

1 **Arthropod segmentation**

2 Erik Clark^{1,2*}, Andrew D. Peel³, and Michael Akam²

3

4 ¹ Department of Systems Biology, Harvard Medical School

5 ² Department of Zoology, University of Cambridge

6 ³ School of Biology, Faculty of Biological Sciences, University of Leeds

7 * correspondence: erik_clark@hms.harvard.edu

8

9 **Summary**

10 There is now compelling evidence that many arthropods pattern their segments using a clock-and-
11 wavefront mechanism, analogous to that operating during vertebrate somitogenesis. In this review,
12 we discuss how the arthropod segmentation clock generates a repeating sequence of pair-rule gene
13 expression, and how this is converted into a segment-polarity pattern by “timing factor” wavefronts
14 associated with axial extension. We argue that the gene regulatory network that patterns segments
15 may be relatively conserved, although the timing of segmentation varies widely, and double-
16 segment periodicity appears to have evolved at least twice. Finally, we describe how the repeated
17 evolution of a simultaneous (*Drosophila*-like) mode of segmentation within holometabolan insects
18 can be explained by heterochronic shifts in timing factor expression plus extensive pre-patterning of
19 the pair-rule genes.

20

21 **Introduction**

22 Arthropods are an ecdysozoan phylum defined by their segmented bodies and jointed limbs. True
23 arthropods (euarthropods) comprise three living clades: Chelicerata (spiders, scorpions and mites),
24 Myriapoda (centipedes and millipedes), and Pancrustacea (crustaceans and insects). The closest
25 relatives of arthropods are onychophorans (velvet worms) and tardigrades (water bears); together
26 these phyla form the segmented superphylum Panarthropoda (**Fig. 1A**).

27 The great diversity of arthropod species is testament to the evolutionary potential of a segmented
28 body plan: a modular organisation of fundamentally similar units arrayed serially along the
29 anteroposterior (AP) axis (Hannibal and Patel, 2013). Arthropod segments, and their associated
30 appendages, have diversified remarkably through adaptation to specific functions, such as feeding,
31 locomotion, or reproduction. In addition, segment number can vary enormously, from fewer than
32 twenty in insects and malacostracan crustaceans, to over a hundred in certain centipedes and

33 millipedes, resulting in a wide spectrum of organismal forms (Brusca et al., 2016). With over a million
34 named species, arthropods have colonised and exploited almost every environment on Earth, thanks
35 in no small part to the evolution of segmentation.

36 Our understanding of how segments are patterned in arthropod embryos has traditionally been
37 heavily influenced by study of the fruit fly *Drosophila melanogaster*. Over the past two decades,
38 research into sequentially-segmenting species has complemented the well-established *Drosophila*
39 model, resulting in the discovery of an arthropod “segmentation clock”, and an outline of conserved
40 and divergent aspects of arthropod segment patterning networks. In the light of these findings,
41 recent studies have re-examined segmentation in *Drosophila*, uncovering new subtleties and
42 interpreting their evolutionary significance.

43 In the sections that follow, we provide a general overview of arthropod segmentation and review
44 our current understanding of three key issues: (1) the nature of the arthropod segmentation clock;
45 (2) how the “pair-rule” genes pattern segments; and (3) the evolution of *Drosophila*-style
46 simultaneous segmentation from a sequentially-segmenting ancestral state. We also reflect on the
47 origins of arthropod segmentation (**Box 1**) and the control of segment number (**Box 2**). As we have
48 chosen to focus on the time window when segments are actively being patterned, we do not discuss
49 earlier AP patterning processes, such as axis specification, or later ones, such as segment
50 morphogenesis.

51

52 **Overview of arthropod segmentation**

53 *Segments and parasegments*

54 In arthropods, morphological segmentation is built upon a more fundamental developmental unit,
55 the “parasegment” (Martinez-Arias and Lawrence, 1985). Parasegment boundaries are established
56 during embryogenesis by “segment-polarity” genes such as *engrailed* and *wingless*, which are
57 expressed in a series of persistent stripes along the AP axis. Interestingly, parasegments are offset
58 slightly from morphological segments: parasegment boundaries fall at the anterior edge of each
59 *engrailed* domain and line up with the middle of each appendage, while segment boundaries fall at
60 the posterior edge of each *engrailed* domain and lie in between the appendages (**Fig. 1B**). Analogous
61 to vertebrate “resegmentation” (each vertebra being formed from portions of two different somite
62 pairs), this developmental phase shift makes sense if the role of the parasegments is chiefly to
63 organise the nervous system and associated appendicular structures, while the role of morphological

64 segmentation is to protect these centres and form exoskeletal articulations between them (Deutsch,
65 2004).

66 Each segment-polarity gene is expressed at a particular position within a segmental unit, and the
67 overall arrangement is remarkably conserved across Panarthropoda (Damen, 2002; Janssen and
68 Budd, 2013). A central goal of segmentation research is to understand how upstream regulatory
69 processes establish this important pattern within the embryo.

70

71 *Sequential segmentation and the segment addition zone*

72 Most arthropods pattern their segments sequentially, from head to tail, coupling the segmentation
73 process to progressive axial extension (Sander, 1976). They usually specify some number of anterior
74 segments in the blastoderm, but the majority of the segments emerge rhythmically from a posterior
75 “segment addition zone” (SAZ) after the blastoderm to germband transition. The SAZ retracts
76 posteriorly as new segments are added to the trunk, generally shrinking in size, until the embryo
77 reaches full germband extension (**Fig. 1C**).

78 “SAZ” is now preferred over the traditional term “growth zone”, because it makes no assumption of
79 localised and continuous cell proliferation in the posterior of the embryo (Janssen et al., 2010). The
80 material for new segments is generally provided by a combination of cell division and convergent
81 extension, but – as in vertebrates – the relative contributions of these cell behaviours to axial
82 elongation vary widely across species (Auman et al., 2017; Benton, 2018; Benton et al., 2016; Mito et
83 al., 2011; Nakamoto et al., 2015; Steventon et al., 2016). Accordingly, while cell division may in some
84 species be coordinated with segment addition, segment patterning processes do not appear to be
85 mechanistically dependent on the cell cycle (Cepeda et al., 2017), aside from in special cases such as
86 malacostracan crustaceans. This group exhibits a highly derived mode of segmentation in which
87 patterning occurs through regimented asymmetrical divisions of rows of posterior cells (Scholtz,
88 1992).

89 While the shape, size, and proportions of the SAZ vary considerably across species, certain features
90 are conserved. Segment-polarity stripes emerge at the anterior of the SAZ, and Wnt is expressed at
91 its posterior (Williams and Nagy, 2017). Between these limits, we define the “anterior SAZ” as the
92 portion of the SAZ that contains segments in the process of being patterned, and the “posterior SAZ”
93 as the portion that contains cells not yet assigned to any particular prospective segment. These
94 functionally-defined regions correlate with the differential expression of key developmental
95 transcription factors; for example, Caudal (the arthropod homolog of the vertebrate Cdx proteins)

96 appears to be specifically associated with the posterior SAZ (Auman et al., 2017; Clark and Peel,
97 2018).

98 Importantly, SAZ identity is transient and dynamic for any given cell. With the generation of each
99 new segment, newly-patterned tissue “leaves” the anterior SAZ, which is simultaneously
100 “replenished” by cells from the posterior SAZ. (Whether cells flow anteriorly out of the SAZ or the
101 SAZ retracts posteriorly along the embryo depends on one’s choice of reference frame.) Thus, a cell
102 which starts out within the posterior SAZ, expressing one set of genes, will at some point end up
103 within the anterior SAZ, expressing a different set of genes, and finally within the segmented
104 germband, expressing yet another (**Fig. 1C**). This provides a mechanistic explanation for the tight
105 coupling between axial elongation and the segmentation process, because the changing expression
106 levels of SAZ-associated factors such as Caudal are likely to trigger coordinated expression changes
107 in segment patterning genes as the SAZ retracts (Clark and Peel, 2018; El-Sherif et al., 2014).

108

109 *Segment patterning by a clock-and-wavefront mechanism*

110 Arthropod segmentation is frequently compared to vertebrate somitogenesis (reviewed in Hubaud
111 and Pourquié, 2014; Oates et al., 2012). While segments and somites are not homologous
112 morphological structures, it is now becoming clear that both arthropods and vertebrates have
113 converged on a “clock-and-wavefront” strategy (Cooke and Zeeman, 1976) to pattern their AP axis.
114 Temporal periodicity is generated by an oscillator (the “clock”), and progressively translated into
115 spatial periodicity by a second signal (the “wavefront”), which travels along an axis and freezes (or
116 reads out) the phase of the clock.

117 In vertebrates, the clock consists of cycles of gene expression in the presomitic mesoderm (PSM),
118 while in arthropods it consists of cycles of gene expression in the posterior ectoderm. In both the
119 vertebrate anterior PSM and the arthropod anterior SAZ, the oscillations are slowed by the
120 retraction of posterior signals associated with axial extension, converting them into a series of
121 stripes. These stripes then pattern other genes, which determine the AP polarity of somites (in
122 vertebrates) or segments (in arthropods).

123 Curiously, the periodicity of the segmentation clock is not fixed across arthropods. Most groups
124 pattern a single new segment for each cycle of the clock (as do vertebrates), but some species
125 pattern two segments in each cycle, meaning that their clock has a double-segment (or “pair-rule”)
126 periodicity (Chipman et al., 2004; Sarrazin et al., 2012) .

127

128 *Other modes of segmentation*

129 The sequential mode of segmentation is widespread and almost certainly ancestral within
130 arthropods. However, across species, the timing of segmentation can vary dramatically relative to
131 other developmental events.

