The effect of different particle residence time distributions on the chemical looping combustion process

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A model for a reactor-regenerator system has been developed. Residue time distribution of solids is important in chemical looping combustion. Reducing the extent of solid mixing increases the extent of conversion and rates. Residence time distribution of solids should be accounted for in simulations.

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ABSTRACT

A model for chemical looping combustion has been developed to allow the effect of different residence time distributions of oxygen carrier particles in the air and fuel reactors to be investigated. The model envisages two, coupled fluidised bed reactors with steady circulation of particles between them. The results show that the process is sensitive to the residence time distributions, particularly when the mean residence time of particles in the reactors is similar to the time required for them to react completely. Under certain operating conditions, decreasing the variance of the residence time distribution, leads to a greater mean conversion of the particles by the time they leave the reactors and higher mean rates of reaction in the beds. In this way the required inventory and circulation rate of solids could be reduced, which would lower the capital and operating costs of a CLC process. Since the residence time distribution of solids is important, it should be taken into account when modelling or designing a chemical looping combustion process, e.g. by using a tanks-in-series model. This work indicates that if the number of tanks, \( N \leq 5 \), knowing \( N \) to the nearest integer is generally sufficient, unless a high degree of accuracy is needed. As \( N \) increases, the sensitivity of the coupled system decreases, so for \( N > 5 \), knowing the value to the nearest 5 or 10 tanks is sufficient. This is valid whether \( N \) is the same or different in the two reactors. Chemical looping combustion is one example of a reactor-regenerator system, so the results are also relevant for other processes of this type, such as fluidised catalytic cracking.

1. Introduction

Chemical looping combustion (CLC) is a technique which allows fossil fuels to be burnt with inherent capture of the carbon dioxide emissions. It is based on the redox cycling of an oxygen carrier, which is typically an oxide of a transition metal. The carrier supplies oxygen from its crystal lattice in the fuel reactor and is reduced in the process. It is then transferred to the air reactor where the oxide is regenerated by reaction with air. CLC is thus a type of reactor-regenerator system, often exemplified by fluidised catalytic cracking [1]. Generally CLC is designed in a configuration consisting of two interconnected fluidised bed reactors [2,3], as shown in Fig. 1. Reduction of the oxygen carrier takes place in the fuel reactor, while regeneration is conducted in the air reactor.

A significant amount of research has been conducted on CLC, ranging from the scale of the oxygen carrier materials [2,4] up to the industrial scale, such as modelling the integration of CLC reactors with a power cycle for generating electricity [5]. At the scale of the interconnected fluidised bed reactors, a number of different pilot scale units have been built and operated with a variety of different oxygen carrier...
In general, the solids in fluidised beds are assumed to be well-mixed [19–23]. As a result, a tanks-in-series (TIS) model is often used to represent the RTD function [24–28], where it is assumed that the system consists of $N$ continuous stirred tank reactors (CSTRs), of equal volume, in series. Each tank is statistically independent and, in each, the solids are perfectly mixed. The RTD is given by [29]:

$$E(t) = \frac{N^{N-1}}{(N-1)!} \frac{e^{-\frac{t}{\bar{t}}}}{\bar{t}^N}$$

(4)

where $t$ is the time a particle spends in the overall reactor. $N = 1$ corresponds to a well-mixed system and as $N \to \infty$, the RTD from the model approaches plug flow. The variance, $\sigma^2$, of the RTD is

$$\sigma^2 = \frac{\bar{t}^2}{N}$$

(5)

In this form, the TIS model is only valid for $N \in \mathbb{N}$. The model can be adapted so that $N$ can take non-integer values e.g. the fractional tank model [29] or the gamma extension model [30]. In the gamma extension model, the gamma function, $\Gamma(N)$ is used as a generalised factorial function and replaces the $(N-1)!$ term in Eq. (4):

$$\Gamma(N) = \int_0^\infty x^{N-1}e^{-x}dx$$

(6)

where $N$ can now be any rational number greater than zero.

