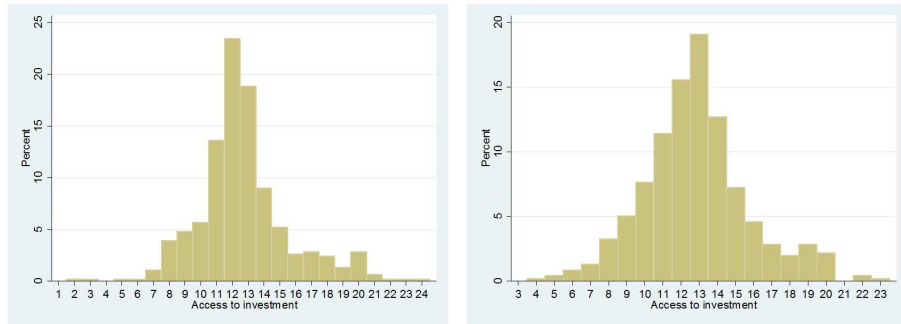


Figure 2: Distribution of investment available to individuals in Treatment I ( $c=5, k=10$ ) and Treatment IV ( $c=3, k=10$ )

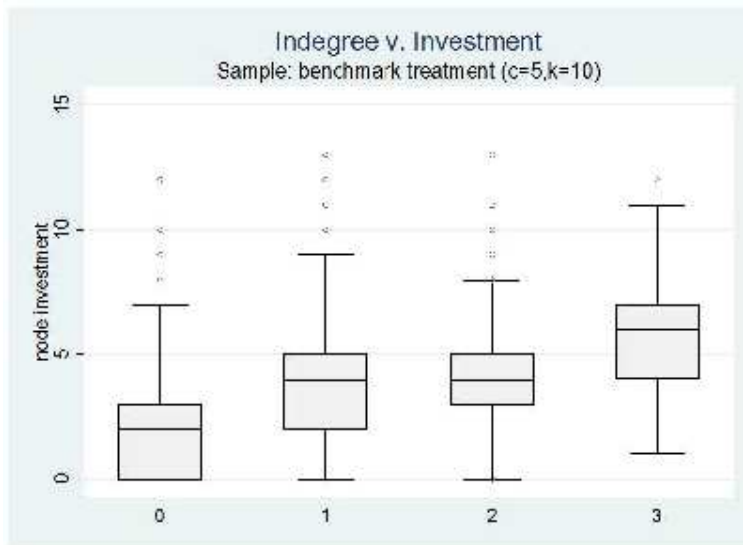


Figure 3: Box plot investment versus in-degree

Network structures	Treatment I $c = 5, k = 10$	Treatment II $c = 5, k = 24$	Treatment III $c = 5, k = 36$	Treatment IV $c_i = 3, k = 10$	Treatment V $c_i = 3, k = 24$	Treatment IV $c_i = 3, k = 36$
<b>Connected</b>	105 (92.11%)	109 (95.61%)	81 (71.05%)	104 (91.23%)	107 (93.86%)	85 (74.56%)
<b>1 Isolate</b>	4 (3.51%)	4 (3.51%)	18 (15.79%)	6 (5.26%)	4 (3.51%)	14 (12.28%)
<b>2 Isolates</b>	0	0	5 (4.39%)	0	0	2 (1.75%)
<b>Dyads</b>	5 (4.39%)	1 (0.88%)	10 (8.77%)	4 (3.51%)	3 (2.63%)	13 (11.40%)
<b>Total</b>	114	114	114	114	114	114

Table reports number of observations and % of total (in parentheses).

Table 4: Components in networks

	$N$	Hub2			Hub3		
		$n$	avg $n$ / grp (SD)	Investment median (SD)	$n$	avg $n$ / grp (SD)	Investment median (SD)
Baseline	456	182	1.596*** (0.646)	5*** (2.285)	78	0.684 (0.502)	5.962*** (2.122)
Treatment II $c = 5, k = 24$	456	124	1.088 (0.556)	7	70	0.614 (0.487)	7.314 (1.822)
Treatment III $c = 5, k = 36$	456	133	1.167 (0.879)	6	47	0.412*** (0.527)	7.362 (2.847)
Treatment IV $c_i = 3, k = 10$	456 [114]	185 [65]	1.623*** (0.755)	6	79 [42]	0.693 (0.58)	6.519*** (2.717)
Treatment V $c_i = 3, k = 24$	456 [114]	127 [70]	1.114 (0.455)	7	71 [41]	0.623 (0.503)	7.62 (2.167)
Treatment VI $c_i = 3, k = 36$	456 [114]	120 [54]	1.053 (0.687)	7	53 [33]	0.465*** (0.499)	8.226 (3.93)

\*\*\*,\*\*\* denote  $p < 0.1, < .05, < 0.01$  levels of statistical significance for Treatments I-III and IV-VI, compared with each of the remaining two levels of  $k$ .