132 For example, arthropod embryos differ widely in the number of segments they pattern at the
133 blastoderm stage, versus afterwards during germband extension. In insects, this variation is roughly
134 correlated with a spectrum of “germ types” defined in the pre-molecular era (Davis and Patel, 2002;
135 Krause, 1939), but for simplicity and generality, we have chosen to eschew such terminology in this
136 review. Instead, we will refer to sequential segmentation (usually occurring in a germband, under
137 the control of a segmentation clock) versus simultaneous segmentation (usually occurring in a
138 blastoderm, downstream of non-periodic spatial cues). The mechanisms underlying simultaneous
139 segmentation are discussed in more detail below.

140 Outside of the insects, many arthropod groups undergo post-embryonic segmentation, i.e. delay the
141 development of a portion of the AP axis until after hatching. In crustaceans with naupliar larvae, for
142 example, only the head segments are patterned in the embryo, and trunk segments develop
143 sequentially from a SAZ-like region after the larva has begun feeding (Anderson, 1973). Other, less
144 extreme, examples are found within myriapods: these pattern the head and the first trunk segments
145 in the embryo, but may add one or more trunk segments after each moult (Blower, 1985).

146 Our focus here is on the segmentation of the trunk (i.e. the axial patterning of the gnathal, thoracic,
147 and abdominal segments), but note that there are other parts of the arthropod body that are
148 segmented by different mechanisms, such as the anterior head (Posnien et al., 2010) or the jointed
149 appendages (Angelini and Kaufman, 2005a). Within the trunk itself, the mechanisms we describe
150 specifically control ectodermal segmentation; mesodermal segmentation occurs later, apparently
151 directed by inductive signals from the segmented ectoderm (Azpiazu et al., 1996; Green and Akam,
152 2013; Hannibal et al., 2012). Finally, there is evidence that dorsal segmentation in millipedes is
153 decoupled from ventral segmentation, which later leads to segment fusions (Janssen, 2011; Janssen
154 et al., 2004).

155

156 *Segment patterning genes*

157 Most of the arthropod segmentation genes we know about were originally identified from a genetic
158 screen in *Drosophila* (Nüsslein-Volhard and Wieschaus, 1980). *Drosophila* represents an extreme
159 example of simultaneous segmentation, patterning all but its most terminal segments in the

160 blastoderm. It has taught us a lot about how segmentation genes regulate one another's expression
161 (Akam, 1987; Nasiadka et al., 2002), but studies in other arthropods were (and are) necessary to
162 reveal how these networks relate to more ancestral modes of segmentation (Peel et al., 2005).

163 In *Drosophila*, as in other arthropods, the segment-polarity genes are patterned by the "pair-rule"
164 genes, which code for various transcription factors. In *Drosophila*, the pair-rule genes are expressed
165 in stripes in the blastoderm, but in sequentially-segmenting species they are also expressed in the
166 SAZ (Patel et al., 1994). In general, the pair-rule genes that turn on earliest in *Drosophila* ("primary"
167 pair-rule genes) are expressed in the posterior SAZ in sequentially-segmenting species, and may
168 oscillate, while those that turn on later ("secondary" pair-rule genes) are expressed in the anterior
169 SAZ. The periodicity of pair-rule gene expression can be segmental or double-segmental depending
170 on the species (in *Drosophila* it is double-segmental, hence the term "pair-rule"), but the genes are
171 always referred to as the "pair-rule genes" regardless. There has been some confusion over the
172 years as to which *Drosophila* pair-rule genes should be classed as primary and which as secondary or
173 even tertiary. However, the most recent analysis (Schroeder et al., 2011), which classifies only *paired*
174 (*prd*) and *sloppy-paired* (*slp*) as secondary, and all of *hairy*, *even-skipped* (*eve*), *runt*, *odd-skipped*
175 (*odd*) and *fushi tarazu* (*ftz*) as primary, meshes well with the comparative evidence.

176 In *Drosophila*, the primary pair-rule genes are patterned by the "gap" genes, which code for another
177 set of transcription factors. In *Drosophila*, these genes are expressed in broad, partially-overlapping
178 domains along the length of the blastoderm, but in sequentially-segmenting species some portion of
179 this pattern is generated over time, in the SAZ (**Box 2**). Gap genes in sequentially-segmenting species
180 do not seem to be important for directing pair-rule gene expression. They do, however, appear to
181 play a relatively conserved role in patterning the Hox genes, which regulate segment identity
182 (Hughes and Kaufman, 2002a; Marques-Souza et al., 2008; Martin et al., 2016)

183

184 **BOX 1: The evolutionary origins of arthropod segmentation**

185 The major segmented phyla – arthropods, annelids, and chordates – are evolutionarily distant and
186 separated by many unsegmented groups. While losses of segmentation are possible in evolution
187 (e.g. from spoon worms and peanut worms within annelids), we are sceptical about the existence of
188 a segmented urbilaterian ancestor that could have given rise to all three phyla (Couso, 2009).
189 Instead, segmentation appears to have evolved repeatedly during animal evolution, involving
190 various developmental mechanisms (Graham et al 2014).

191 Some of the developmental commonalities between different segmented phyla may reflect
192 bilaterian homologies that predate segmentation itself, such as elongation of the body from a
193 posterior zone (Jacobs et al 2005, Martin and Kimelman 2009). Other similarities may reflect the
194 convergent adoption of generic patterning strategies, such as molecular oscillators (Richmond and
195 Oates 2012). Finally, certain similarities may reflect the parallel redeployment of ancient molecular
196 mechanisms (Chipman, 2010), and therefore require both homology and convergence to fully
197 explain. For example, segment boundary formation in some, but not all, annelids shows striking
198 similarities to parasegment boundary formation in arthropods (Dray et al., 2010; Prud'homme et al.,
199 2003; Seaver et al., 2001; Seaver and Kaneshige, 2006). Probably, this boundary specification
200 mechanism evolved before trunk segmentation, possibly in the context of patterning the head and
201 anterior nervous system (Vellutini and Hejzol, 2016).

202 The evolutionary success of segmented phyla emphasizes the adaptive value of diversified
203 metameric structures, but it does not explain why segmentation evolved in the first place. One long-
204 standing hypothesis stresses the advantages of a segmented body for generating coordinated waves
205 of muscular activity to drive locomotion (Clark, 1964). Given that most of the earliest arising
206 segmented lineages have many similar segments, this seems a likely explanation for the initial
207 origins of serial repetition along the body axis, which was likely the forerunner for metameric
208 segmentation. Under this scenario, repetition would be expected first in the nervous system and
209 body wall musculature. Interestingly, onychophorans have distinct mesodermal somites, and show
210 clear parasegmental boundaries in the limbs and nervous system (Eriksson et al., 2009), but show no
211 obvious segmentation of the body wall ectoderm.

212

213 **BOX 2: Regulation of segment number**

214 In arthropods, segment number is determined by the total number of pair-rule stripes (and the
215 periodicity with which they regulate segment-polarity genes). In simultaneously-segmenting insects
216 such as *Drosophila*, individual pair-rule stripes are positioned by gap factors at specific locations
217 along the AP axis, hardcoding segment number. In sequentially-segmenting species, segment
218 number instead depends on the temporal duration of segmentation, divided by the period of the
219 segmentation clock.

220 Gap genes appear to play some role in controlling the duration of segment addition (Cerny et al.,
221 2005; Nakao, 2016). Over time, gap genes are expressed sequentially within the SAZ, their turnover
222 driven by cross-regulatory interactions (Boos et al., 2018; Verd et al., 2018). This process, effectively

223 a developmental “timer”, shows intriguing similarities to the “neuroblast clock” (Isshiki et al., 2001;
224 Peel et al., 2005). It evidently exerts some control over the body plan, since perturbing *hunchback*
225 expression can both decrease (Liu and Kaufman, 2004a; Marques-Souza et al., 2008; Mito et al.,
226 2005) and increase (Boos et al., 2018; Nakao, 2016) segment number in sequentially-segmenting
227 insects. These phenotypes are not well understood, but might result from gap genes directly or
228 indirectly regulating cell behaviour within the SAZ. Such effects are unlikely to be mediated via the
229 Hox genes, since significant perturbations of Hox gene expression in insects and crustaceans have
230 not been found to affect segment number (Angelini et al., 2005; Martin et al., 2016; Stuart et al.,
231 1991).

232 Despite varying widely among arthropods, segment number is usually fixed within a species.
233 However, there are certain groups, such as geophilomorph centipedes, where naturally occurring
234 variation might provide clues as to how this number evolves (Kettle and Arthur, 2000; Vedel et al.,
235 2008; Vedel et al., 2010). Another interesting question is how species which undergo post-
236 embryonic segmentation coordinate segment patterning with the moult cycle. Ecdysone-related
237 genes play segmentation roles in some embryos (Erezyilmaz et al., 2009; Heffer et al., 2013),
238 suggesting these two processes might be deeply related.

239

240 **Nature of the arthropod segmentation clock**

241 *Oscillating gene expression in the SAZ*

242 Some segmentation genes exhibit extremely variable expression patterns in the posterior SAZs of
243 fixed embryos, suggesting that they continually turn on and off over time. In the beetle *Tribolium*,
244 split-embryo experiments have confirmed that this variability results from a temporally dynamic
245 “segmentation clock” within individuals rather than spatially variable expression between individuals
246 (Sarrazin et al., 2012). Expression dynamicity has also been demonstrated in *Tribolium* by comparing
247 the average patterns of finely-staged cohorts of embryos, visualising discrepancies between the
248 transcript and protein domains of a given gene, and gaining an understanding of cell dynamics within
249 the SAZ via live imaging (Benton, 2018; El-Sherif et al., 2012; Sarrazin et al., 2012). In other species,
250 gene expression dynamics within the SAZ have rarely been studied in detail. However, convincing
251 “pseudo time-series” assembled from carefully-staged *Strigamia* (centipede) and *Parasteatoda*
252 (spider) embryos imply that oscillatory dynamics are widespread (Brena and Akam, 2013; Schönauer
253 et al., 2016).