2. Model development

The model developed in this work was based on two, coupled fluidised bed reactors, with steady circulation of particles between them, as depicted in Fig. 1. In terms of the gas-solid reaction, a characteristic time for a particle to react completely in the air and in the fuel reactor, $t_{\text{tot,air}}$ and $t_{\text{tot,fuel}}$ respectively was specified. These two parameters were inputs to particle models, describing the rate of reaction of oxygen carrier particles, assumed to be either shrinking core (controlled by one or more of intrinsic chemical reaction, diffusion through the product layer and external mass transfer) or uniform throughout the particle [31]. In this paper, which is general for any CLC system, a non-dimensional time, $\bar{t}$ was used throughout, where

$$\bar{t} = \frac{t}{\hat{t}}$$

(7)

and $t$ is the mean residence time of particles in the air or the fuel reactor. Large values of $\bar{t}$ correspond to short residence times and small values to long residence times compared to the time taken for a particle to react completely. A non-dimensional time was used to make the model general to any CLC system, regardless of the scale. In fact it is general to any reactor-regenerator system. It also meant that it was not necessary to have precise values for $t_{\text{tot,air}}$ and $t_{\text{tot,fuel}}$.

The RTD of the particles in the reactors was modelled using a tanks-in-series (TIS) model, where $N$ can take non-integer values (Eqs. (4) and (6)). The particles were assumed to be of equal size and it was assumed that there was no irreversible decay in performance over time. The latter is an appropriate assumption to make since the time taken for the CLC process to reach a steady state would usually be short compared to the time taken for the performance of particles to deteriorate due to repetitive redox cycling. The state of conversion of particles was tracked over time. This is important since particles can build up complex local distributions of oxidised and reduced material as they are cycled between the air and fuel reactors [32].

A Monte Carlo (MC) approach was used to determine the mean conversion of the stream of particles as they leave the air and the fuel reactors, $X_{\text{air}}$ and $X_{\text{fuel}}$ respectively. The mean rates of reaction of particles within the beds were also determined. When the system is well mixed ($N = 1$), the properties of the particles within the bed are the same as the properties of the particles leaving the bed. In all other cases, there is a difference, which reaches a maximum as plug flow is
approached \((N \gg 1)\). In the MC simulation, a single particle was cycled at least 1000 times with different values of \(\theta\).

The particle being cycled carries the complete statistics of the process. When simulating steady state behaviour, these statistics remain constant over time. The ergodic hypothesis can therefore be invoked, stating that cycling one particle \(x\) times gives the same distribution of values as cycling \(x\) particles once. The initial conversion does not matter since after a small number of cycles, it becomes insignificant. From the second time that the particle enters a reactor, its initial conversion is the final conversion with which it left the other reactor i.e. the initial conditions are automatically determined. Each time the particle entered a reactor, the time that it spent there was determined using a rejection sampling algorithm from the appropriate RTD. The modelling approach was similar to that used by Schnellmann et al. [31].

The modelling approach could be applied to a specific CLC system to evaluate further aspects, such as the conversion of the fuel in the fuel reactor. This is beyond the scope of this paper. It could be done by refining the particle model and determining precise times for particles to react completely experimentally. The experiments should use the chosen oxygen carrier material and fuel and the conditions should replicate those that the particles would experience in the two reactors in the specific CLC system e.g. temperature and gas concentrations.

### 3. Results

#### 3.1. Sensitivity of CLC to the RTD functions of particles in the air and fuel reactors

A number of MC simulations were run, using the TIS model (Eqs. (4) and (6)) for the RTDs of the oxygen carrier particles. Values of \(N\), ranging from 1 to 50, were used to account for the full range of possible RTDs from well-mixed to approaching the plug flow limit, as shown in Fig. 2. The results of these simulations are shown in Figs. 3–6. For the case where the oxygen carrier particles were well mixed, the analytical solution rather than the MC result is shown [32], there being excellent agreement between the analytical solution and the MC result [31]. By accounting for the range of possible RTDs, Fig. 3 shows the envelope of possible mean conversions that particles can have when leaving the air and fuel reactors for different values of \(\theta\). Throughout this paper, results are shown for the case where the particles react according to a shrinking core model under chemical reaction control. The trends for the other forms of kinetics, described in Section 2 were similar.

From Fig. 3, it is clear that for \(\theta > 0.1\), if the RTD is changed, it has an impact on the mean conversion of particles as they leave the reactors. The sensitivity reaches a peak when \(\theta\) is between 1 and 2. This corresponds to the operating region where the mean residence time is similar to the time taken for a particle to react completely. If \(\theta\) is kept constant, a decrease in the extent of mixing leads to a greater \(\Delta X = X_{\text{fuel}} - X_{\text{air}}\), e.g. if \(\theta = 1\), an increase in the value of \(N\) in both reactors from 1 to 2 gives an increase in \(\Delta X\) from 0.682 to 0.824. Therefore the same amount of oxygen can be transferred between the
air and the fuel reactor but at a reduced solid circulation rate.

