

# Resonant-light diffusion in a dense disordered atomic layer

R. Saint-Jalm<sup>1</sup>, M. Aidelsburger<sup>1,†</sup>, J.L. Ville<sup>1</sup>, L. Corman<sup>1,‡</sup>, Z. Hadzibabic<sup>2</sup>,  
D. Delande<sup>1</sup>, S. Nascimbene<sup>1</sup>, N. Cherroret<sup>1</sup>, J. Dalibard<sup>1</sup>, and J. Beugnon<sup>1\*</sup>

<sup>1</sup>Laboratoire Kastler Brossel, Collège de France, CNRS, ENS-PSL University,  
Sorbonne Université, 11 Place Marcelin Berthelot, 75005 Paris, France and

<sup>2</sup>Cavendish Laboratory, University of Cambridge, J.J. Thomson Avenue, Cambridge CB3 0HE, United Kingdom

(Dated: May 18, 2018)

Light scattering in dense media is a fundamental problem of many-body physics, which is also relevant for the development of optical devices. In this work we investigate experimentally light propagation in a dense sample of randomly positioned resonant scatterers confined in a layer of sub-wavelength thickness. We locally illuminate the atomic cloud and monitor spatially-resolved fluorescence away from the excitation region. We show that light spreading is well described by a diffusion process, involving many scattering events in the dense regime. For light detuned from resonance we find evidence that the atomic layer behaves as a graded-index planar waveguide. These features are reproduced by a simple geometrical model and numerical simulations of coupled dipoles.

Multiple-scattering in disordered materials is currently the focus of intense investigations in many different contexts like electron transport in solids [1], sound wave propagation [2], matter waves in optical potentials [3] and light propagation in dielectric materials [4]. Multiple light scattering is of paramount importance to understand light transport, for instance, in biological tissues, planetary atmospheres or interstellar clouds [5]. In addition, the development of custom photonic materials allows one to engineer disordered materials in a controlled way and opens new applications in random lasing [6] or in the development of solar cells [7].

Cold atomic gases offer a unique platform to investigate light scattering. Due to the simple atomic level structure, all photons incident on the gas are scattered without absorption. Cooling techniques can bring the atoms to a temperature where their residual motion is so small that Doppler broadening is negligible. Additionally, the gas dimensionality can be changed rather easily by shaping the trapping potential. Finally, the tunability of the scattering cross section and the atomic density allows one to explore light scattering from the dilute to the dense regime.

In the multiple-scattering regime, light is scattered several times before exiting the material in random directions. In sufficiently dilute atomic clouds, this process is known to be well captured by a random-walk type, diffusive model [1]. This regime has been explored in several experiments, achieving for instance the observation of coherent backscattering [8, 9], subradiant and superradiant modes [10–12], cooperative radiation pressure force [13] or collective light scattering [14, 15]. At higher densities  $\rho$  where the product of the light wave number  $k$  and the inter-atomic spacing  $\rho^{-1/3}$  becomes of the order of unity, the situation is still poorly understood. Indeed, scatterers are no longer independent of each other and significant induced dipole-dipole interactions occur [16–20]. These

interactions are responsible for “cooperative” effects such as broadening and shift of the resonance line [21–26].

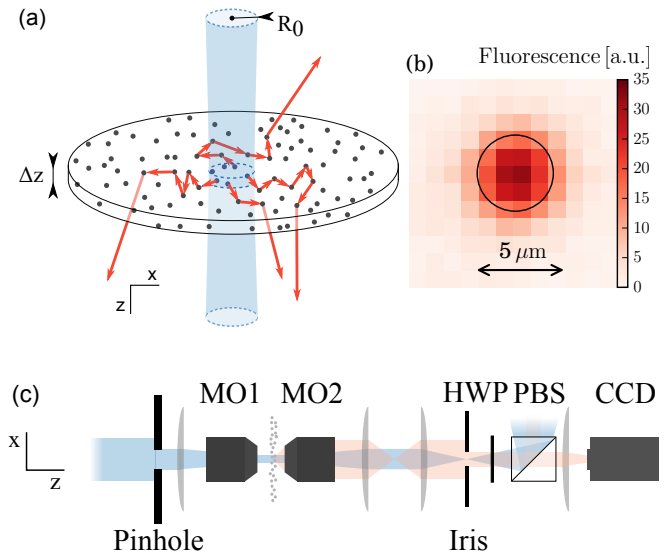


FIG. 1. Experimental setup. A layer of atoms is illuminated at its center with a resonant light beam of radius  $R_0$ . Photons initially emitted in the excitation region can be scattered several times in the atomic layer before exiting the system and being collected and imaged. (b) Typical fluorescence image at resonance and maximum density. The black circle, of diameter of  $2R_0 = 5 \mu\text{m}$ , delineates the excitation region. Intensity is not uniform inside the excitation region partially because of finite optical resolution but also and more importantly, because of the light diffusion process itself, as described in the text. (c) Schematics of the imaging system. A pinhole is imaged on the atomic cloud thanks to a microscope objective (MO1). The atomic fluorescence is imaged on a camera (CCD) thanks to a second and identical objective (MO2) and a set of lenses. Fluorescence is spatially filtered thanks to an iris and the detected polarization is chosen by adjusting a combination of a half-wave plate (HWP) and a polarization beam splitter (PBS).