In columns two, three and seven the number of low-cost players is given in square brackets, in column three the asterisks refer to a Kolmogorov-Smirnov test for equality of distribution functions, in columns four and nine to a Wilcoxon rank-sum (Mann-Whitney) test for equality of medians. Medians of  $k = 24$  and  $k = 36$  do not differ statistically. In columns five and ten they refer to a Kolmogorov-Smirnov test for equality of distribution functions. Means and distributions of  $k = 24$  and  $k = 36$  do not differ statistically.

Table 5: Number of hubs and investment by hubs



	Hub3 Treatment IV	Hub2 Treatment IV	Hub3 Treatments IV-VI	Hub2 Treatment IV-VI
low-cost player	5.065*** [5.349]	2.648*** [3.506]	5.692*** [9.529]	4.152*** [8.968]
$k = 10$			0.65 [-0.352]	1.254 [0.189]
$k = 36$			0.386 [-0.772]	0.62 [-0.398]
Period	0.808 [-0.536]	1.145 [0.603]	1.123 [0.336]	1.144 [0.390]
Session dummies	yes	yes	yes	yes
Period dummies	yes	yes	yes	yes
Constant	1.74 [0.116]	0.146 [-0.709]	0.048 [-1.026]	0.057 [-0.962]
No. observations	456	456	1368	1368
No. clusters	114	114	342	342
Log Likelihood	-186.224	-282.441	-508.682	-779.102
Pseudo $R^2$	0.114	0.083	0.114	0.087
$\chi^2$	49.899	167.07	112.034	160.553
Prob > $\chi^2$	0.000	0.000	0.000	0.000

Table reports odds ratios; z-values in parentheses; heteroskedasticity-consistent estimator of variance; standard errors corrected for intra-network correlation.\*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ .

Table 6: Logistic estimation on the likelihood of being a hub (Treatment IV)

<b>Hub2</b>		<b>Homogeneous, <math>c = 5</math></b>			<b>Heterogeneous, <math>c_i = 3</math></b>		
		I	II	III	IV	V	VI
		$k = 10$	$k = 24$	$k = 36$	$k = 10$	$k = 24$	$k = 36$
Hubs:	investment	5.093	6.645	6.293	5.324	7.039	7.058
	best-response	3.983	4.250	4.361	4.995	4.811	5.733
	$z$ -value	0.000	0.000	0.000	0.292	0.000	0.000
Non-hubs:	investment	2.930	3.557	4.279	2.838	3.689	4.098
	best-response	2.974	3.731	4.328	3.708	4.295	4.798
	$z$ -value	0.604	0.595	0.918	0.000	0.000	0.000

<b>Hub3</b>		I	II	III	IV	V	VI
		$k = 10$	$k = 24$	$k = 36$	$k = 10$	$k = 24$	$k = 36$
Hubs:	investment	5.926	7.314	7.362	6.518	7.620	8.226
	best-response	4.410	3.743	4.766	5.860	4.141	6.321
	$z$ -value	0.000	0.000	0.000	0.128	0.000	0.000
Non-hubs:	investment	3.347	3.868	4.579	3.286	4.070	4.437
	best-response	3.164	3.896	4.288	3.888	4.494	4.876
	$z$ -value	0.170	0.718	0.023	0.000	0.000	0.000

The  $z$ -values correspond to Wilcoxon rank-sum tests, significance is also confirmed in two-tailed  $t$ -tests.

Table 7: Best-response for hubs and non-hubs

Costs	Hub <sup>1</sup>	N	Profit <sup>2</sup> (mean)	Profit $\pm 2.58 \times S.E.$		Theory		Theory vs Sample (P)
				low	high	low	high	
$c = 5,$ $k = 10$	no	274	158.8	155.3	162.3	154	194	$154 < P < 194$
	yes	182	173.5	171.1	175.8	144	184	$144 < P < 184$
	all	456	164.6	162.2	167.1	174	182	$P < 174$
$c = 5,$ $k = 24$	no	332	150.5	147.4	153.6	154	194	$P < 154$
	yes	124	169.3	166.3	172.4	130	170	$130 < P \approx 170$
	all	456	155.6	153.0	158.2	159	171	$P < 159$
$c = 5,$ $k = 36$	no	409	151.4	148.3	154.5	168	168	$P < 168$
	yes	47	166.9	161.2	172.7	144	144	$144 < P$
	all	456	153.0	150.1	155.9	162	162	$P < 162$
$c_i = 3,$ $k = 10$	no	377	165.4	162.6	168.2	198	198	$P < 198$
	yes	79	176.8	172.4	181.2	169	169	$169 < P$
	all	456	167.4	164.9	169.8	190.75	190.75	$P < 190.75$
$c_i = 3,$ $k = 24$	no	385	156.2	153.6	158.8	184	184	$P < 184$
	yes	71	182.2	178.8	185.5	169	169	$169 < P$
	all	456	160.2	157.7	162.8	180.25	180.25	$P < 180.25$
$c_i = 3,$ $k = 36$	no	403	154.9	151.9	157.8	172	172	$P < 172$
	yes	53	174.4	164.8	184.0	169	169	$169 \lesssim P$
	all	456	157.1	154.2	160.0	171.25	171.25	$P < 171.25$