Fig. 4 shows the variation in the standard deviation of the conversion of particles as they leave the reactors, for different RTDs. As expected, it can be seen that a greater degree of mixing leads to a larger standard deviation. In the plug flow limit, for \( \theta < 1 \), there is almost no spread since the particles leave the reactors completely oxidized or reduced. A standard deviation of 0 is only achieved for \( \theta > 1 \) when there is perfect plug flow.

Fig. 5 shows how the mean rate of reaction of particles in the beds varies for different RTDs. For simplicity and so that the air and fuel reactor results are the same, the mean rate of reaction is shown relative to the well-mixed value when \( \theta = 1 \). When operating in a regime where \( \theta > 0.5 \) in the reactors, the mean rate of reaction is sensitive to different RTDs. The rate of reaction is higher when there is less mixing, which agrees with the higher mean conversion of particles as they leave the reactors seen in Fig. 3.

Fig. 6 shows the sensitivity of the standard deviation of the rate of reaction of particles in the reactors for different RTDs. For \( \theta < 0.5 \), the standard deviations are the same, irrespective of the RTD. At larger values of \( \theta \), the values diverge, with a well-mixed system exhibiting a greater spread of rate of reaction.

The values of \( \Delta X \) between the exit streams of the reactors and the mean rates of reaction in the reactors, were used to determine the circulation rate of solids, \( \dot{m}_f \) and the inventories of solids, \( m_{fuel} \) and \( m_{air} \), required of the CLC system. Thus,

\[
\dot{m}_f = \frac{2af}{\rho_o \Delta X} \tag{8}
\]

\[
\dot{m}_{fuel} = \frac{f}{r_{fuel}} \tag{9}
\]

\[
\dot{m}_{air} = \frac{af}{r_{air}} \tag{10}
\]

where \( a \) is a stoichiometric coefficient (moles \( O_2 \)/mole fuel), \( f \) is the flow rate of fuel (moles fuel/s), \( \rho_o \) is a molar density of the oxygen carrier (moles lattice \( O_2 \)/g carrier) and \( r_{fuel} \) (mol fuel/s/g carrier) and \( r_{air} \) (mol \( O_2 \)/s/g carrier) are the mean rates of reaction in the fuel and air reactors respectively. The results are shown in Fig. 7. Both the circulation rate and the inventories are given relative to the well mixed values when \( \theta = 1 \).

The lowest circulation rate is achieved when \( \Delta X = 1 \), which is the case when the particles are given sufficient time to react completely, i.e. when CLC is operated with low values of \( \theta \). As the RTD tends toward the plug flow limit, the value of \( \theta \) necessary to achieve \( \Delta X = 1 \) tends to unity. On the other hand, in order to reduce the inventories in the air and fuel reactors, a high rate of reaction in the beds and therefore operation with high values of \( \theta \) is desirable. As the RTD tends toward plug flow, it leads to lower inventories.

### 3.2. Experimental RTDs of particles

Donat [14] measured the RTDs of particles for the air and fuel reactors in a laboratory-scale circulating fluidised bed (CFB) at room temperature. Silica sand particles were used, sieved to 180–250 \( \mu \)m. The particle density, \( \rho_p \), was 2650 kg/m\(^3\), the minimum fluidisation velocity, \( U_{mf} \), was 0.0485 m/s and the bed voidage at \( U_{mf} \) was 0.465. The total inventory of particles was \( \sim 0.4 \) kg. The CFB was operated under ambient conditions, with \( U_0/U_{mf} = 6 \) and \( U_0/U_{mf} = 2.2 \) in the air and fuel reactors, respectively, where \( U_0 \) is the superficial fluidising velocity. A description of the apparatus is given in Appendix A and further information is given by Donat et al. [33]. While the CFB was in operation, positron emission particle tracking (PEPT), a non-invasive method, was used to track a single tracer particle [34]. From the results, distributions of residence times of the solids were calculated, where a single residence time was defined as the time, experimentally, that the tracer particle spent within the defined boundaries of the air and fuel reactors. The relevant volumes are shown in Fig. 14 in Appendix A. Although theoretically possible, it was not observed that the tracer re-entered the reactors after initially leaving.