\* beugnon@lkb.ens.fr cherroret@lkb.upmc.fr; <sup>†</sup>Present address: Fakultät für Physik, Ludwig-Maximilians-Universität München, Schellingstr. 4, 80799 Munich, Germany; <sup>‡</sup>Present address: Institute for Quantum Electronics, ETH Zurich, 8093 Zurich, Switzerland

Here, we explore the phenomenon of multiple-scattering of light in a dense and large cloud of atoms. In our ultracold sample the motion of the atoms is negligible on the timescale

of the experiment, so they act as a gas of fixed, randomly distributed point scatterers. Atoms are confined in a layer geometry in the focal plane of a high resolution imaging system, which allows us to inject light in a region with sharp boundaries and monitor its spreading away from this region (see Fig. 1a). We observed that the fluorescence intensity, which measures the local photon escape rate, decays exponentially with the distance from the excitation zone. We show that this behavior is compatible with a two-dimensional (2D) diffusive model. For resonant light, we measured the decay length of the fluorescence signal as a function of the atomic density, all the way from the dilute to the dense regime. The decay length coincides with the escape radius of the photons, *i.e.* the average distance they travel before they escape the sample. It decreases when increasing density, and then saturates in the regime of high density where photons undergo a few tens of scattering events before leaving the cloud. For detuned light and in the dense regime, the photon escape rate is significantly modified, in a way that suggests a light-guiding mechanism reminiscent of a graded-index planar waveguide. We also observed these phenomena in numerical simulations based on a model of coupled dipoles, and explained them in a semi-quantitative way by an analytical model of light guiding in an open, disordered 2D slab.

We use a dense layer of  $^{87}\text{Rb}$  atoms as previously described in Refs. [26, 27]. In the  $xy$  plane, we produce a uniform disk-shaped atomic layer of radius  $R = 20\ \mu\text{m}$  with a controllable surface density up to  $\rho_{2\text{D}} = 135(15)\ \mu\text{m}^{-2}$  and a temperature  $T_0 = 270(10)\ \text{nK}$ . Atoms are strongly confined along the vertical  $z$  direction with an approximately Gaussian density distribution of r.m.s. thickness  $\Delta z \approx 0.3\ \mu\text{m} < \lambda_0$ , with  $\lambda_0 = 2\pi/k = 0.78\ \mu\text{m}$  the resonant wavelength for the  $|F = 2\rangle$  to  $|F' = 3\rangle$  D2 transition of rubidium atoms. This corresponds to a maximum density at the center of the Gaussian profile of  $\rho_{3\text{D}}k^{-3} = 0.35(5)$  where  $\rho_{3\text{D}} = \rho_{2\text{D}}/(\sqrt{2\pi}\Delta z)$ .

We tune this density by varying the number of atoms in the  $|F = 2, m_F = -2\rangle$  hyperfine ground state, which is sensitive to our light probe. The population in this state is controlled thanks to partial transfer from the  $|F = 1, m_F = -1\rangle$  state in which the atoms are initially spin-polarized. As discussed in Ref. [26], dipole-dipole interactions play a dominant role at the densities achieved in our setup. Because of these interactions, the thickness of the cloud could increase, depending on its density, during the light excitation. We estimate that the effective cloud thickness, in the illuminated region, could reach at the end of the excitation the maximum value of  $0.4\ \mu\text{m}$ .

The atomic cloud is locally excited by light at a wavelength  $\lambda_0$ , propagating perpendicular to the atomic plane along the  $z$  axis, as illustrated in Fig. 1a, and linearly polarized along  $x$ . In the illuminated region, the intensity of the beam is on the order of  $7 I_{\text{sat}}$ , where  $I_{\text{sat}} = 1.6\ \text{mW cm}^{-2}$  is the saturation intensity for this transition (with a linewidth  $\Gamma = 2\pi \times 6.0\ \text{MHz}$ ) [28]. The light beam profile on the atomic cloud is given by the image of a pinhole whose diameter on the atomic cloud is  $2R_0 = 5\ \mu\text{m}$ . The excitation duration is  $\tau = 10\ \mu\text{s}$ . The atomic fluorescence is collected, spatially filtered and imaged on a CCD camera, as shown in Fig. 1c. We detect only photons with a linear polarization perpendicular to the excitation