254 Candidate gene approaches in species including *Tribolium*, *Strigamia*, the millipede *Glomeris*, and a
255 second spider, *Cupiennius*, indicate that oscillating SAZ genes include the primary pair-rule genes
256 *hairy*, *eve*, *runt* and *odd* (Choe et al., 2006; Damen et al., 2005; Green and Akam, 2013; Janssen et
257 al., 2011). (The segmentation role of *ftz* is less widely conserved (Pick, 2016).) In addition, Notch
258 signalling components appear to oscillate in many clades (see below), as do *prd* and *hedgehog* in
259 spiders (Davis et al., 2005; Schoppmeier and Damen, 2005a; Schwager, 2008). However, since there
260 has not yet been an exhaustive screen for cyclic expression, we don't know how many other genes
261 may have been missed.

262 Measurements from *Tribolium* (El-Sherif et al., 2012; Nakamoto et al., 2015; Sarrazin et al., 2012)
263 and *Strigamia* (Brena and Akam, 2012) suggest an oscillation period in these species of ~3 hours at
264 18-20°C (or equivalently ~6 hrs at 13 °C or ~1.5 hours at 30°C, as segmentation speed scales with
265 developmental rate). Adjusted for temperature, these numbers are comparable to the fastest
266 segmenting vertebrates, such as zebrafish or snakes (Gomez et al., 2008). Interestingly, the rate of
267 segment addition is not constant throughout development (Brena and Akam, 2013; Nakamoto et al.,
268 2015). This implies that there is stage-specific variation in the oscillation period, the axial elongation
269 rate, and/or the dynamics of tissue maturation in the SAZ (Schröter et al., 2012; Soroldoni et al.,
270 2014).

271 At present, the mechanistic basis for the oscillations is not well understood. Nonetheless, it is useful
272 to think about contributing regulatory processes using a three-tier framework (Oates et al., 2012):
273 (1) gene expression dynamics within cells; (2) signalling interactions between cells; and (3) the
274 changing regulatory context along the SAZ.

275

276 *Gene expression dynamics within cells*

277 In vertebrates such as zebrafish, (auto)repressive interactions between Her/Hes transcription factors
278 (homologs of the *Drosophila* pair-rule gene *hairy*) are thought to form the core of the segmentation
279 clock, driving oscillations by time-delayed negative feedback (Lewis, 2003; Schröter et al., 2012).
280 Analogously, it is possible that the arthropod segmentation clock is driven by an intracellular
281 negative feedback loop formed by some or all of the oscillating pair-rule genes.

282 The main evidence for this is that knocking down primary pair-rule genes can block segmentation
283 and truncate the body axis, as has been found in *Tribolium* (Choe et al., 2006), the silkworm *Bombyx*
284 (Nakao, 2015), a second beetle species *Dermestes* (Xiang et al., 2017), and the hemipteran bug
285 *Oncopeltus* (Auman and Chipman, 2018; Liu and Kaufman, 2005). It can also cause the expression of

286 other primary pair-rule genes to become aperiodic (Choe et al., 2006; Nakao, 2015), suggesting that
287 at least some of the oscillations are mutually interdependent. This observation distinguishes these
288 knockdowns from those of downstream patterning genes, which may also yield asegmental
289 phenotypes but do not perturb expression dynamics in the SAZ (Choe and Brown, 2007; Farzana and
290 Brown, 2008).

291 The topology for a pair-rule gene segmentation clock is not clear. An early RNAi study in *Tribolium*
292 found that *eve*, *runt*, or *odd* knockdown resulted in truncation, while *hairy* knockdown resulted only
293 in head defects (Choe et al., 2006). This led to the hypothesis that *eve*, *runt*, and *odd* are linked into
294 a three-gene ring circuit, and that even though *hairy* oscillates in the SAZ, it is not required for
295 segmentation. Specifically, it was proposed that Eve activates *runt*, Runt activates *odd*, and Odd in
296 turn represses *eve*, returning the sequence to the beginning (**Fig. 2A**). However, more recent
297 evidence has raised issues with this proposal.

298 First, whether *hairy* is involved in the *Tribolium* segmentation clock or not remains unclear. A later
299 study found that *hairy* knockdown gave a pair-rule phenotype for gnathal and thoracic segments
300 (Aranda et al., 2008), and the iBeetle screen (Dönitz et al., 2015) additionally recovered posterior
301 truncations. *hairy* also has a paralog, *deadpan*, expressed with similar dynamics in the SAZ (Aranda
302 et al., 2008), and so its role might be masked by functional redundancy. Finally, *hairy* knockdown
303 was recently found to produce truncations in *Dermestes* (Xiang et al., 2017), and *hairy* is also known
304 to regulate segment patterning in the cockroach *Periplaneta* (Pueyo et al., 2008), the parasitic wasp
305 *Nasonia* (Rosenberg et al., 2014), and of course *Drosophila*, indicating that a role in segmentation is
306 widely conserved.

307 Second, whether *eve* and *odd* are part of the primary oscillator is also not certain. *eve* expression
308 may be necessary for establishing and/or maintaining the SAZ (Cruz et al., 2010; Liu and Kaufman,
309 2005; Mito et al., 2007; Xiang et al., 2017), and therefore its severe truncation phenotype may be
310 independent of its potential role in the segmentation clock. *odd*, on the other hand, has been found
311 to cause pair-rule defects rather than truncations in *Dermestes* (Xiang et al., 2017) and *Oncopeltus*
312 (Auman and Chipman, 2018), although the interpretation of these phenotypes is complicated by the
313 existence of *odd* paralogs, such as *sob*. Notably, neither *eve* nor *odd* shows dynamic expression in
314 the posterior SAZ of *Oncopeltus* (Auman and Chipman, 2018; Liu and Kaufman, 2005), indicating that
315 periodicity is likely to be generated by other genes in this species.

316 Finally, the specific regulatory interactions proposed for the circuit seem unlikely. In holometabolous
317 insects (and also *Strigamia*), *eve*, *runt*, and *odd* are expressed sequentially within each pattern
318 repeat (Choe et al., 2006; Clark, 2017; Green and Akam, 2013; Nakao, 2015; Rosenberg et al., 2014).

319 In both *Tribolium* and *Bombyx*, Eve is necessary for *runt* expression, and Runt is necessary for *odd*
320 expression (Choe et al., 2006; Nakao, 2015). However, it is probably not the case that Eve directly
321 activates *runt* and Runt directly activates *odd*, as was proposed for *Tribolium*. Instead, genetic
322 evidence from *Bombyx* and *Drosophila* (and wild-type expression dynamics from *Tribolium*) suggest
323 something closer to a “repressilator” scenario (Elowitz and Leibler, 2000), where each gene in the
324 sequence represses the one before it (**Fig. 2A**).

325 In summary, while it is likely that cross-regulation plays a considerable role in shaping dynamic pair-
326 rule gene expression, it is not yet clear whether the oscillating genes are linked into a single circuit,
327 whether this circuit is sufficient to generate oscillations, what the topology of this circuit is likely to
328 be, nor indeed the extent to which it may have diverged in different lineages (Krol et al., 2011).

329

330 *Signalling interactions between cells*

331 Regardless of whether the pair-rule gene network is capable of producing intracellular oscillations
332 autonomously, the segmentation clock must also involve intercellular communication to keep
333 oscillations synchronised across the SAZ. Notch signalling, known to synchronise oscillations during
334 vertebrate somitogenesis (Liao and Oates, 2017), is the key candidate for this role. Indeed, Notch
335 signalling components appear to oscillate along with the pair-rule genes in chelicerates
336 (Schoppmeier and Damen, 2005b; Stollewerk et al., 2003), myriapods (Chipman and Akam, 2008;
337 Kadner and Stollewerk, 2004), crustaceans (Eriksson et al., 2013), and some insects (Pueyo et al.,
338 2008), suggesting that arthropod segmentation ancestrally involved Notch.

339 Experiments in *Cupiennius*, *Periplaneta*, and the branchiopod crustacean *Daphnia* have found that
340 segment boundaries and the expression of segmentation genes become disorganised when Notch
341 signalling is perturbed (Eriksson et al., 2013; Pueyo et al., 2008; Schoppmeier and Damen, 2005b;
342 Stollewerk et al., 2003). Inhibiting Notch signalling also blocks segmentation (but not axial
343 elongation) in anostracan crustaceans (Williams et al., 2012). These findings indicate that Notch may
344 play an explicit role in generating and/or coordinating pair-rule gene oscillations, perhaps via
345 regulation of *hairy* (**Fig. 2B**).

346 However, the pleiotropy of the Notch pathway means that characterising this potential
347 segmentation function may be difficult. During development, Notch signalling also regulates cell
348 proliferation (Go et al., 1998), SAZ establishment (Chesebro et al., 2013; Oda et al., 2007; Schönauer
349 et al., 2016), and fertility (Xu and Gridley, 2012). Accordingly, strong Notch perturbations in

350 sequentially-segmenting arthropods often result in uninterpretable axial truncations, or simply a
351 failure to lay many eggs (Kux et al., 2013; Mito et al., 2011; Stahi and Chipman, 2016).

352 Surprisingly, in the insects *Gryllus*, *Oncopeltus*, and *Tribolium*, the Notch ligand *Delta* is not
353 expressed in the posterior SAZ (Aranda et al., 2008; Auman et al., 2017; Kainz et al., 2011). Either
354 Notch signalling acts through a different ligand in these species, or it does not directly regulate the
355 clock. *Delta* also seems not to play a segmentation role in the honeybee *Apis* (a simultaneously-
356 segmenting species), even though it is expressed in stripes at an appropriate time (Wilson et al.,
357 2010).