The tracer particle was a gamma-alumina substitute for a sand particle of similar density, size and shape as the silica sand particles used in the CFB. The tracer particle was labelled with the proton-rich radionuclide \( ^{110} \text{P} \) (half-life \( \sim 110 \) min), which undergoes beta-decay, accompanied by the emission of positrons. Upon contact with an electron, annihilation occurs, resulting in the emission of a pair of back-to-back (180° \( \pm \) 0.5°) gamma-rays of 511 keV each. An ADAC Forte dual-headed gamma camera was used to detect these coincident gamma rays to locate the tracer particle. The \( x \), \( y \), and \( z \)-coordinates of the particle were obtained as a function of time, with the absolute error associated with each position being no more than 7 mm.

It was found that, although the mean residence time of particles changed when the circulation rate of solids, \( \dot{m}_s \), was altered, the shape of the RTD remained almost the same, within the limits investigated [35]. Typical RTDs for the air and fuel reactors are shown in Fig. 8 (\( \dot{m}_s = 3.7 \) g/s and \( \dot{m}_s = 5.9 \) g/s for the air and fuel reactor respectively). The mean residence time and the standard deviation of the RTDs were calculated from the experimental measurements, and using Eq. (5), the equivalent number of tanks in series, \( N \), was calculated. The values are shown in Table 1. The values of \( N \) calculated were used as inputs for tanks-in-series with gamma extension models for the air and fuel reactors. The resulting model RTDs are also shown in Fig. 8. Given the restricted number of data points, chi-squared goodness of fit tests were used to determine confidence intervals on \( N \) for the air and fuel reactors. The tests showed that the experimental data can be modelled satisfactorily at the 5% level, with \( N \) in the range 0.8–2.5 for the air reactor and 0.5–1.5 for the fuel reactor. The results indicate that the hydrodynamics in the two reactors are unlikely to be the same, probably due to differences in geometry. The fuel reactor can be assumed to be well-mixed with respect to solids. While this would be within the confidence interval on \( N \) for the air reactor, it is at the extreme lower end.

Two simulations were run to assess whether a TIS with gamma extension model is appropriate for modelling experimental RTDs. In the first, the experimental RTDs were used in the MC simulation i.e. the rejection sampling algorithm was used to sample directly from the experimental RTDs shown in Fig. 8. In the second simulation, the values of \( N \), given in Table 1 (\( N = 1.08 \) and \( N = 1.51 \) for the fuel and air reactors respectively) were used as parameters for the TIS with gamma extension model. In Fig. 9, the results for the mean conversion of particles as they leave the reactors are shown for both simulations. It is clear that there is excellent agreement for all values of \( \theta \). In Fig. 10, the results for the mean rate of reaction of particles in the reactors are shown for both simulations. As for the case of the mean conversion of particles as they leave the reactors, there is excellent agreement for all values of \( \theta \).
3.3. The effect of different mixing in the air and fuel reactors

The degree of mixing and therefore the value of $N$ will not necessarily be the same in both reactors of a coupled system, as demonstrated in Section 3.2. Further simulations were run where the mixing in one of the reactors (the fuel reactor) was kept constant at $N = 1$, while that in the air reactor was varied ($N = 2, 5$ and $50$). In Fig. 11, the mean conversions of particles as they leave the reactors is shown for these different cases. The mean rate of reaction of particles in the reactors is shown in Fig. 12 and Fig. 13 for the fuel and air reactors respectively. The second simulation result from Section 3.2 is also shown, with values of $N$ determined for the laboratory-scale CFB (given in Table 1). These results are also shown in Figs. 11–13.