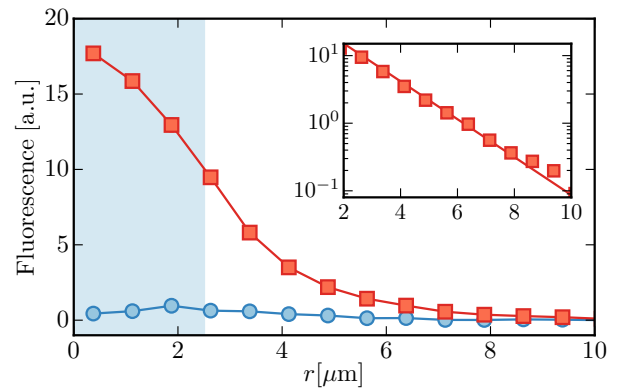


FIG. 2. Fluorescence decay. Binned and azimuthally averaged profile for the measured atomic fluorescence (squares). Circles show the small background signal observed without atoms. The shaded area represents the excitation region. Statistical errors bars due to photon counting are smaller than the size of the points. The solid lines are broken lines linking the points. The inset shows the same data outside the excitation region in a semilog plot to emphasize the exponential decay of the fluorescence signal. We attribute the deviation of the two last points from the exponential fit to the contribution from stray light. Data are averaged over 100 measurements.

polarization and block the residual transmitted light in the spatial mode of the incident beam. The optical resolution of our system ( $\sim 1\ \mu\text{m}$ ) is characterized in [29]. Atoms outside the illuminated region are only excited by scattered light and feel a much lower intensity than in the illuminated region. Taking into account our collection and detection efficiencies, assuming that the scatterers are independent and that polarization is randomized for photons emitted from outside the excitation region, we obtain a rough estimate for the intensity seen by atoms at  $1\ \mu\text{m}$  from the edge of the illuminated region of approximately  $0.1 I_{\text{sat}}$ . It is important to operate in this low saturation regime to enable comparison with the simulations described below.

We show in Fig. 1b a typical measurement of the atomic fluorescence signal integrated over the full duration of the excitation. The circle indicates the illuminated region. Photons are detected up to several micrometers away from this region. We show in Fig. 2 a binned and azimuthally averaged profile of the fluorescence image. There is a large ratio between the atomic signal and residual stray light over the explored experimental range. Outside the illuminated region we observe an exponential decay with distance of the atomic fluorescence over almost two decades (see inset in Fig. 2). The escape radii investigated in this work typically range from 1 to  $2\ \mu\text{m}$ .

We first focus on the experimental results for a resonant excitation. We fit the experimental fluorescence signal for various densities by  $Ae^{-r/R_e}$  and obtain the escape radius  $R_e$  as a function of density (see Fig. 3a). The escape radius decreases for increasing densities and reaches an approximately constant value for  $\rho_{3\text{D}}k^{-3} > 0.1$ . The measurements in the low

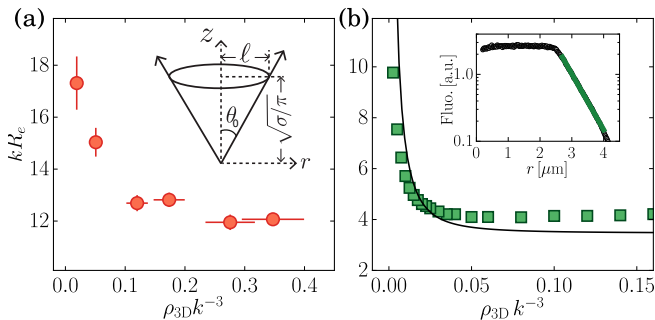


FIG. 3. (a) Measured escape radius  $R_e$  for different densities at resonance ( $\Delta = 0$ ). Vertical error bars correspond to the standard deviation of the results of exponential fits to the data obtained with a bootstrap approach [30]. Each data set is obtained from the average of 100 measurements. Horizontal error bars represent the statistical uncertainty on the atom number. The inset shows the relevant parameters of the simple model described in the main text. (b) Escape radius  $R_e$  obtained from the analytical result of Eq. (4) (solid curve) and numerical simulations of a model of classical coupled dipoles (squares) as a function of density. Statistical error bars on  $R_e$  obtained from the fitting procedure of the coupled dipole simulations are smaller than the size of the points. The inset shows the fluorescence signal computed with coupled dipole simulations for  $\rho_{3D}k^{-3} = 0.12$  and averaged over  $> 1000$  atomic distributions. The solid line is the exponential fit outside the illuminated region.

density regime (lower values of  $\rho_{3D}k^{-3}$ ) correspond to a “single scattering event” regime where a photon typically leaves the sample after the first scattering event outside the illuminated region. In this case the escape radius is on the order of the scattering mean free path  $\ell = 1/(\rho_{3D}\sigma)$ , where  $\sigma$  is the light cross section and we expect  $R_e \sim \ell$ , in agreement with the observed decrease of  $R_e$  with density.