358 If a role for Notch signalling in sequential segmentation has indeed been lost in some insect lineages,
359 it is not clear what mechanism(s) might synchronise cells instead. One possibility is the Toll genes,
360 which are thought to influence intercellular affinity and are expressed dynamically in the SAZ across
361 arthropods (Benton et al., 2016; Paré et al., 2014). However, they seem only to affect
362 morphogenetic processes downstream of segment establishment, rather than segment patterning.
363 Another possibility that has been raised is intercellular communication via Tenascin major (Ten-m)
364 (Hunding and Baumgartner, 2017), a transmembrane protein that was erroneously identified as a
365 *Drosophila* pair-rule factor owing to an *opa* mutation present on the balancer chromosome of its
366 stock (Zheng et al., 2011). However, mutation/knockdown of *Ten-m* does not affect segmentation in
367 either *Drosophila* or *Tribolium* (Choe et al., 2006; Zheng et al., 2011), and Ten-m is expressed
368 periodically only after segment-polarity stripes have formed (Baumgartner et al., 1994; Jin et al.,
369 2019).

370

371 *The changing regulatory context along the SAZ*

372 The segmentation clock oscillates in the posterior SAZ and its phase is read out in the anterior SAZ.
373 Therefore, the “wavefront” can be loosely identified with the boundary between these regions,
374 which retracts posteriorly across the embryo over time. The posterior SAZ and the anterior SAZ are
375 apparently defined by the differential expression of specific regulatory factors (“timing factors” in
376 our terminology), which are expressed dynamically over the course of axial elongation, determining
377 where and when segment patterning takes place (Clark and Peel, 2018). Understanding the
378 mechanistic basis for the wavefront therefore entails characterising (1) the identities of these
379 factors, (2) how they regulate segmentation gene expression, and (3) how they themselves are
380 regulated in the embryo.

381 Many genes are specifically expressed in a subregion of the SAZ (Oberhofer et al., 2014). However,
382 most studies to date have focused on *Wnt* and *caudal*, supplemented recently by *Dichaete/Sox21b*
383 and *odd-paired (opa)/zic*. The expression patterns of these genes are relatively consistent across
384 species (**Fig. 2C**). *Wnt* is expressed in a small zone around the proctodaeum (Janssen et al., 2010).
385 (We note that this population of cells appears to be distinct from the SAZ proper, and may not
386 contribute to segmental tissue). In *Tribolium*, two of its receptors are expressed ubiquitously in the
387 embryo, and one is expressed in the anterior SAZ and in segmental stripes (Beermann et al., 2011).
388 *caudal* is expressed in the posterior SAZ (Copf et al., 2004; Schulz et al., 1998), and *Dichaete* is
389 expressed in a similar zone to *caudal*, but does not overlap with posterior *Wnt* (Clark and Peel, 2018;
390 Janssen et al., 2018; Paese et al., 2018). In contrast, *opa* is expressed in the anterior SAZ, i.e. anterior
391 to or slightly overlapping *caudal* and *Dichaete*, and also in segmental stripes (Clark and Peel, 2018;
392 Green and Akam, 2013; Janssen et al., 2011). Across arthropods, *Wnt*, *caudal* and *Dichaete* are
393 required to establish and maintain the SAZ (Angelini and Kaufman, 2005b; Bolognesi et al., 2008;
394 Chesebro et al., 2013; Copf et al., 2004; McGregor et al., 2008; Miyawaki et al., 2004; Nakao, 2018;
395 Paese et al., 2018; Schönauer et al., 2016; Shinmyo et al., 2005). In *Tribolium*, *opa* is required for
396 segmentation, following earlier roles in blastoderm formation and head specification (Clark and Peel,
397 2018).

398 Caudal and Dichaete are strong candidates for activating the segmentation clock, since their
399 expression domains roughly correlate with the extent of its oscillations, and they positively regulate
400 pair-rule gene expression in *Drosophila*. Caudal has also been shown to be necessary for *eve* and
401 *runt* expression in *Parasteatoda* (Schönauer et al., 2016). *Opa*, on the other hand, may be important
402 for reading out the phase of the clock, since it activates segment polarity genes and regulates late
403 pair-rule gene expression in *Drosophila* (Clark and Akam, 2016). Given that all three are transcription
404 factors, they might regulate segmentation by activating or repressing specific genes, modulating the
405 regulatory effects of other transcription factors, or switching expression control between different
406 enhancers. However, the severity of their knockdown phenotypes in sequentially-segmenting
407 species means that uncovering the details may require precisely targeted functional perturbations,
408 and probably transgenic reporters.

409 In sequentially-segmenting species, the relative expression patterns of different timing factors
410 remain consistent across development, suggesting that they regulate each other's expression. *Wnt* is
411 thought to act as a posterior organiser (Chesebro et al., 2013; Oberhofer et al., 2014), and we have
412 hypothesised that regulatory interactions between *caudal*, *Dichaete* and *opa* drive their sequential
413 expression over time (Clark and Peel, 2018). In addition, *caudal* has been found to be activated by
414 *Wnt* in diverse arthropods (Beermann et al., 2011; Chesebro et al., 2013; McGregor et al., 2008;

415 Miyawaki et al., 2004), while Opa, as a Zic factor, might physically bind the Wnt effector TCF and
416 modulate its effects on downstream genes (Murgan et al., 2015; Pourebrahim et al., 2011).
417 Therefore, while details are currently sketchy, it seems probable that the timing factors are
418 integrated into a regulatory network that ensures the maintenance of the SAZ over time, and also
419 governs its gradual posterior retraction. Given the numerous parallels between posterior
420 development in arthropods and posterior development in other bilaterian phyla, a similar network
421 might have ancestrally coordinated cell differentiation during axial extension, and only later been
422 exploited to regulate segmentation.

423 In the basic clock-and-wavefront model, the clock stops abruptly when it is hit by the wavefront.
424 However, in both arthropod segmentation and vertebrate somitogenesis, segmentation clock
425 oscillations may resolve into narrowing travelling waves before they stabilise, indicating that the
426 clock winds down relatively gradually. The way in which the oscillation period varies along the SAZ is
427 described phenomenologically by a “frequency profile” (Morelli et al., 2009), and this can vary over
428 developmental time, as well as between species. While the shape of the frequency profile is not
429 predicted to affect segmentation rate or segment size, models suggest that a graded profile might
430 make patterning more robust (El-Sherif et al., 2014; Vroomans et al., 2018).

431 Wnt signalling perturbations distort the size and proportions of the SAZ (as judged by the expression
432 of *caudal*), and cause equivalent distortions to the frequency profile (as judged by the expression of
433 *eve*) (El-Sherif et al., 2014). This indicates that Wnt signalling affects the dynamics of the
434 segmentation clock, and that its effects might be mediated by SAZ timing factors. However, the
435 mechanism for modulating the oscillation period is not clear. One hypothesis proposes that the clock
436 is quantitatively regulated by a morphogen gradient of Caudal (El-Sherif et al., 2014; Zhu et al.,
437 2017), but the effects of specific timing factors are yet to be disentangled and assessed. Currently, it
438 is unknown whether the period of the clock is indeed explicitly determined by the concentrations of
439 particular timing factors (i.e. given control of these levels one could produce sustained oscillations of
440 arbitrary period), or whether the slowing of the segmentation clock is an inherently transient
441 phenomenon inseparable from its temporal transition from an oscillating to a non-oscillating state
442 (Verd et al., 2014).

443

444 **Segment patterning by the pair-rule network**

445 *Reading out the pattern*

446 In the anterior SAZ, each segmentation clock cycle resolves into an anterior-to-posterior array of
447 partially overlapping stripes of pair-rule gene expression. Because the pair-rule genes are expressed
448 in a strict sequence across a clock repeat (e.g. first *eve*, then *runt*, then *odd*), they convey
449 unambiguous phase information to the cells they are expressed in, which provides significant
450 patterning benefits over a single-gene oscillator (**Fig. 3A**). The internal organisation of a parasegment
451 consists of at minimum three distinct segment-polarity states (Jaynes and Fujioka, 2004; Meinhardt,
452 1982). Therefore, each pair-rule gene expression repeat must specify at least three output domains
453 in species with single-segment periodicity, and at least six output domains in species with double-
454 segment periodicity (**Fig. 3B**).

455 In *Drosophila*, the relative expression patterns of pair-rule genes and segment-polarity genes have
456 been characterised in a variety of genetic backgrounds, allowing us to infer the regulatory
457 interactions involved in specifying and resolving the segment pattern (reviewed in Clark and Akam,
458 2016; Jaynes and Fujioka, 2004). Equivalent data is generally lacking from other arthropod species.
459 However, as far as we can tell from what does exist (mainly single or double stains in wild-type
460 embryos) the overall process appears to be fairly conserved, at least in its broad outline (Auman and
461 Chipman, 2018; Damen et al., 2005; Green and Akam, 2013; Xiang et al., 2017).

462 First, the primary pair-rule genes pattern the secondary pair-rule genes. Across arthropods, *prd* and
463 *slp* are expressed in a conserved, partially overlapping arrangement, which aligns with prospective
464 parasegment boundaries (Choe and Brown, 2007; Green and Akam, 2013). In both *Drosophila* and
465 other arthropods, *prd* turns on earlier than *slp*, at a time when upstream pair-rule gene expression is
466 still dynamic. In *Drosophila*, both genes are patterned by Eve, and we have proposed that the
467 dynamic nature of the Eve stripes (see below) helps differentially position the two domains (Clark,
468 2017) (**Fig. 3C**).

469 Next, the segment polarity-genes are activated. Each segment-polarity gene is activated or repressed
470 by particular pair-rule factors, which combinatorially define where it is expressed within the pattern
471 repeat (Bouchard et al., 2000; Choe and Brown, 2009; DiNardo and O'Farrell, 1987). In species with
472 double-segment periodicity, odd-numbered and even-numbered segment-polarity stripes may be
473 driven by different regulatory logic (**Fig. 3D**).