In Fig. 9, whilst an increase in the value of $N$ leads to a significant shift in the mean conversion of particles as they leave the reactors, the increase in the important parameter, $\Delta X$ is far less significant than when $N$ in both reactors is increased. For $\theta = 1$, an increase in the value of $N$ in both reactors from 1 to 2 raises $\Delta X$ from 0.682 to 0.824 (Fig. 3), while when $N$ is increased in the air reactor only from 1 to 2, $\Delta X$ rises to 0.731 (Fig. 11). The mean rate of reaction in the beds also increases much less significantly when only the mixing in the air reactor is changed (Figs. 12 and 13). The trends are exactly the same when $N$ is kept constant in the air reactor and varied in the fuel reactor. As

![Fig. 8. RTDs for a laboratory-scale CFB, determined from positron emission particle tracking data [35] and the model fit using the values of $N$ from Table 1 in a tanks-in-series with gamma extension model, (a) is for the air reactor and (b) for the fuel reactor.](image)

<table>
<thead>
<tr>
<th>Number of data points</th>
<th>Mean residence time, $\tau$ (s)</th>
<th>Standard deviation, $\sigma$ (s)</th>
<th>$N$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fuel reactor</td>
<td>90</td>
<td>36.0</td>
<td>34.7</td>
</tr>
<tr>
<td>Air reactor</td>
<td>71</td>
<td>22.2</td>
<td>18.1</td>
</tr>
</tbody>
</table>

**Table 1**
The mean residence times, standard deviation and the equivalent number of tanks-in-series for the RTDs from a laboratory-scale CFB [35].

![Fig. 9. Mean conversions of particles as they leave the reactors, using the experimental RTDs, shown in Fig. 8, and using the calculated values of $N$ for the laboratory-scale CFB in a TIS with gamma extension model ($N = 1.08$ and $N = 1.51$ for the fuel and air reactors respectively). The analytical solution when the two reactors are well-mixed is also shown.](image)

![Fig. 10. Mean rate of reaction of particles in the fuel and air reactors, using the experimental RTDs, shown in Fig. 8, and using the calculated values of $N$ for the laboratory-scale CFB in a TIS with gamma extension model ($N = 1.08$ and $N = 1.51$ for the fuel and air reactors respectively). The analytical solution when the two reactors are well-mixed is also shown. The rate values are relative to the well-mixed value when $\theta = 1$.](image)

![Fig. 11. Mean conversions of particles as they leave the reactors as the RTD in the air reactor is varied. The results using the calculated values of $N$ for the laboratory-scale CFB are also shown.](image)
expected, the results from the simulation using the values of $N$ determined for the laboratory-scale CFB lie between the well-mixed result and that when $N = 1$ in the fuel reactor and $N = 2$ in the air reactor.

4. Discussion

CLC is likely to be operated in an interconnected fluidised bed arrangement [36]. Figs. 3 and 11 show that the mean conversion of particles as they leave the reactors is sensitive to different RTDs in the air and fuel reactors when $\theta > 0.1$, i.e. when the mean residence time of particles is less than ten times the characteristic time taken for a particle to react completely. When operated in this regime, an increase in the number of CSTRs, $N$, corresponding to a decrease in the degree of mixing of the particles, was found to increase $\Delta X = X_{\text{fuel}} - X_{\text{air}}$. The impact is greatest around $\theta = 1$. This is the region where CLC is likely to be operated, since it gives the optimal balance between a low circulation rate and low inventories of solids, as seen in Fig. 7.

Increasing the size of particles can lead to a reduction in mixing [42,43]. Of course, the RTDs of solids could be changed dramatically by altering the design or the operation of the reactor. In the bubbling regime, bubbles lead to good mixing of the solids and beds are generally well-mixed with respect to solids [22]. In terms of operation, increasing the superficial gas velocity or decreasing the solid circulation rate, leads to better mixing in bubbling beds [21,27]. In the fast fluidisation regime, an increase in the superficial gas velocity or a decrease in the solid circulation rate decreases the mean residence time of solids, decreases the variance and increases the coefficient of variation [40]. A change in the geometry of the bed, e.g. by the addition of baffles, by modification of the aspect ratio, by adding stages, or by modifying the exit has been found to alter the mixing behaviour [21,23,41]. Increasing the size of particles can lead to a reduction in mixing [42,43]. Of course, the RTDs of solids could be changed dramatically by switching to a different type of reactor e.g. from a fluidised bed to a moving bed [44].