In the opposite regime of large densities, photons are scattered several times before leaving the sample and we observe a saturation of the escape radius. It remains around  $kR_e \approx 12$  while varying the density by a factor of about 3. We checked that this saturation is not due to the finite resolution of our imaging system which allows us to measure spatial structures with a size below  $1 \mu\text{m}$  ( $kR_e \lesssim 8$ ). In this regime the system can be described by a diffusion model of light transport. In the steady-state regime, the light energy density  $I(\mathbf{r})$  at a point  $\mathbf{r}$  in the sample obeys a diffusion equation with losses:

$$-D_0 \nabla^2 I(\mathbf{r}) = -\gamma I(\mathbf{r}) + S(\mathbf{r}), \quad (1)$$

where  $D_0$  is the diffusion constant,  $\gamma$  the escape rate of photons and  $S(\mathbf{r})$  the source term describing the laser excitation. We consider the situation where the source term is  $S(\mathbf{r}) = S_0$  for  $r < R_0$  and 0 otherwise. The solution of this equation in two dimensions is given by

$$I(\mathbf{r}) = \frac{S_0}{2\pi D_0} \iint_{|\mathbf{r}'| < R_0} K_0\left(\frac{|\mathbf{r} - \mathbf{r}'|}{R_e}\right) d^2 r' \underset{r \gg R_0 + R_e}{\propto} \frac{e^{-r/R_e}}{\sqrt{r}}, \quad (2)$$

where  $K_0$  is the modified Bessel function of the second kind of order zero and  $R_e = \sqrt{D_0/\gamma}$ . Outside the illuminated region,

at large  $r$ , the function  $I(r)$  decays almost exponentially [31] in agreement with our measurements. These results allow us to relate the measured photon escape radius  $R_e$  to the diffusion constant  $D_0$  and to the escape rate  $\gamma$  that we cannot measure individually in a direct way. In this diffusive regime and for large  $r$ , the escape radius  $R_e$  can also be related to the microscopic parameters describing the propagation of a photon in a random walk picture

$$R_e \sim \ell / \sqrt{p}, \quad (3)$$

where  $p$  is the probability of escaping the cloud after a scattering event and  $\ell$  the (already defined) scattering mean free path.

We have developed a simple geometrical model to estimate the escape probability  $p$  and to explain the main features of the curve in Fig. 3a. Consider an atom in a 2D gas emitting a photon as being placed at the center of a vertical cylinder of radius  $\ell$ , corresponding to the typical distance to the next scatterer. The photon will escape the cloud if its emission angle  $\theta_0$  is small enough so that it would meet the next scatterer at a height larger than  $\sqrt{\sigma/\pi}$ . Emitted photons that escape the medium are then effectively contained within a cone of half-angle  $\theta_0$  (see inset of Fig. 3a). This gives a probability  $p \sim 2 \times 2\pi(1 - \cos \theta_0)/(4\pi)$  with  $\tan \theta_0 = \ell / \sqrt{\sigma/\pi}$ , and in turn:

$$kR_e = \frac{k\ell}{\sqrt{1 - (1 + \ell^2\pi/\sigma)^{-1/2}}}. \quad (4)$$

We display Eq. (4) computed for the resonant scattering cross section  $3\lambda_0^2/(2\pi)$  in Fig. 3b (solid line). At large densities,  $p \sim \ell^2\pi/(2\sigma)$  so that  $R_e$  becomes independent of the density and much larger than the mean free path. This saturation of  $R_e$  with increasing density thus stems from the compensation of two antagonistic effects: (i) the decrease of  $\ell$ , which tends to make the escape radius smaller and (ii) the decrease of  $p$ . The extension of Eq. (3) to low densities (large  $\ell$ ) is consistent with  $R_e \propto \ell$  and this simple model thus reproduces roughly the behavior of the ensemble of the experimental points.

Using the random walk picture and this estimate of  $p$ , we find that the typical number of scattering events before a photon leaves the sample is  $N_{\text{scatt}} = 1/p = 2\sigma/(\pi\ell^2)$ . Considering an atomic density of  $\rho_{3D}k^{-3} = 0.07$ , in the “plateau” of Fig. 3b but not too large so that  $\ell$  could still be interpreted with the classical picture of a mean free path, we get a typical value of about 20 scattering events. This value justifies the diffusion model and confirms that we investigate experimentally a steady-state situation (the total duration of a photon random walk,  $\approx N_{\text{scatt}}\Gamma^{-1}$ , is much shorter than the duration  $\tau$  of the illumination pulse).