<sup>1</sup> Hub2 for Treatments I and II, Hub3 for Treatments III-VI.

<sup>2</sup> All hub profits are greater than non-hub profits at a confidence level (CI) of 99% (t-statistic, 2-tailed) for means and Wilcoxon rank sum test for medians.

Table 8: Profits of hubs and non-hubs

# Appendix I

1. *In Treatments I-III, aggregate investments in equilibrium are equal to 12.*

**Proof:** The proof exploits the assumption that investments take integer values and that  $n = 4$ . First, we prove that in equilibrium the network is connected. Suppose it is not connected then we need to consider networks of one, two, three (and four) isolated players and networks with disconnected pairs. Observe that no network with a single isolated player is an equilibrium: this is because the isolated player will optimally choose 12. But then from Galeotti and Goyal (2010) we know that there must be only one hub, which contradicts the hypothesis that the player is isolated. So we need to consider the case of two disconnected pairs only. When  $k = 10$  or 24, in each pair there is at least one player who chooses 6 or more. But then the larger investing player in one pair has an incentive to form a link with the larger investing players in the other pair. When  $k = 36$ , it follows that in each pair the higher investing player is choosing 8 or more. But then the higher investing player in one pair has a strict incentive to form a link with the higher investing player in the other pair.

So consider connected networks. If only one player invests then it follows from optimality that this player must be investing 12. If only two players are investing then it follows from arguments in Galeotti and Goyal (2010) that neither is investing 12. So they must be connected to each other. This implies from optimality of individual actions that each of them must access exactly 12. Consider next the case that 3 players are investing. Again all of them must be investing strictly less than 12. As everyone accesses 12, each of them must access at least one other player. If a positive investing player accesses all three then the sum total investments must equal 12. So in the three investors case we have proved that the sum of investments must equal 12.

Finally, consider the case that all four players make positive investments. We first consider the case that a player with  $x$  is a leaf. Observe that in this case there is a player with  $y$  such that  $x + y = 12$ . However, as the network is connected  $y$  must have one other link with someone with investment  $z$ . So there is a player who accesses  $x + y + z$ , where all investments are positive. From optimality of individual investments it follows that  $x + y + z = 12$ , but this is a contradiction. So no player is a leaf. Similarly, we can show that a network in which a player has three links must imply that this player accesses

all investments, which must then be equal to 12. So the only possibility left is that every player has two links. This means that the network is a ring. This means that all players must make equal investments and sum of three investments must equal 12. In other words, every player invests 4. This is impossible if  $k = 24$  or  $k = 36$ . If  $k = 10$ , then each player is strictly better off cutting down own investment and linking with a new player. This completes the proof. **QED**

**2.** *In Treatments IV-VI, in equilibrium all high-cost players choose 0 investments.*

**Proof:** The proof of connectedness is as in the previous result. So from now on we restrict attention to connected networks.

We go through the different cases with 1, 2, 3 and 4 contributors. Suppose there is 1 contributor. This contributor cannot be the high-cost (H) player as he will choose 12; but then the low-cost (L) player will raise his investment to a positive amount so that total investment accessed is 13.

Next consider the case of two contributors. If both players are high cost and contributing then neither can be contributing 12. But then it follows from optimality of individual behavior that the sum of investments must be 12. But then an L player will have a strict incentive to increase investment to 1. So consider the case where one investor is H and the other is L. Again it follows that the sum must be 13 and both players must access each other. But then, the H player is accessing too much investment.

Consider next the case of 3 contributors. We need to separately consider the case of three H players, 2 H players and 1 L player. Straightforward arguments exploiting the fact that an L player must access at least 13 and an active H player must access exactly 12 imply that there is no equilibrium like that.