474 At the same time, some of the pair-rule genes also start being expressed in segment-polarity
475 patterns. In pair-rule species, this involves the splitting of existing stripes or the intercalation of new
476 ones. The new patterns are explained by a new network of regulatory interactions between the pair-
477 rule genes (Clark and Akam, 2016). In contrast to the earlier network, which drives dynamic
478 expression, this later one behaves like a multistable switch, "locking in" specific segment-polarity

479 fates (Clark, 2017). Interestingly, different primary pair-rule genes undergo frequency doubling in
480 each of *Drosophila*, *Bombyx*, *Tribolium*, and *Nasonia* (Choe et al., 2006; Clark and Akam, 2016;
481 Nakao, 2015; Rosenberg et al., 2014), contrasting with the conserved expression of the segment-
482 polarity and secondary pair-rule genes.

483 The resulting segmental patterns go on to regulate morphological segmentation. Note that the pair-
484 rule genes are therefore pleiotropic: they are involved in generating the segment pattern, but some
485 additionally play roles in maintaining segment-polarity, and they also regulate the development of
486 other structures, such as the nervous system. In some cases, these functions have become
487 distributed between multiple paralogs, e.g. *prd/gooseberry/pox-neuro* in *Drosophila* (He and Noll,
488 2013), or the three copies of *eve* in *Strigamia* (Green and Akam, 2013). Across species, there can be
489 considerable variation in both the number of paralogs present in the genome and the degree of
490 subfunctionalization between them, complicating the interpretation of genetic perturbations.

491

492 *The evolution of pair-rule patterning*

493 In several insect species, and also the centipede *Strigamia* (Chipman et al., 2004), segmentation
494 gene expression undergoes a striking transition from double-segment periodicity to single-segment
495 periodicity as the segment pattern is resolved. However, there is no indication of an initial double-
496 segment periodicity during sequential segmentation in the spiders *Cupiennius* (Davis et al., 2005;
497 Schoppmeier and Damen, 2005a) and *Parasteatoda* (Schwager, 2008), the millipede *Glomeris*
498 (Janssen et al., 2011), or the crustacean *Daphnia* (Eriksson et al., 2013) (**Fig. 1A**). This suggests that
499 the ancestral arthropod segmentation clock had a single-segment periodicity, and that pair-rule
500 patterning in insects and centipedes originated independently.

501 Beyond this, it is not clear exactly when or how many times pair-rule patterning evolved in either of
502 the centipede or insect lineages. *eve* is expressed segmentally rather than in pair-rule stripes in a
503 different centipede species, *Lithobius* (Hughes and Kaufman, 2002b), which could indicate that pair-
504 rule patterning evolved relatively recently within the centipede clade, possibly correlating with the
505 origin of longer bodied forms. However, the dynamics of the *Lithobius* segmentation clock will need
506 be investigated to rule out a transient or cryptic double-segment periodicity.

507 In insects, most of the available data come from holometabolan or orthopteran species, as well as
508 the cockroach *Periplaneta* and hemipteran bug *Oncopeltus* (**Fig. 1A**). Holometabolans (Binner and
509 Sander, 1997; Nakao, 2010; Patel et al., 1994; Rosenberg et al., 2014) and orthopterans (Davis et al.,
510 2001; Mito et al., 2007) both show obvious transitions from double-segment to single-segment

511 periodicity, but the mapping between the pair-rule pattern and the segmental pattern is different in
512 the two groups, suggesting that their respective pair-rule mechanisms might have evolved
513 independently. Consistent with this possibility, gene expression in *Periplaneta* (more closely related
514 to orthopterans than to holometabolans) appears to be single-segmental (Pueyo et al., 2008),
515 although, as with *Lithobius*, the dynamics of its segmentation clock have not been explicitly
516 investigated. Finally, *Oncopeltus* is a rather strange case: based on the expression and function of
517 *eve*, it appears to lack pair-rule patterning, but pair-rule expression and/or function of certain other
518 genes hints at an underlying double-segment periodicity (Auman and Chipman, 2018; Benton et al.,
519 2016; Erezylmaz et al., 2009; Liu and Kaufman, 2005).

520 Thus, while the evidence from some of these species is ambiguous, the current picture suggests that
521 pair-rule patterning may have evolved within crown-group insects, possibly multiple times. This is
522 puzzling, because the specialised and relatively invariant body plan of insects presents a
523 morphological constraint that is hard to reconcile with a saltational doubling of segmentation rate.
524 (Instead, it is much easier to imagine pair-rule patterning evolving in remipedes, which are thought
525 to be the sister group of hexapods (Schwentner et al 2017), and have homonomous, centipede-like
526 bodies.) How was the evolution of double-segment periodicity coordinated with compensatory
527 changes to Hox dynamics and the duration of axial extension, so as to keep segment number (**Box 2**)
528 and segment identity constant? Given that *Strigamia* seems to switch to a single segment periodicity
529 when adding its most posterior segments (Brena and Akam, 2013), and that pair-rule patterns are
530 seen during the anterior patterning of otherwise segmental species (Dearden et al., 2002; Janssen et
531 al., 2012), one possibility is that pair-rule patterning was introduced gradually along the AP axis,
532 allowing other developmental parameters the chance to adapt.

533 Since pair-rule patterning requires half the number of clock cycles to generate a given number of
534 segment-polarity stripes, its evolution may have been driven by selection for faster development (in
535 holometabolans) or a longer body (in centipedes). However, it is currently not obvious how the
536 ancestral segment patterning mechanism was modified to become pair-rule. Segmental frequency
537 could have been doubled by changing the “readout” of a conserved clock, i.e. by evolving new
538 enhancers to drive additional segment-polarity stripes in between the originals, or altering the
539 control logic of existing enhancers to drive a pair of stripes instead of just one. Alternatively, the
540 clock itself could have been modified, e.g. by recruiting new genes into the original cyclic repeat and
541 thereby expanding its patterning potential. To reconstruct the specific regulatory changes that
542 occurred, it will be informative to find out how the gene expression and enhancer logic of pair-rule
543 species compares to their closest segmental relatives.

544

545 **The evolution of simultaneous segmentation**

546 *Reconciling sequential and simultaneous segmentation*

547 A segmentation clock is one strategy for generating periodicity, but another is simply to regulate
548 each stripe individually, exploiting whatever positional information is locally available (François et
549 al., 2007; Salazar-Ciudad et al., 2001; Vroomans et al., 2016). This latter method is used in the
550 *Drosophila* blastoderm, where over 20 “stripe-specific elements” (SSEs) regulate the expression of
551 the five primary pair-rule genes (Schroeder et al., 2011). These elements receive spatial information
552 from gap factors, and each drives expression at a different AP position along the blastoderm,
553 contributing just one or two stripes to a gene’s overall 7-stripe pattern. Sepsid flies (which diverged
554 from drosophilids about 100 million years ago) are also known to use this kind of element (Hare et
555 al., 2008), and it is likely that similarly ad hoc regulatory mechanisms are used wherever periodicity
556 emerges simultaneously, e.g. in the blastoderms of *Nasonia* (Rosenberg et al., 2014) and *Oncopeltus*
557 (Stahi and Chipman, 2016), or in the chelicerate prosoma (Pechmann et al., 2011; Schwager et al.,
558 2009). While less “elegant” than using temporal oscillations, this explicitly spatial mode of
559 segmentation can—in principle—occur much faster, since a number of different pattern repeats can
560 be initialised at once.

561 Simultaneous segmentation, typified by *Drosophila*, is traditionally thought of as mechanistically
562 distinct from sequential segmentation, typified by e.g. *Tribolium* or *Gryllus*. The textbook model of
563 the hierarchical “subdivision” of a syncytial blastoderm by morphogen gradients seems a world away
564 from waves of gene expression within a cellularised, elongating germband. However, the *Drosophila*
565 blastoderm is now known to be more dynamic than was previously imagined, and the basic structure
566 of its segment patterning network seems remarkably similar to that of other arthropods (**Fig. 4A**).

567 As the *Drosophila* blastoderm stage is so short, the effects of dynamic gene expression are subtle,
568 and for years were overlooked. However, quantitative expression atlases suggest that expression
569 domains in the posterior half of the blastoderm travel anteriorly across cells over time (Jaeger et al.,
570 2004; Keränen et al., 2006; Surkova et al., 2008), and this has recently been demonstrated through
571 live imaging (El-Sherif and Levine, 2016; Lim et al., 2018). The shifts reflect sequential patterns of
572 transcriptional states within cells, and trace back to asymmetric repressive interactions in the gap
573 gene network (Jaeger, 2011; Verd et al., 2018) (**Fig. 4B1**) – perhaps similar to the ones driving their
574 temporal expression in the SAZs of sequentially-segmenting species.

575 In the *Drosophila* blastoderm, the expression dynamics of the gap genes are directly transferred to
576 pair-rule genes via their SSEs (**Fig. 4B2**). In addition, the pair-rule genes cross-regulate each other
577 through “zebra elements”: enhancers that drive expression in all of the trunk stripes simultaneously
578 (Schroeder et al., 2011). (Some primary pair-rule genes, and both secondary pair-rule genes, possess
579 zebra elements.) These regulatory interactions are also dynamic, and they combine with the stripe
580 shifts driven by the gap genes to generate a staggered sequence of pair-rule gene expression within
581 each double-segment repeat (Clark, 2017) (**Fig. 4B3**). This spatiotemporal sequence is the same as
582 that driven by the segmentation clock in sequentially-segmenting species such as *Tribolium* and
583 *Strigamia* (Choe et al., 2006; Green and Akam, 2013), suggesting that zebra enhancers and “clock”
584 enhancers may be homologous.