As shown in Fig. 3b, the variation of escape radius with density is also reproduced by numerical simulations based on the method of coupled dipoles. As described in Ref. [32], we model our atomic system by a random ensemble of randomly positioned classical coupled dipoles (with transition  $J = 0$  to  $J = 1$ ) in a layer geometry with the same thickness as in the experiment. We compute the exact radiated field from these dipoles for a given excitation field taking into account

213 simultaneously all effects related to dipole-dipole interactions  
 214 and interferences. Fluorescence signals are obtained from the  
 215 modulus square of each dipole and escape radii from an expo-  
 216 nential fit to the fluorescence signal in the range  $r_1 = 2.7 \mu\text{m}$   
 217 to  $r_2 = 4 \mu\text{m}$ , where  $r$  is the distance from the center. For each  
 218 density we adapt the atom number in the simulations (from  
 219 100 up to 4000) and the number of repetitions over which the  
 220 result of the simulations are averaged (from 20 to more than  
 221  $10^5$ ).

222 The two models that we have developed are in good agree-  
 223 ment with each other. But although these predictions quali-  
 224 tatively reproduce the measurements in Fig. 3a, note the dif-  
 225 ference by a factor  $\approx 3$  between the scales of the two graphs.  
 226 Possible reasons for this difference are discussed below.

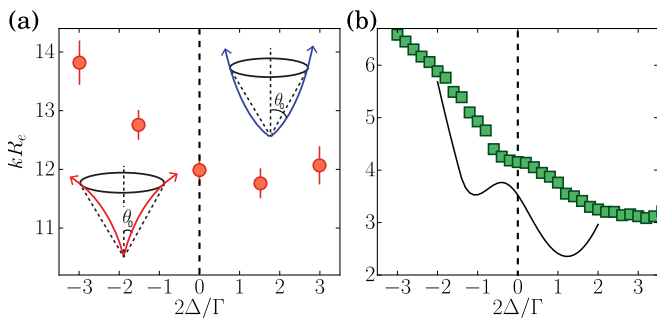


FIG. 4. Escape radius versus detuning. (a) Experimental results obtained for a dense cloud with  $\rho_{3D}k^{-3} \approx 0.35$ . The insets show the bending of the trajectories which depends on the sign of the detuning. The dashed lines in the insets correspond to the maximal emission angle a photon leaving the sample could have without considering the bending effect. Taking into account the bending effect, this maximal angle is smaller for negative detuning and larger for positive detunings. Each point is the average result of 100 measurements. (b) Escape radius computed from a numerical model of coupled dipoles (squares), escape radius  $R_e = \ell / \sqrt{1 - \cos \theta_0}$  obtained by solving Eq. (5) for  $\theta_0$  (solid line). All theory curves are computed for the largest density we are able to handle  $\rho_{3D}k^{-3} = 0.1$ . Statistical error bars obtained from the fitting procedure for the coupled dipole simulations are smaller than the size of the points.

227 An interesting feature of atomic systems is the possibility  
 228 to change dramatically the response of the system by vary-  
 229 ing the detuning  $\Delta$  of the excitation light with respect to the  
 230 resonance. We report in Fig. 4a the influence of the detuning  
 231 on the experimental escape radius  $R_e$  for the cloud of highest  
 232 density. We observe a clear asymmetry around  $\Delta = 0$ : the  
 233 escape radius is larger for negative than for positive detun-  
 234 ings, which indicates that photons are escaping more easily  
 235 the sample when  $\Delta > 0$ . Clearly, the results of Fig. 4a cannot  
 236 be explained by the dependence of Eq. (4) on  $\Delta$ , which origi-  
 237 nates only from the photon scattering cross section by a single  
 238 atom and is thus symmetric with respect to  $\Delta = 0$ .

239 We attribute the asymmetry mainly to a refractive-index  
 240 gradient effect and we developed a simple model to describe  
 241 this effect. We approximate the atomic slab by a continuous  
 242 medium with a spatially-varying index of refraction  $n(z)$  along  
 243 the vertical direction and use the low-density expression for  
 244 this index:  $n(z) = 1 - [6\pi\rho_{3D}(z)\Delta/\Gamma]/[k^3(1 + 4\Delta^2/\Gamma^2)]$ . It is

245 thus either larger than one below the resonance ( $\Delta < 0$ ), or  
 246 lower than one above the resonance ( $\Delta > 0$ ). In our system,  
 247 the density distribution  $\rho_{3D}(z)$  has an approximately Gaussian  
 248 shape with a maximum at  $z = 0$  leading to a gradient of the  
 249 index of refraction. For negative detuning,  $n(z)$  decreases with  
 250  $|z|$  from the center of the cloud. This gives rise to a phe-  
 251 nomenon of light guiding close to the one encountered in op-  
 252 tical waveguides, explaining qualitatively why the escape ra-  
 253 dius gets larger. For  $\Delta > 0$ , the opposite effect is expected,  
 254 with a decrease of the escape radius.