Finally, consider the case of 4 contributors. Here we follow the line of argument in the previous result. We start by showing that a player cannot be peripheral in an equilibrium network. We then consider networks in which no player is peripheral. Here we take up networks in which some player has 3 links. If this is an H player then it contradicts the requirement that an H player must access exactly 12, while there is an L player who is accessing exactly 13. Similarly, if the L player has 3 links then we need to consider a range of networks with 3, 4, 5 and 6 links and in each case we can use integer investments, and the requirement that the L player must access exactly 13,

while the H player accesses exactly 12, to show that this cannot be sustained in equilibrium. This leaves only the case in which every player has exactly 2 links. In the ring network, it can be checked that we run afoul of integer constraints. So 4 contributors cannot be sustained in equilibrium. We are left with only one option: one contributor who is of the low-cost type. **QED**

**Proof of Observation:** We start with incentives of the hub player.

- Adding a link to hub player: this would simply lower payoff by  $k$  and is clearly unprofitable.
- Cutting a link to hub player: this can potentially raise payoffs by  $k$ .
- Increasing information acquisition: the hub player already accesses investments in excess  $\hat{y}$ . All other players are already connected to the hub. So an increase in investment can only lead to lower investments by others and thus lower utility.
- Reducing information acquisition: we know that lower investments than  $\hat{y} - (m + 1)k/c$  will mean that periphery players invest in excess of  $k/c$  and this will lead to switches between self investment and links with other peripheral players, thus destroying the core-periphery network.

We next consider incentive of the periphery player:

- Severing the link to hub: this will clearly reduce payoffs since  $x_i > k/c$  and aggregate investments accessed by periphery player are  $\hat{y}$ .
- Adding a link to non-hub player: this is clearly unprofitable as  $x_j < k/c$ . It will also not raise investments of the new neighbor as this player will then accessing investments in excess of  $\hat{y}$ .
- Reducing investments: this is unprofitable as total investments accessed are  $\hat{y}$  and lower investment will not induce greater investment from current hub contacts. This was explained in the main text of the paper and defines the upper bound for  $z$ .
- Increasing investment: this is not by itself profitable as periphery player is accessing  $\hat{y}$  in current profile. So the only incentive would be a link from a periphery player. However, such a link would lead to that new contact lowering investment to 0. So again increasing investment cannot be profitable.

■

We now compute the bounds for  $z$  for the different cost of linking and for the different core-periphery networks. The case with single hub has already

been presented in the main text. We now complete the other cases,  $k=24$  and  $m=2$ : The bounds for  $z$  are  $-2.4 < z < 2.4$ . So investment by a hub player is  $x_i = 4.8$  and by the periphery player is  $x_j = 2.4$ . This means that aggregate investment is 14.4.

Turning to the low cost case  $k = 10$ . For  $m = 2$ , we find the bounds for  $z$  are  $6 < z < 8$ . The investment by the hub is  $x_i = 5$  and the investment by the peripheral player is  $x_j = 2$ . This means that the aggregate investment is 14.

## Appendix II

Session	Treatments					
	I ( $k = 10, c = 5$ )	II ( $k = 24, c = 5$ )	III ( $k = 36, c = 5$ )	IV ( $k = 10, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	VI ( $k = 36, c_i = 3$ )
1	I ( $k = 10, c = 5$ )	II ( $k = 24, c = 5$ )	III ( $k = 36, c = 5$ )	IV ( $k = 10, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	VI ( $k = 36, c_i = 3$ )
2	III ( $k = 36, c = 5$ )	II ( $k = 24, c = 5$ )	I ( $k = 10, c = 5$ )	VI ( $k = 36, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	IV ( $k = 10, c_i = 3$ )
3	IV ( $k = 10, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	VI ( $k = 36, c_i = 3$ )	I ( $k = 10, c = 5$ )	II ( $k = 24, c = 5$ )	III ( $k = 36, c = 5$ )
4	VI ( $k = 36, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	IV ( $k = 10, c_i = 3$ )	III ( $k = 36, c = 5$ )	II ( $k = 24, c = 5$ )	I ( $k = 10, c = 5$ )
5	I ( $k = 10, c = 5$ )	II ( $k = 24, c = 5$ )	III ( $k = 36, c = 5$ )	IV ( $k = 10, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	VI ( $k = 36, c_i = 3$ )
6	III ( $k = 36, c = 5$ )	II ( $k = 24, c = 5$ )	I ( $k = 10, c = 5$ )	VI ( $k = 36, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	IV ( $k = 10, c_i = 3$ )
7	IV ( $k = 10, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	VI ( $k = 36, c_i = 3$ )	I ( $k = 10, c = 5$ )	II ( $k = 24, c = 5$ )	III ( $k = 36, c = 5$ )
8	VI ( $k = 36, c_i = 3$ )	V ( $k = 24, c_i = 3$ )	IV ( $k = 10, c_i = 3$ )	III ( $k = 36, c = 5$ )	II ( $k = 24, c = 5$ )	I ( $k = 10, c = 5$ )