The mean and standard deviations of experimental RTDs from a laboratory-scale CFB gave values of $N$ close to 1, as seen in Table 1. Fig. 9 and Fig. 10 show that modelling experimental RTDs using a TIS with gamma extension model is an excellent approximation. In fact Fig. 11 shows that the difference between the mean conversion of particles as they leave the reactors when assuming that the reactors are well-mixed (the analytical solution) and when the appropriate values of $N (N = 1.08$ in the fuel reactor and $N = 5.15$ in the air reactor) were used was small. The difference between using the later and using values of $N = 1$ and $N = 2$ for the fuel and air reactors respectively was also small. The same trend was seen for the mean rates of reaction in the beds, shown in Figs. 12 and 13.
generating accurate models at the reactor scale. As $N$ increases, the sensitivity of the coupled system decreases, so for $N > 5$, knowing the value to the nearest 5 or 10 tanks is sufficient. These criteria are valid whether $N$ is the same or different in the two reactors.

5. Conclusions

The sensitivity of CLC to different RTDs of solids in the air and fuel reactors has been investigated. It was found that when the mean residence time of particles is less than ten times the characteristic time taken for a particle to react completely, CLC is sensitive to different RTDs. A decrease in the extent of mixing leads to a greater mean conversion by the time the particles leave the reactors, meaning that more oxygen is transferred each time a particle is cycled. It also leads to greater mean rates of reaction in the beds, allowing the inventory and circulation rate of solids to be lowered for the same combustion performance. This is valuable for design since it could significantly reduce the capital and operating costs of a CLC process. It was found that, for the case of a laboratory-scale CFB, described in this paper, it is appropriate to assume that both reactors are well-mixed with respect to solids. Generally in design and modelling of the CLC process it is important to take account of the residence time distribution of solids. If a tanks-in-series approach is used, for small values of $N$, knowing $N$ to the nearest integer is likely to be sufficient, while for higher values, to the nearest 5 or 10 tanks is sufficient.

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Fig. 14. Schematic diagram of the experimental CFB. The shaded regions indicate the volumes relevant for measurement of the RTDs using a single tracer particle.
References


[11] Zhang Y, Chao Z, Jakobsen HA. Modelling and simulation of chemical looping combustion through an Industrial CASE studentship. The authors are grateful to Dr. Thomas Leadbeater, Dr. Andrew Ingram and Prof. David Parker at the University of Birmingham for their help with PEPT measurements.

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Appendix A. Description of laboratory-scale circulating fluidised bed

Fig. 14 shows a schematic diagram of the experimental CFB, which was made of stainless steel (Alloy 310) and consisted of two fluidised bed reactors connected through two identical loop seals. The fuel reactor (FR) was a bubbling fluidised bed with an operating bed height of ~100 mm and an i.d. of 40 mm. The solids were transported from the FR to the air reactor (AR) via the lower standpipe (SP2) and the lower loop seal (LS2). The loop seals consisted of two chambers, which could be aerated independently. They each had a cross-sectional area of 20 mm × 20 mm and a height of 80 mm. The AR was a bubbling fluidised bed with an operating bed height of ~120 mm and an i.d. of 27 mm. The outlet of the AR tapered to a tube with a length ~1.6 m and an i.d. of 10 mm, acting as a riser to transport the solids upwards. To assist with the transport of particles up the riser, secondary air could be injected at the top of the bubbling fluidised bed of the AR. The solids were recovered downstream of the riser by a cyclone and transported via the upper standpipe (SP1) to the upper loop seal (LS1). Particles from LS1 entered the FR via tubing of i.d. 10 mm. This tubing was immersed in the bed of the FR, with the exit 15 mm above the distributor. The standpipes were operated in packed bed flow.

The pressure drop across various sections of the CFB was monitored continuously (at a frequency of 10 Hz) using pressure transducers (First Sensor, HDI) to ensure the system operated stably. Mass flow controllers (Brooks, 5850S) were used to control the flow rate of air to the LSs. Rotameters (MPB Industries) were used to control the flow rates of air to the AR (primary and secondary air inlet) and to the FR.

The circulation rate of solids, $\dot{m}_s$, was measured in the riser of the CFB, using a method developed and validated for this system. This is described in detail elsewhere [35]. In brief, pressure signals associated with the passage of solids in the riser were cross-correlated to estimate their time-averaged velocity, $U_p$. At the same time, the time-averaged voidage, $\epsilon_{\text{riser}}$, was measured in the riser. This enabled the value of $\dot{m}_s$ to be computed using $\dot{m}_s = A_{\text{riser}} \times \rho_p \times (1 - \epsilon_{\text{riser}}) \times U_p$, where $A_{\text{riser}}$ is the cross-sectional area of the riser and $\rho_p$ is the particle density.