255 More quantitatively, the effect of the refractive-index gra-  
 256 dient on  $R_e$  can be estimated by modifying the geometrical  
 257 picture of the inset in Fig. 3a to account for the *bending* of  
 258 photon trajectories that escape the layer, as illustrated in the  
 259 insets of Fig. 4a for  $\Delta > 0$  and  $\Delta < 0$ . For negative detunings,  
 260 this bending leads to a decrease of the maximum value of the  
 261 emission angle  $\theta_0$  for which a photon leaves the cloud. Simi-  
 262 larly, it leads to an increase of  $\theta_0$  for positive detunings. The  
 263 principle of the calculation is the following. We compute the  
 264 equation for the trajectory  $z(r)$  of a photon emitted in  $z = 0$ ,  
 265  $r = 0$  and determine the emission angle  $\theta_0$  that fulfills the  
 266 “escape condition”

$$z(\ell) = \sqrt{\sigma/\pi}. \quad (5)$$

267 where  $\sigma = 3\lambda_0^2/(2\pi)/(1 + 4\Delta^2/\Gamma^2)$ . To find  $z(r)$ , we use the  
 268 low-density expression of  $n(z)$  given above, and approximate  
 269 the density profile  $\rho_{3D}(z)$  of the atomic layer by an inverted  
 270 parabola. Details of the calculation and complementary data  
 271 for other densities are available in [29]. The escape radius ob-  
 272 tained from this model is displayed in Fig. 4b as a function of  
 273  $\Delta$  and shows a significant asymmetric behavior with detuning.

274 A similar asymmetry is also visible in our numerical simu-  
 275 lations of coupled dipoles (see Fig. 4b). Note that differences  
 276 show up between the numerical simulations and our geometri-  
 277 cal model. In particular, the simulations display a weaker  
 278 variation with  $\Delta$  than the one predicted by Eq. (5). This effect  
 279 could be attributed to light-induced dipole-dipole interactions  
 280 between atoms. These interactions are known to give rise to  
 281 a broadening and a blue shift of the line [26], present in the  
 282 simulations but not taken into account in Eq. (5). More gener-  
 283 ally, cooperative effects could be taken into account by modi-  
 284 fying also the mean free path and the cross section, which are  
 285 fundamental parameters of our model. Calculation of these  
 286 parameters in the dense regime is however a difficult task that  
 287 we leave for future work.

288 Since the measured escape radii are on the order of the op-  
 289 tical wavelength, their measurement is rather challenging. We  
 290 discuss two possible experimental limitations for this mea-  
 291 surement. First, the finite resolution of the imaging system  
 292 leads to an overestimate of the escape radius, but our setup  
 293 benefits from a good spatial resolution, and we estimate that  
 294 this correction should be at most on the order of 10%. Sec-  
 295 ond, light-induced forces caused by dipole-dipole interactions  
 296 are strong when operating in the dense regime. We have thus  
 297 chosen the duration of the excitation short enough to limit the  
 298 atomic motion, while being long enough to probe the steady-  
 299 state regime. With these parameters dipole-dipole interactions  
 300 still lead to a small increase of the cloud size along the vertical



axis. This increase of the cloud thickness (only in the illuminated region where the scattering rate is large) could favor the propagation of photons to a larger distance. For a pulse duration twice as long [33] we observed an increase of the escape radius  $R_e$  by about 20%.

Both the coupled dipole simulations and the geometrical model predict a variation of  $R_e$  with density and detuning qualitatively similar to the experimental results, but with a factor  $\sim 3$  difference in the absolute value for  $R_e$ . A possible explanation for this discrepancy is the complex level structure of the rubidium atom. For instance, the averaging of the Clebsch-Gordan coefficients over all possible  $\pi$  transitions relevant for our incident linearly polarized light should at least lead to a correction of the effective single-atom scattering cross section which is not taken into account in our expression of the mean free path  $\ell$  [34]. Taking into account this level structure on the determination of  $R_e$  requires complex simulations beyond the scope of this article [25]. An alternative approach would be to reproduce this study with atomic species like ytterbium and strontium which present well-isolated  $J = 0$  to  $J = 1$  transitions. One could also couple our method for producing thin slabs with the method to isolate an effective two-level system in a multilevel atom dis-

cussed in Refs [35–37] and based on the large Zeeman effect produced by an external magnetic field.

In summary, we have explored the diffusion of light in a dense and extended sample of fixed scatterers. Experiments with cold atomic systems are usually limited to lower densities. Still, the dense regime was explored in Refs. [23–25] but with a microscopic sample where light propagation cannot be investigated, and also in Ref. [21] but with a hot and thus Doppler-broadened cloud. Complementary studies on light transport in photonic planar waveguides have also been reported, for instance, in Ref. [38]. However, our system reveals a unique combination of multiple-scattering, high densities and guiding effects which can be tuned rather easily. Our experiment paves the way to a deeper understanding of the propagation of light in dense samples and possibly on the role of interference-induced (localization) effects in this geometry [39, 40]. Indeed, while the observation of photon localization is still elusive [39], presumably due to the vector nature of light detrimental to interference [40], the problem could be circumvented in a 2D system illuminated by a light field linearly polarized perpendicular to the disordered plane. Our atomic system could constitute a good candidate for that objective, using the escape radius – directly controlled by the diffusion coefficient – as a probe for localization [41].