Table 9: Sequence of treatments



	Model 1 Baseline Treatment I	Model 2 Treatment IV $c_i = 3, k = 10$	Model 3 Homogeneous Treatments I-III	Model 4 Heterogeneous Treatments IV-VI	Model 5 Full Sample
in-degree	1.367*** [13.501]	1.574*** [12.183]	1.316*** [18.549]	1.528*** [17.893]	1.413*** [25.094]
$k = 10$			-0.868** [-2.493]	-1.328*** [-3.581]	-0.926** [-2.364]
$k = 36$			0.581 [1.565]	0.204 [0.506]	0.56 [1.423]
Homogeneous costs					-0.095 [-0.753]
Round	-0.088 [-0.510]	-1.99 [-0.735]	0.017 [0.100]	0.091 [0.496]	-0.079 [-0.376]
Session dummies	yes	yes	yes	yes	yes
Period dummies	yes	yes	yes	yes	yes
Constant	1.911*** [2.805]	1.770 [1.927]	2.962*** [6.241]	3.048*** [5.803]	3.325*** [9.473]
No. observations	456	456	1368	1368	2736
No. clusters	114	114	342	342	684
$R^2(\text{adj.})$	15.261	13.090	16.953	16.467	26.872
$F$	0.340	0.328	0.214	0.227	0.221
$\text{Prob} > F$	0.000	0.000	0.000	0.000	0.000

Table reports t-values in parentheses; heteroskedasticity-consistent estimator of variance; standard errors corrected for intra-network correlation; period and session dummies incl. \*  $p < 0.1$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ .

Table 10: OLS regressions with individual investment as dependent variable, Treatments I - VI

	Treatment I $c = 5, k = 10$	Treatment II $c = 5, k = 24$	Treatment III $c = 5, k = 36$	Treatment IV $c_i = 3, k = 10$	Treatment V $c_i = 3, k = 24$	Treatment VI $c_i = 3, k = 36$
<b>Data</b>						
Equilibria	1 (0.8%)	4 (3.4%)	2 (1.7%)	2 (1.7%)	0	0
Equilibrium structures	29 (25.4%)	34 (29.7%)	17 (14.9%)	5 (4.4%)	22 (19.29%)	14 (12.28%)
<b>Chance</b>						
Equilibria	< 0.01 (< 0.001%)	< 0.01 (< 0.001%)	< 0.01 (< 0.001%)	< 0.01 (< 0.001%)	< 0.01 (< 0.001%)	< 0.01 (< 0.001%)
Equilibrium structures	5.79 (5%)	3.56 (3.1%)	1.78 (1.5%)	0.44 (0.4%)	0.44 (0.4%)	0.44 (0.4%)
Total	114	114	114	114	114	114
Table reports number of observations and % of total (in parentheses).						

Table 11: Frequencies and percentages of equilibria and equilibrium structures



## - Instructions -

Please read the following instructions carefully. These instructions are equal for all the participants. The instructions state everything you need to know in order to participate in the experiment. If you have any questions, please raise your hand. One of the experimenters will approach you in order to answer your question.

You can earn money by means of earning points during the experiment. The number of points that you earn depends on your own choices and the choices of other participants. At the end of the experiment, the total number of points that you earn during the experiment will be exchanged at an exchange rate of:

**200 points = 1 Euro**

The money you earn will be paid out in cash at the end of the experiment without other participants being able to see how much you earned. Further instructions on this will follow in due time. During the experiment you are not allowed to communicate with other participants. Turn off your mobile phone and put it in your bag. Also, you may only use the functions on the screen that are necessary to carry out the experiment. Thank you very much.