585 Once primary pair-rule gene expression is properly phased within each double-segment repeat,
586 *Drosophila* segment patterning proceeds just as it would in the anterior SAZ of a sequentially-
587 segmenting species, beginning with the activation of *prd* and *slp*, and moving on to segment-polarity
588 gene expression and stripe doubling. This conserved process of pattern resolution is apparently
589 regulated by a conserved sequence of timing factor expression: posterior SAZ factors Caudal and
590 Dichaete are expressed throughout the trunk during the early, dynamic stages of pair-rule gene
591 expression in *Drosophila*, and are replaced by anterior SAZ factor Opa as the segment-polarity
592 pattern is being resolved (Clark and Peel, 2018).

593 The *Drosophila* blastoderm therefore seems effectively equivalent to a SAZ, except that rather than
594 maturing gradually from anterior to posterior, it does so all at once (**Fig. 4C**). We suspect that much
595 of the ancestral segmentation machinery remains intact. However, since spatial information is no
596 longer conveyed by the delayed maturation of posterior tissue, gap genes and SSEs preload it into
597 the system instead (**Fig. 4A**). Importantly, while genetic perturbations tend to result in different
598 phenotypes in the two modes of segmentation (e.g. primary pair-rule genes cause pair-rule
599 phenotypes in *Drosophila* rather than truncations), this might often be explained by the divergent
600 deployment of the genes in the embryo, rather than divergent function.

601

602 *The evolution of stripe-specific elements*

603 Simultaneous segmentation differs from sequential segmentation in two key respects: its temporal
604 regulation (determined by the expression profiles of the timing factors), and the spatial pre-
605 patterning of the pair-rule genes by gap genes (**Fig. 4C**). Simultaneous segmentation is also
606 associated with an anterior shift of the blastoderm fate map and an increase in the number of

607 segments patterned prior to gastrulation. (Note, however, that although segment patterning in the
608 blastoderm is often simultaneous and regulated by gap genes, this need not be the case: *Tribolium*
609 patterns its blastoderm segments sequentially, using retracting timing factors and a clock (El-Sherif
610 et al., 2014, 2012).)

611 The evolution of simultaneous segmentation appears to be constrained by early embryogenesis
612 (French, 1988). Some insects, such as orthopterans, have “panoistic” ovaries, in which all germline
613 cells become oocytes, and the eggs contain little but yolk (Büning, 1994). These species pattern their
614 segments sequentially. Other insects, such as hemipterans and holometabolans, have “meroistic”
615 ovaries, in which germline-derived “nurse” cells load oocytes with maternal mRNA. These species
616 frequently have a biphasic mode of segmentation, in which anterior segments are patterned
617 simultaneously. Meroistic ovaries (which facilitate pre-patterning of the egg), may therefore be a
618 pre-adaptation for simultaneous segmentation.

619 Extreme examples of simultaneous segmentation (e.g. *Drosophila*) have evolved independently
620 within each of the major holometabolan orders (Davis and Patel, 2002). (Intriguingly, there has also
621 been at least one reversion to sequential segmentation, within braconid wasps (Sucena et al.,
622 2014)). A *Drosophila*-like mode of segmentation likely requires far-reaching changes to early
623 embryogenesis, such as a novel anterior patterning centre to help spatially pattern gap genes along
624 the entire AP axis of the egg (Lynch et al., 2006) (**Fig. 4A**). Here, we focus on understanding how SSEs
625 and gap genes are together able to take over stripe patterning from the clock. It seems likely that
626 this transition to intricate spatial regulation involves a series of selectively favourable regulatory
627 changes, which incrementally increase the speed or robustness of segmentation, while strictly
628 preserving its output (**Fig. 5**).

629 First, new SSEs seem to be easy to evolve, because they tend to be short, with simple regulatory
630 logic and high sequence turnover between closely related species (Hare et al., 2008; Ludwig et al.,
631 1998). Some of them may have been selected simply to increase the robustness of segmentation
632 clock expression; this might have occurred in either a blastoderm or a SAZ context. (There is one
633 report from *Tribolium* suggesting the existence of SSEs that drive expression in the germband (Eckert
634 et al., 2004)). Importantly, because gap gene expression is inherently dynamic (whether in the
635 blastoderm or the SAZ), SSE-regulated stripes are predicted to “shadow” stripes driven by the clock,
636 allowing them to take over downstream functions quite gradually (Verd et al., 2018) (**Fig. 5A**).

637 Second, only a single new SSE need evolve at one time. Simultaneous patterning seems likely to have
638 evolved progressively, from anterior to posterior, with each new SSE-driven stripe reducing the
639 number of cycles needed from the clock (Peel and Akam, 2003) (**Fig. 5B**). Furthermore, cross-

640 regulation between the pair-rule genes means that a SSE for one gene could in principle go on to
641 organise a whole pattern repeat, with the remaining genes evolving their own SSEs afterwards, to
642 make patterning faster or more robust (Clark, 2017) (**Fig. 5C**). This process might be highly
643 contingent: in *Drosophila*, *eve* and *runt* have full sets of SSEs and *odd* is patterned largely through
644 cross-regulation (Schroeder et al., 2011), but RNAi evidence from *Bombyx* suggests precisely the
645 opposite (Nakao, 2015).

646 Finally, SSEs can be reused. In *Drosophila* there are several SSEs that drive a pair of stripes, typically
647 arranged symmetrically around a particular gap domain (Schroeder et al., 2011). This suggests that
648 posterior gap gene expression evolved to duplicate the regulatory environments of anterior stripes,
649 initialising additional pair-rule gene stripes without the need to evolve additional SSEs (**Fig. 5D**).

650 Interestingly, *Drosophila eve* stripes 3 and 7, which are co-driven by a single SSE, are regulated by
651 the same gap genes as are *eve* stripes 3 and 6 in *Anopheles* (Goltsev et al., 2004), which has led to a
652 proposal that certain stripes have been lost or gained from these lineages over time (Rothschild et
653 al., 2016). This hypothesis is hard to reconcile with the gradualist scenario we favour, since the
654 transitional states would have severely compromised fitness. We think it more likely that the
655 posterior gap gene domains were recruited in a different order in the *Drosophila* and *Anopheles*
656 lineages, resulting in a homologous “stripe 3” element additionally driving non-homologous
657 posterior stripes. In support of this alternative, a midge species more closely related to *Drosophila*
658 than to *Anopheles* patterns only five *eve* stripes before gastrulation (Rohr et al., 1999), indicating
659 that the two lineages probably evolved fully simultaneous segmentation independently (Jaeger,
660 2011).

661

662 **Conclusion**

663 Our current understanding is that arthropod segment patterning is an inherently dynamic and a
664 significantly conserved process, ancestrally taking the form of a clock-and-wavefront system. Note,
665 however, that many of the conclusions in this review extrapolate from fragmentary data gathered
666 from a small number of model species, with functional data available from an even smaller number.
667 This is certainly not the last word on arthropod segmentation, but we hope to have provided a
668 coherent framework for further thought and experiment.

669 We anticipate that future investigation will centre on two contrasting but interrelated tasks. First,
670 better resolving the nature of the ancestral arthropod clock-and-wavefront system: the topology of
671 the gene regulatory networks comprising the clock, the production of timing factor wavefronts by a

672 retracting SAZ, and the mechanistic basis for the interactions between them. Second, reconstructing
673 how arthropod segmentation networks have diversified over time, giving rise to such remarkable
674 novelties as simultaneous patterning and double-segment periodicity. In addition, we believe that
675 sequentially-segmenting arthropod models are well placed to complement and inform the study of
676 vertebrate axial patterning, especially given their benefits of cost-efficiency, short generation times,
677 experimental tractability, and relatively simple genomes.

678 The most pressing next step is to collect good-quality multiplexed expression data from a variety of
679 arthropod species (Choi et al., 2018, 2016) and cross-reference this with information about tissue
680 dynamics (Wolff et al., 2018), to better characterise how segmentation gene expression changes
681 over space and time. Building on a solid descriptive foundation, there are numerous exciting
682 directions to pursue: genome editing to generate mutants, misexpression constructs, and live
683 reporters (Gilles et al., 2015; Lai et al., 2018); construction and analysis of data-informed dynamical
684 models (Sharpe, 2017); single-cell sequencing of segmenting tissues (Griffiths et al., 2018); *ex vivo*
685 culturing of SAZ cells (Lauschke et al., 2013). Over the past four decades, arthropod segmentation
686 has contributed enormously to our understanding of developmental gene networks and their
687 evolution. As we enter a new “golden age” of developmental biology, we see great promise for this
688 legacy to continue.

689

690 **Acknowledgements**

691 We thank Olivia Tidswell, Matthew Benton, Lauren Bush, Mariana Wolfner and Roger Keynes for
692 comments on the manuscript.

693

694 **Funding**

695 MEA and EC were supported by BBSRC research grant BB/P009336/1. EC was also supported by a
696 Junior Research Fellowship from Trinity College, Cambridge, and an EMBO Long Term Fellowship.
697 ADP was supported by BBSRC research grant BB/L020092/1.