- 
- [1] E. Akkermans and G. Montambaux, *Mesoscopic physics of electrons and photons* (Cambridge university press, 2007).
- [2] H. Hu, A. Strybulevych, J.H. Page, S.E. Skipetrov, and B.A. van Tiggelen, “Localization of ultrasound in a three-dimensional elastic network,” *Nat. Phys.* **4**, 945–948 (2008).
- [3] A. Aspect and M. Inguscio, “Anderson localization of ultracold atoms,” *Physics today* **62**, 30–35 (2009).
- [4] M.C.W. van Rossum and Th.M. Nieuwenhuizen, “Multiple scattering of classical waves: microscopy, mesoscopy, and diffusion,” *Rev. Mod. Phys.* **71**, 313–371 (1999).
- [5] H.C. Van de Hulst, *Multiple light scattering: tables, formulas, and applications* (Elsevier, 2012).
- [6] D.S. Wiersma, “The physics and applications of random lasers,” *Nat. Phys.* **4**, 359–367 (2008).
- [7] D.S. Wiersma, “Disordered photonics,” *Nat. Photon.* **7**, 188–196 (2013).
- [8] G. Labeyrie, F. de Tomasi, J.-C. Bernard, C. A. Müller, C. Miniatura, and R. Kaiser, “Coherent backscattering of light by cold atoms,” *Phys. Rev. Lett.* **83**, 5266–5269 (1999).
- [9] Y. Bidel, B. Klappauf, J. C. Bernard, D. Delande, G. Labeyrie, C. Miniatura, D. Wilkowski, and R. Kaiser, “Coherent light transport in a cold Strontium cloud,” *Phys. Rev. Lett.* **88**, 203902 (2002).
- [10] S.J. Roof, K.J. Kemp, M.D. Havey, and I.M. Sokolov, “Observation of single-photon superradiance and the cooperative Lamb shift in an extended sample of cold atoms,” *Phys. Rev. Lett.* **117**, 073003 (2016).
- [11] W. Guerin, M.O. Araújo, and R. Kaiser, “Subradiance in a large cloud of cold atoms,” *Phys. Rev. Lett.* **116**, 083601 (2016).
- [12] M.O. Araújo, I. Krešić, R. Kaiser, and W. Guerin, “Superradiance in a large and dilute cloud of cold atoms in the linear-optics regime,” *Phys. Rev. Lett.* **117**, 073002 (2016).
- [13] T. Bienaimé, S. Bux, E. Lucioni, P.W. Courteille, N. Piovella, and R. Kaiser, “Observation of a cooperative radiation force in the presence of disorder,” *Phys. Rev. Lett.* **104**, 183602 (2010).
- [14] S. Balik, A.L. Win, M.D. Havey, I.M. Sokolov, and D.V. Kupriyanov, “Near-resonance light scattering from a high-density ultracold atomic  $^{87}\text{Rb}$  gas,” *Phys. Rev. A* **87**, 053817 (2013).
- [15] S.L. Bromley, B. Zhu, M. Bishof, X. Zhang, T. Bothwell, J. Schachenmayer, T.L. Nicholson, R. Kaiser, S.F. Yelin, M.D. Lukin, A.M. Rey, and J. Ye, “Collective atomic scattering and motional effects in a dense coherent medium,” *Nat. Commun.* **7** (2016).
- [16] R.H. Lehmburg, “Radiation from an  $N$ -atom system. I. General formalism,” *Phys. Rev. A* **2**, 883–888 (1970).
- [17] R. Friedberg, S.R. Hartmann, and J.T. Manassah, “Frequency shifts in emission and absorption by resonant systems of two-level atoms,” *Phys. Rep.* **7**, 101–179 (1973).
- [18] M. Gross and S. Haroche, “Superradiance: An essay on the theory of collective spontaneous emission,” *Phys. Rep.* **93**, 301–396 (1982).
- [19] O. Morice, Y. Castin, and J. Dalibard, “Refractive index of a dilute Bose gas,” *Phys. Rev. A* **51**, 3896–3901 (1995).
- [20] N. Cherroret, D. Delande, and B.A. van Tiggelen, “Induced dipole-dipole interactions in light diffusion from point dipoles,” *Phys. Rev. A* **94**, 012702 (2016).
- [21] J. Keaveney, A. Sargsyan, U. Krohn, I. G. Hughes, D. Sarkisyan, and C. S. Adams, “Cooperative Lamb shift in an atomic vapor layer of nanometer thickness,” *Phys. Rev. Lett.* **108**, 173601 (2012).
- [22] J. Javanainen, J. Ruostekoski, Y. Li, and S.M. Yoo, “Shifts of a resonance line in a dense atomic sample,” *Phys. Rev. Lett.* **112**, 113603 (2014).
- [23] J. Pellegrino, R. Bourgain, S. Jennewein, Y. R. P. Sortais, A. Browaeys, S. D. Jenkins, and J. Ruostekoski, “Observa-