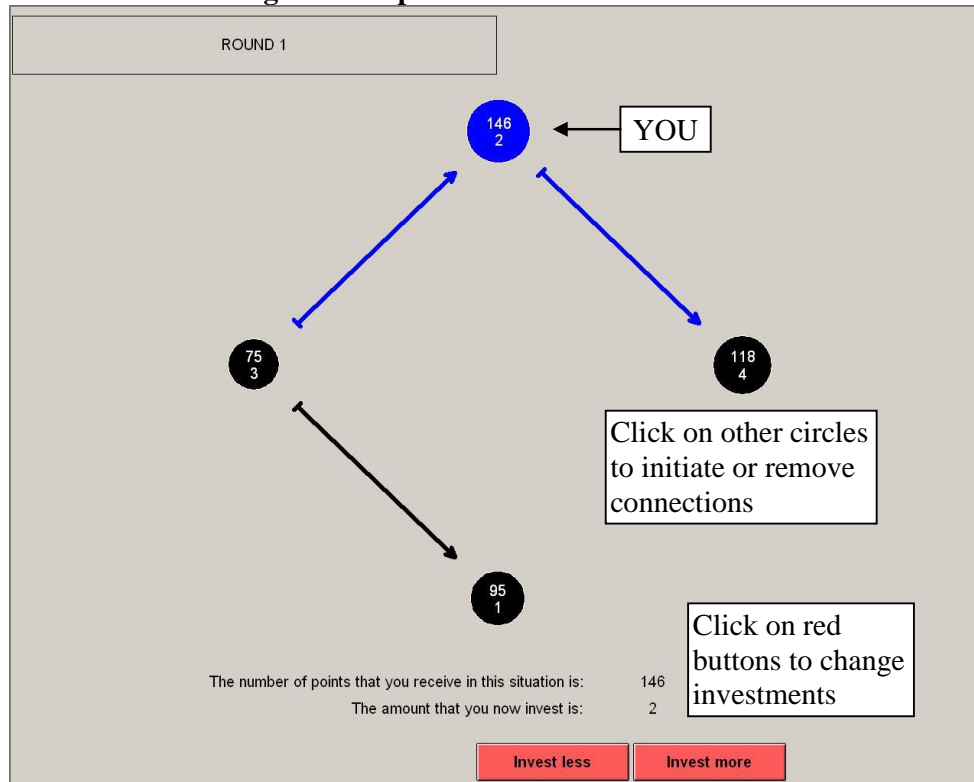
## - Overview of the experiment -

The experiment consists of *six scenarios*. Each scenario consists again of *one trial round* and *three paid rounds* (altogether 24 rounds of which 18 are relevant for your earnings).

In *all scenarios* you will be *grouped* with three other randomly selected participants. At the beginning of *each of the 24 rounds*, the groups and the positions within the groups will be randomly changed. The participants that you are grouped with in one round are very likely different participants from those you will be grouped with in the next round. It will not be revealed with whom you were grouped at any moment during or after the experiment.

The participants in your group will be shown as circles on the screen (see Figure 1). You are displayed as a **blue** circle, while the other participants are displayed as **black** circles. You will be able to connect to one or more other participants in your group during each round. By clicking on one of the other participants, you become connected to this other participant. An arrow appears to indicate the connection. By clicking again on the participant the arrow and, thus, the connection is removed again. You are also connected to another participant if this other participant clicks once on you. The participant on whose side a one-sided arrow starts has initiated this connection and has to pay some points for this connection. If both participants have clicked for a specific connection a two-headed arrow appears and both participants need to pay points for this connection. All participants that are connected to you by any kind of arrow will be called *your neighbors*. Hence, in Figure 1 the participants with “75” and with “118” in their circles are your neighbors.

**Figure 1: Explanation of screen elements**



You can earn **points** in a round by investing, but investing also costs points. The points you receive in the end depend on your own investment and the investments of your neighbors. By clicking on one of the two buttons at the bottom of the screen you increase or decrease your investment. At the end of the round, you receive the amount of points that is shown on the screen at that moment in time. In other words, your final earnings only depend on the situation at the end of every round.

Each round lasts *between 105 and 135 seconds*. The end will be at an unknown and random moment in this time interval. Therefore, different rounds will not last equally long.

The points you will *receive* can be seen as the *top number* in your blue circle. The points others will receive are indicated as the top number in the black circles of others. Next to this, the *size of the circles* changes with the points that you and the other participants will receive: a larger circle means that the particular participant receives more points. The *bottom number* in the circles indicates the amount *invested* by that participant.

**Remarks:**

- It can occur that there is a time-lag between your click and the changes of the numbers on the screen. One click is enough to change a connection or to change your investment by one unit. A subsequent click will not be effective before the previous click is effectuated.
- **Therefore wait until a connection is changed or your investment is adapted before making further changes!**

**- Your earnings -**

Now we explain in detail how the number of points that you earn depends on the investments and the connections. Read this carefully. Do not worry if you find it difficult to grasp immediately. We also present an example with calculations below. Next to this, there is a trial round for each scenario to gain experience with how connections and investments affect your earnings.