References

- Akam, M., 1987. The molecular basis for metameric pattern in the *Drosophila* embryo. *Development* 101, 1–22.
- Anderson, D.T., 1973. Embryology and phylogeny in annelids and arthropods., International series of monographs in pure and applied biology. Pergamon Press, Oxford.
- Angelini, D.R., Kaufman, T.C., 2005a. Insect appendages and comparative ontogenetics. *Dev. Biol.* 286, 57–77.
- Angelini, D.R., Kaufman, T.C., 2005b. Functional analyses in the milkweed bug *Oncopeltus fasciatus* (Hemiptera) support a role for Wnt signaling in body segmentation but not appendage development. *Dev. Biol.* 283, 409–423.
- Aranda, M., Marques-Souza, H., Bayer, T., Tautz, D., 2008. The role of the segmentation gene hairy in *Tribolium*. *Dev. Genes Evol.* 218, 465–477.
- Auman, T., Chipman, A.D., 2018. Growth zone segmentation in the milkweed bug *Oncopeltus fasciatus* sheds light on the evolution of insect segmentation. *BMC Evol. Biol.* 18, 178.
- Auman, T., Vreede, B.M.I., Weiss, A., Hester, S.D., Williams, T.A., Nagy, L.M., Chipman, A.D., 2017. Dynamics of growth zone patterning in the milkweed bug *Oncopeltus fasciatus*. *Development* 144, 1896–1905.
- Azpiaz, N., Lawrence, P.A., Vincent, J.P., Frasch, M., 1996. Segmentation and specification of the *Drosophila* mesoderm. *Genes Dev.* 10, 3183–3194.
- Baumgartner, S., Martin, D., Hagios, C., Chiquet-Ehrismann, R., 1994. Tenm, a *Drosophila* gene related to tenascin, is a new pair-rule gene. *EMBO J.* 13, 3728–3740.
- Beermann, A., Prühs, R., Lutz, R., Schröder, R., 2011. A context-dependent combination of Wnt receptors controls axis elongation and leg development in a short germ insect. *Development* 138, 2793–2805.
- Benton, M.A., 2018. A revised understanding of *Tribolium* morphogenesis further reconciles short and long germ development. *PLOS Biol.* 16, e2005093.
- Benton, M.A., Pechmann, M., Frey, N., Stappert, D., Conrads, K.H., Chen, Y.-T., Stamatakis, E., Pavlopoulos, A., Roth, S., 2016. Toll Genes Have an Ancestral Role in Axis Elongation. *Curr. Biol.* 26, 1609–1615.
- Binner, P., Sander, K., 1997. Pair-rule patterning in the honeybee *Apis mellifera*: Expression of even-skipped combines traits known from beetles and fruitfly. *Dev. Genes Evol.* 206, 447–454.
- Blower, J.G., 1985. Millipedes, Linnean Society Synopses of the British Fauna. E.J. Brill/Dr. W. Backhuys, London.
- Bolognesi, R., Farzana, L., Fischer, T.D., Brown, S.J., 2008. Multiple Wnt genes are required for segmentation in the short-germ embryo of *Tribolium castaneum*. *Curr. Biol. CB* 18, 1624–1629.
- Bouchard, M., St-Amand, J., Côté, S., 2000. Combinatorial Activity of Pair-Rule Proteins on the *Drosophila* gooseberry Early Enhancer. *Dev. Biol.* 222, 135–146.
- Brena, C., Akam, M., 2013. An analysis of segmentation dynamics throughout embryogenesis in the centipede *Strigamia maritima*. *BMC Biol.* 11, 112.
- Brena, C., Akam, M., 2012. The embryonic development of the centipede *Strigamia maritima*. *Dev. Biol.* 363, 290–307.
- Brusca, R.C., Moore, W., Shuster, S.M., 2016. Invertebrates, 3rd. ed. Sinauer, Sunderland Mass.
- Büning, J., 1994. The Insect Ovary: Ultrastructure, previtellogenic growth and evolution. Springer Netherlands.
- Cepeda, R.E., Pardo, R.V., Macaya, C.C., Sarrazin, A.F., 2017. Contribution of cell proliferation to axial elongation in the red flour beetle *Tribolium castaneum*. *PLOS ONE* 12, e0186159.
- Chesebro, J.E., Pueyo, J.I., Couso, J.P., 2013. Interplay between a Wnt-dependent organiser and the Notch segmentation clock regulates posterior development in *Periplaneta americana*. *Biol. Open* 2, 227–237.

- Chipman, A.D., Akam, M., 2008. The segmentation cascade in the centipede *Strigamia maritima*: Involvement of the Notch pathway and pair-rule gene homologues. *Dev. Biol.* 319, 160–169.
- Chipman, A.D., Arthur, W., Akam, M., 2004. A Double Segment Periodicity Underlies Segment Generation in Centipede Development. *Curr. Biol.* 14, 1250–1255.
- Choe, C.P., Brown, S.J., 2009. Genetic regulation of engrailed and wingless in *Tribolium* segmentation and the evolution of pair-rule segmentation. *Dev. Biol.* 325, 482–491.
- Choe, C.P., Brown, S.J., 2007. Evolutionary flexibility of pair-rule patterning revealed by functional analysis of secondary pair-rule genes, paired and sloppy-paired in the short-germ insect, *Tribolium castaneum*. *Dev. Biol.* 302, 281–294.
- Choe, C.P., Miller, S.C., Brown, S.J., 2006. A pair-rule gene circuit defines segments sequentially in the short-germ insect *Tribolium castaneum*. *Proc. Natl. Acad. Sci.* 103, 6560–6564.
- Choi, H.M.T., Calvert, C.R., Husain, N., Huss, D., Barsi, J.C., Deverman, B.E., Hunter, R.C., Kato, M., Lee, S.M., Abelin, A.C.T., Rosenthal, A.Z., Akbari, O.S., Li, Y., Hay, B.A., Sternberg, P.W., Patterson, P.H., Davidson, E.H., Mazmanian, S.K., Prober, D.A., Rijn, M. van de, Leadbetter, J.R., Newman, D.K., Readhead, C., Bronner, M.E., Wold, B., Lansford, R., Sauka-Spengler, T., Fraser, S.E., Pierce, N.A., 2016. Mapping a multiplexed zoo of mRNA expression. *Development* 143, 3632–3637.
- Choi, H.M.T., Schwarzkopf, M., Fornace, M.E., Acharya, A., Artavanis, G., Stegmaier, J., Cunha, A., Pierce, N.A., 2018. Third-generation in situ hybridization chain reaction: multiplexed, quantitative, sensitive, versatile, robust. *Development* 145, dev165753.
- Clark, E., 2017. Dynamic patterning by the *Drosophila* pair-rule network reconciles long-germ and short-germ segmentation. *PLOS Biol.* 15, e2002439.
- Clark, E., Akam, M., 2016. Odd-paired controls frequency doubling in *Drosophila* segmentation by altering the pair-rule gene regulatory network. *eLife* 5, e18215.
- Clark, E., Peel, A.D., 2018. Evidence for the temporal regulation of insect segmentation by a conserved sequence of transcription factors. *Development* 145, dev155580.
- Cooke, J., Zeeman, E.C., 1976. A clock and wavefront model for control of the number of repeated structures during animal morphogenesis. *J. Theor. Biol.* 58, 455–476.
- Copf, T., Schröder, R., Averof, M., 2004. Ancestral role of caudal genes in axis elongation and segmentation. *Proc. Natl. Acad. Sci. U. S. A.* 101, 17711–17715.
- Cruz, C., Maegawa, S., Weinberg, E.S., Wilson, S.W., Dawid, I.B., Kudoh, T., 2010. Induction and patterning of trunk and tail neural ectoderm by the homeobox gene *eve1* in zebrafish embryos. *Proc. Natl. Acad. Sci.* 107, 3564–3569.
- Damen, W.G.M., 2002. Parasegmental organization of the spider embryo implies that the parasegment is an evolutionary conserved entity in arthropod embryogenesis. *Development* 129, 1239–1250.
- Damen, W.G.M., Janssen, R., Prpic, N.-M., 2005. Pair rule gene orthologs in spider segmentation. *Evol. Dev.* 7, 618–628.
- Davis, G.K., D'Alessio, J.A., Patel, N.H., 2005. Pax3/7 genes reveal conservation and divergence in the arthropod segmentation hierarchy. *Dev. Biol.* 285, 169–184.
- Davis, G.K., Jaramillo, C.A., Patel, N.H., 2001. Pax group III genes and the evolution of insect pair-rule patterning. *Development* 128, 3445–3458.
- Davis, G.K., Patel, N.H., 2002. Short, Long, and Beyond: Molecular and Embryological Approaches to Insect Segmentation. *Annu. Rev. Entomol.* 47, 669–699.
- Dearden, P.K., Donly, C., Grbić, M., 2002. Expression of pair-rule gene homologues in a chelicerate: early patterning of the two-spotted spider mite *Tetranychus urticae*. *Development* 129, 5461–5472.
- Deutsch, J.S., 2004. Segments and parasegments in Arthropods: a functional perspective. *BioEssays* 26, 1117–1125.