- tion of suppression of light scattering induced by dipole-dipole interactions in a cold-atom ensemble,” *Phys. Rev. Lett.* **113**, 133602 (2014).
- [24] S. Jennewein, M. Besbes, N. J. Schilder, S. D. Jenkins, C. Sauvan, J. Ruostekoski, J.-J. Greffet, Y. R. P. Sortais, and A. Browaeys, “Coherent scattering of near-resonant light by a dense microscopic cold atomic cloud,” *Phys. Rev. Lett.* **116**, 233601 (2016).
- [25] S.D. Jenkins, J. Ruostekoski, J. Javanainen, R. Bourgain, S. Jennewein, Y.R.P. Sortais, and A. Browaeys, “Optical resonance shifts in the fluorescence of thermal and cold atomic gases,” *Phys. Rev. Lett.* **116**, 183601 (2016).
- [26] L. Corman, J. L. Ville, R. Saint-Jalm, M. Aidelsburger, T. Bienaimé, S. Nascimbène, J. Dalibard, and J. Beugnon, “Transmission of near-resonant light through a dense slab of cold atoms,” *Phys. Rev. A* **96**, 053629 (2017).
- [27] J.L. Ville, T. Bienaimé, R. Saint-Jalm, L. Corman, M. Aidelsburger, L. Chomaz, K. Kleinlein, D. Perconte, S. Nascimbène, J. Dalibard, and J. Beugnon, “Loading and compression of a single two-dimensional Bose gas in an optical accordion,” *Phys. Rev. A* **95**, 013632 (2017).
- [28] The intensity we used is large enough to ensure that, even if our samples have large optical depths, the cloud is well-excited for all positions along the  $z$  direction.
- [29] “For details, see Supplemental Materials,”.
- [30] Bradley E., “Better bootstrap confidence intervals,” *J. Am. Stat. Assoc.* **82**, 171–185 (1987).
- [31] We neglect the  $\sqrt{r}$  dependence which has almost no influence on the shape of the signal in the range of distance we explore in this work.
- [32] L. Chomaz, L. Corman, T. Yefsah, R. Desbuquois, and J. Dalibard, “Absorption imaging of a quasi-two-dimensional gas: a multiple scattering analysis,” *New J. Phys.* **14**, 055001 (2012).
- [33] The amplitude of the signal becomes too low for shorter pulses.
- [34] An average with equal weights on all the transition gives a cross section decreased by a factor  $7/15$ , but it neglects any optical pumping effects during the excitation. The scattering cross section should also be modified to take into account the spectrum of the photons emitted by the illuminated region. Indeed, as the Rabi frequency of our excitation beam is on the order of  $\Gamma$ , we expect a modification of the fluorescence spectrum.
- [35] S. E. Skipetrov and I. M. Sokolov, “Magnetic-field-driven localization of light in a cold-atom gas,” *Phys. Rev. Lett.* **114**, 053902 (2015).
- [36] D.J. Whiting, E. Bimbard, J. Keaveney, M.A. Zentile, C.S. Adams, and I.G. Hughes, “Electromagnetically induced absorption in a nondegenerate three-level ladder system,” *Opt. Lett.* **40**, 4289–4292 (2015).
- [37] D.J. Whiting, J. Keaveney, C.S. Adams, and I.G. Hughes, “Direct measurement of excited-state dipole matrix elements using electromagnetically induced transparency in the hyperfine Paschen-Back regime,” *Phys. Rev. A* **93**, 043854 (2016).
- [38] F. Riboli, F. Uccheddu, G. Monaco, N. Caselli, F. Intonti, M. Gurioli, and S.E. Skipetrov, “Tailoring correlations of the local density of states in disordered photonic materials,” *Phys. Rev. Lett.* **119**, 043902 (2017).
- [39] S.E. Skipetrov and J.H. Page, “Red light for Anderson localization,” *New J. Phys.* **18**, 021001 (2016).
- [40] S. E. Skipetrov and I. M. Sokolov, “Absence of Anderson localization of light in a random ensemble of point scatterers,” *Phys. Rev. Lett.* **112**, 023905 (2014).
- [41] N. Cherroret and S. E. Skipetrov, “Microscopic derivation of self-consistent equations of Anderson localization in a disordered medium of finite size,” *Phys. Rev. E* **77**, 046608 (2008).

#### ACKNOWLEDGMENTS

This work is supported by DIM NanoK, ERC (Synergy UQUAM). This project has received funding from the European Union’s Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement N° 703926. We thank S. Gigan for fruitful discussions. N.C. thanks A. Browaeys for discussions on cooperative effects, and the Agence Nationale de la Recherche (Grant No. ANR-14-CE26-0032 LOVE) for financial support. Z.H. acknowledges support from EPSRC (Grant No. EP/N011759/1) and Sorbonne Université.