In all scenarios, the points you receive at the end of each round depend in a similar way on two factors:

- 1. Every connection that you initiated yourself costs a given number of points (this will be either 10, 24 or 36).**
- 2. Every unit that you invest yourself will cost you 5 points most of the time; in some scenarios, there is one participant in your group (maybe yourself) for whom every unit investment costs only 3 points. This participant will be displayed with an additional square around the circle (see Figure 3).**
- 3. You earn points for each unit that you invest yourself and for each unit that your neighbors invest (the earnings related to a neighbor's investments do not depend on whether an arrow points toward yourself, toward the neighbor, or in both directions).**

If you sum up all units of investment of yourself and your neighbors, the following table gives you the points that you earn from these investments:

Your investment plus your neighbors' investments	0	1	2	3	4	5	6	7	8	9	10
Points	0	28	54	78	100	120	138	154	168	180	190

Your investment plus your neighbors' investments	11	12	13	14	15	16	17	18	19	20	21
Points	198	204	208	210	211	212	213	214	215	216	217

The higher the total investments, the lower are the points earned from an additional unit of investment. Beyond an investment of 21, you earn one extra point for every additional unit invested by you or one of your neighbors.

**Note: if your and your neighbors' investments add up to 12 or more, earnings increase by less than 5 points for each additional unit of investment.**

**- Example shown in Figure 2 -**

Suppose

1. initiating connections costs 24 points in this scenario;
2. you initiated one connection with one participant and one other participant initiated a connection with you;
3. you invested 2 units;
4. one of your neighbors invested 3 units and the other neighbor invested 4 units.

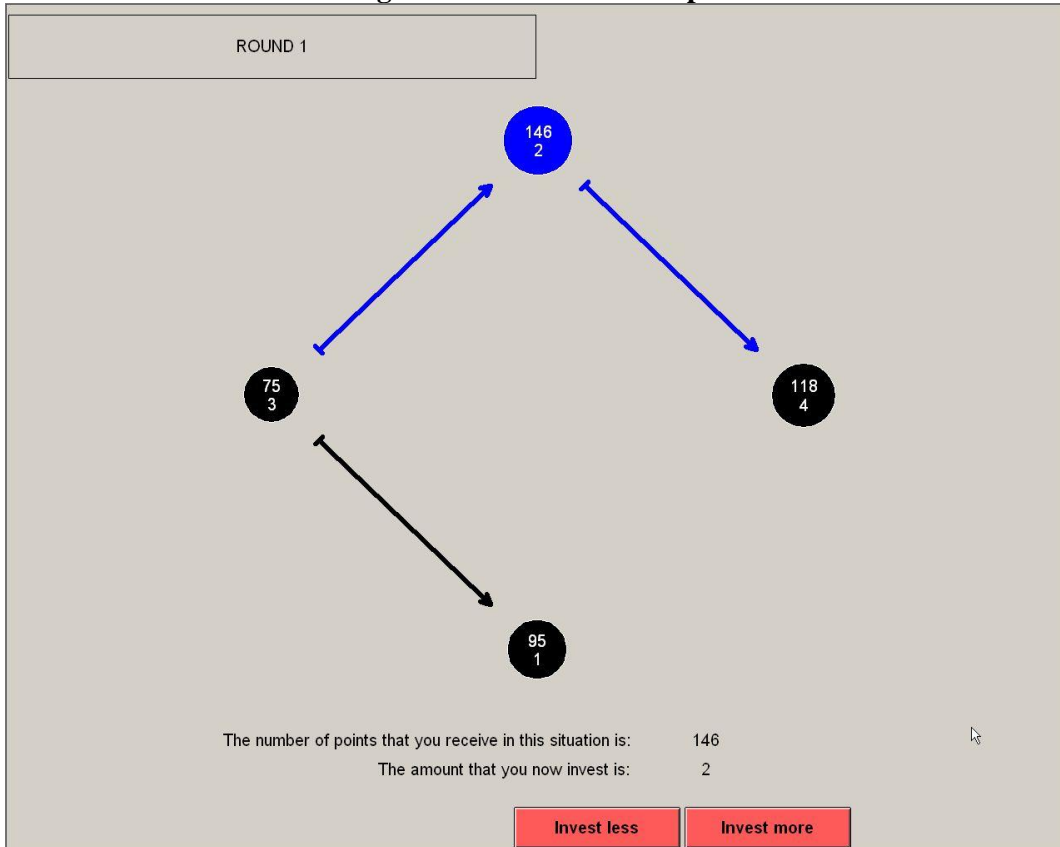
Then you have to pay 24 points for the connection you initiated and 2 times  $5 = 10$  points for your own investments. Therefore, your total costs are 34 points.

The investments that you profit from are your own plus your neighbors' investments:  $2 + 3 + 4 = 9$  (see bottom numbers in the circles from you and your neighbors on the right and on the left). In the table you can see that your earnings from this are 180 points.

In total, you would receive  $180 - 34 = 146$  points if this would be the situation at the end of the round. Figure 2 shows this example as it would appear on the screen. The investment of the fourth participant in your group (at the bottom of the screen) does not affect your earnings. In the trial round before each scenario, you will have time to get used to how the points you receive change with investments.

The participant on the left has initiated two connections, invests in 3 units himself and profits from  $3 + 2 + 1 = 6$  units in total. Therefore, this participant receives in this situation  $138$  (see table)  $- 2 \times 24 - 3 \times 5 = 75$  points.

**Figure 2: Numerical example**



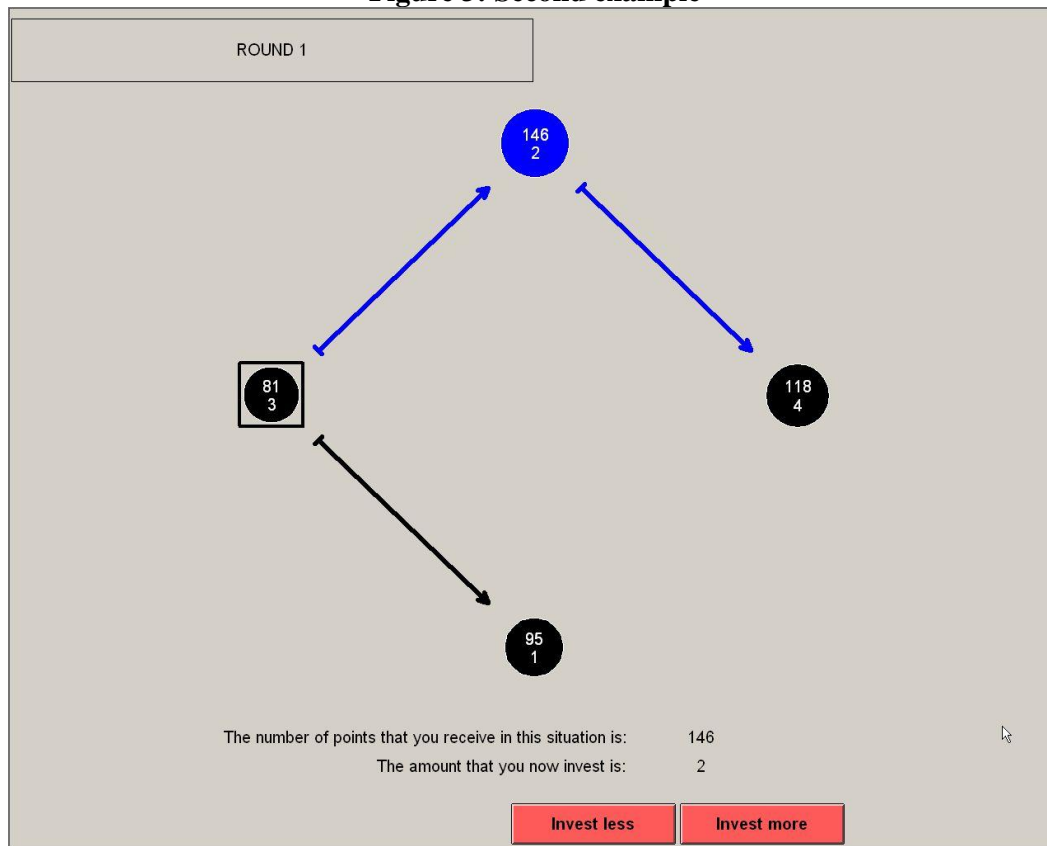
## - Scenarios -

All rounds are basically the same. The things that change between scenarios are:

1. The costs for a connection will be 10, 24, or 36 points.
2. There might be one participant who pays only 3 points per unit of investment. This participant is marked with an additional square. In Figure 3, this is the participant on the left. This participant earns 6 points more than in Figure 2 because he pays  $3 \times 2 = 6$  points less for his three units of investments, which brings his total earnings to  $138 - 2 \times 24 - 3 \times 3 = 81$ .

When a new scenario starts, you will get a message on the screen that describes the new scenario. Please read these messages carefully. As indicated before each scenario starts with a trial round. At the top of the screen you can also see when you are in a trial round. Paying rounds are indicated by "ROUND" while trial rounds are indicated by "TRIAL ROUND".

**Figure 3: Second example**



## - Questionnaire -

After the 24 rounds you will be asked to fill in a questionnaire. Please take your time to fill in this questionnaire accurately. In the mean time your earnings will be counted. Please remain seated until the payment has taken place.