- DiNardo, S., O'Farrell, P.H., 1987. Establishment and refinement of segmental pattern in the *Drosophila* embryo: spatial control of engrailed expression by pair-rule genes. *Genes Dev.* 1, 1212–1225.
- Dönitz, J., Schmitt-Engel, C., Grossmann, D., Gerischer, L., Tech, M., Schoppmeier, M., Klingler, M., Bucher, G., 2015. iBeetle-Base: a database for RNAi phenotypes in the red flour beetle *Tribolium castaneum*. *Nucleic Acids Res.* 43, D720-725.
- Eckert, C., Aranda, M., Wolff, C., Tautz, D., 2004. Separable stripe enhancer elements for the pair-rule gene hairy in the beetle *Tribolium*. *EMBO Rep.* 5, 638–642.
- Elowitz, M.B., Leibler, S., 2000. A synthetic oscillatory network of transcriptional regulators. *Nature* 403, 335.
- El-Sherif, E., Averof, M., Brown, S.J., 2012. A segmentation clock operating in blastoderm and germband stages of *Tribolium* development. *Dev. Camb. Engl.* 139, 4341–4346.
- El-Sherif, E., Levine, M., 2016. Shadow Enhancers Mediate Dynamic Shifts of Gap Gene Expression in the *Drosophila* Embryo. *Curr. Biol.* 26, 1164–1169.
- El-Sherif, E., Zhu, X., Fu, J., Brown, S.J., 2014. Caudal Regulates the Spatiotemporal Dynamics of Pair-Rule Waves in *Tribolium*. *PLOS Genet.* 10, e1004677.
- Erezylmaz, D.F., Kelstrup, H.C., Riddiford, L.M., 2009. The nuclear receptor E75A has a novel pair-rule-like function in patterning the milkweed bug, *Oncopeltus fasciatus*. *Dev. Biol.* 334, 300–310.
- Eriksson, B.J., Ungerer, P., Stollewerk, A., 2013. The function of Notch signalling in segment formation in the crustacean *Daphnia magna* (Branchiopoda). *Dev. Biol.* 383, 321–330.
- Farzana, L., Brown, S.J., 2008. Hedgehog signaling pathway function conserved in *Tribolium* segmentation. *Dev. Genes Evol.* 218, 181–192.
- François, P., Hakim, V., Siggia, E.D., 2007. Deriving structure from evolution: metazoan segmentation. *Mol. Syst. Biol.* 3, 154.
- French, V., 1988. Gradients and insect segmentation. *Development* 104, 3–16.
- Gilles, A.F., Schinko, J.B., Averof, M., 2015. Efficient CRISPR-mediated gene targeting and transgene replacement in the beetle *Tribolium castaneum*. *Dev. Camb. Engl.* 142, 2832–2839.
- Go, M.J., Eastman, D.S., Artavanis-Tsakonas, S., 1998. Cell proliferation control by Notch signaling in *Drosophila* development. *Development* 125, 20131–2040.
- Goltsev, Y., Hsiong, W., Lanzaro, G., Levine, M., 2004. Different combinations of gap repressors for common stripes in *Anopheles* and *Drosophila* embryos. *Dev. Biol.* 275, 435–446.
- Gomez, C., Ozbudak, E.M., Wunderlich, J., Baumann, D., Lewis, J., Pourquié, O., 2008. Control of segment number in vertebrate embryos. *Nature* 454, 335–339.
- Green, J., Akam, M., 2013. Evolution of the pair rule gene network: Insights from a centipede. *Dev. Biol.* 382, 235–245.
- Griffiths, J.A., Scialdone, A., Marioni, J.C., 2018. Using single-cell genomics to understand developmental processes and cell fate decisions. *Mol. Syst. Biol.* 14, e8046.
- Hannibal, R.L., Patel, N.H., 2013. What is a segment? *EvoDevo* 4, 35.
- Hannibal, R.L., Price, A.L., Patel, N.H., 2012. The functional relationship between ectodermal and mesodermal segmentation in the crustacean, *Parhyale hawaiiensis*. *Dev. Biol.* 361, 427–438.
- Hare, E.E., Peterson, B.K., Iyer, V.N., Meier, R., Eisen, M.B., 2008. Sepsid even-skipped Enhancers Are Functionally Conserved in *Drosophila* Despite Lack of Sequence Conservation. *PLOS Genet.* 4, e1000106.
- He, H., Noll, M., 2013. Differential and redundant functions of gooseberry and gooseberry neuro in the central nervous system and segmentation of the *Drosophila* embryo. *Dev. Biol.* 382, 209–223.
- Hubaud, A., Pourquié, O., 2014. Signalling dynamics in vertebrate segmentation. *Nat. Rev. Mol. Cell Biol.* 15, 709–721.
- Hughes, C.L., Kaufman, T.C., 2002a. Hox genes and the evolution of the arthropod body plan1. *Evol. Dev.* 4, 459–499.

- Hughes, C.L., Kaufman, T.C., 2002b. Exploring Myriapod Segmentation: The Expression Patterns of even-skipped, engrailed, and wingless in a Centipede. *Dev. Biol.* 247, 47–61.
- Hunding, A., Baumgartner, S., 2017. Ancient role of ten-m/odf in segmentation and the transition from sequential to syncytial segmentation. *Hereditas* 154, 8–8.
- Jaeger, J., 2011. The gap gene network. *Cell. Mol. Life Sci. CMLS* 68, 243–274.
- Jaeger, J., Surkova, S., Blagov, M., Janssens, H., Kosman, D., Kozlov, K.N., Manu, Myasnikova, E., Vanario-Alonso, C.E., Samsonova, M., Sharp, D.H., Reinitz, J., 2004. Dynamic control of positional information in the early *Drosophila* embryo. *Nature* 430, 368–371.
- Janssen, R., 2011. Diplosegmentation in the pill millipede *Glomeris marginata* is the result of dorsal fusion. *Evol. Dev.* 13, 477–487.
- Janssen, R., Andersson, E., Betnér, E., Bijl, S., Fowler, W., Höök, L., Leyhr, J., Mannelqvist, A., Panara, V., Smith, K., Tiemann, S., 2018. Embryonic expression patterns and phylogenetic analysis of panarthropod *sox* genes: insight into nervous system development, segmentation and gonadogenesis. *BMC Evol. Biol.* 18, 88.
- Janssen, R., Budd, G.E., 2013. Deciphering the onychophoran ‘segmentation gene cascade’: Gene expression reveals limited involvement of pair rule gene orthologs in segmentation, but a highly conserved segment polarity gene network. *Dev. Biol.* 382, 224–234.
- Janssen, R., Budd, G.E., Prpic, N.-M., Damen, W.G., 2011. Expression of myriapod pair rule gene orthologs. *EvoDevo* 2, 5.
- Janssen, R., Damen, W.G.M., Budd, G.E., 2012. Expression of pair rule gene orthologs in the blastoderm of a myriapod: evidence for pair rule-like mechanisms? *BMC Dev. Biol.* 12, 15.
- Janssen, R., Le Gouar, M., Pechmann, M., Poulin, F., Bolognesi, R., Schwager, E.E., Hopfen, C., Colbourne, J.K., Budd, G.E., Brown, S.J., Prpic, N.-M., Kosiol, C., Vervoort, M., Damen, W.G., Balavoine, G., McGregor, A.P., 2010. Conservation, loss, and redeployment of Wnt ligands in protostomes: implications for understanding the evolution of segment formation. *BMC Evol. Biol.* 10, 374.
- Janssen, R., Prpic, N.-M., Damen, W.G.M., 2004. Gene expression suggests decoupled dorsal and ventral segmentation in the millipede *Glomeris marginata* (Myriapoda: Diplopoda). *Dev. Biol.* 268, 89–104.
- Jaynes, J.B., Fujioka, M., 2004. Drawing lines in the sand: even skipped et al. and parasegment boundaries. *Dev. Biol.* 269, 609–622.
- Jin, S., O, J., Stellabotte, F., Brown, S.J., Choe, C.P., 2019. Expression of *teneurin-m/odd* *Oz* during segmentation in the beetle *Tribolium castaneum*. *Gene Expr. Patterns GEP* 31, 26–31.
- Kadner, D., Stollewerk, A., 2004. Neurogenesis in the chilopod *Lithobius forficatus* suggests more similarities to chelicerates than to insects. *Dev. Genes Evol.* 214, 367–379.
- Kainz, F., Ewen-Campen, B., Akam, M., Extavour, C.G., 2011. Notch/Delta signalling is not required for segment generation in the basally branching insect *Gryllus bimaculatus*. *Dev. Camb. Engl.* 138, 5015–5026.
- Keränen, S.V., Fowlkes, C.C., Luengo Hendriks, C.L., Sudar, D., Knowles, D.W., Malik, J., Biggin, M.D., 2006. Three-dimensional morphology and gene expression in the *Drosophila* blastoderm at cellular resolution II: dynamics. *Genome Biol.* 7, R124.
- Krause, G., 1939. *Die Eitypen der Insekten*. Thieme.
- Krol, A.J., Roellig, D., Dequéant, M.-L., Tassy, O., Glynn, E., Hattem, G., Mushegian, A., Oates, A.C., Pourquié, O., 2011. Evolutionary plasticity of segmentation clock networks. *Dev. Camb. Engl.* 138, 2783–2792.
- Kux, K., Kiparaki, M., Delidakis, C., 2013. The two *Tribolium* *E(spl)* genes show evolutionarily conserved expression and function during embryonic neurogenesis. *Mech. Dev.* 130, 207–225.
- Lai, Y.-T., Deem, K.D., Borràs-Castells, F., Sambrani, N., Rudolf, H., Suryamohan, K., El-Sherif, E., Halfon, M.S., McKay, D.J., Tomoyasu, Y., 2018. Enhancer identification and activity evaluation in the red flour beetle, *Tribolium castaneum*. *Dev. Camb. Engl.* 145.

- Lauschke, V.M., Tsiairis, C.D., François, P., Aulehla, A., 2013. Scaling of embryonic patterning based on phase-gradient encoding. *Nature* 493, 101–105.
- Lewis, J., 2003. Autoinhibition with Transcriptional Delay: A Simple Mechanism for the Zebrafish Somitegenesis Oscillator. *Curr. Biol.* 13, 1398–1408.
- Liao, B.-K., Oates, A.C., 2017. Delta-Notch signalling in segmentation. *Arthropod Struct. Dev.* 46, 429–447.
- Lim, B., Fukaya, T., Heist, T., Levine, M., 2018. Temporal dynamics of pair-rule stripes in living *Drosophila* embryos. *Proc. Natl. Acad. Sci.* 115, 8376–8381.
- Liu, P.Z., Kaufman, T.C., 2005. even-skipped is not a pair-rule gene but has segmental and gap-like functions in *Oncopeltus fasciatus*, an intermediate germband insect. *Development* 132, 2081–2092.
- Liu, Q., Onal, P., Datta, R.R., Rogers, J.M., Schmidt-Ott, U., Bulyk, M.L., Small, S., Thornton, J.W., 2018. Ancient mechanisms for the evolution of the bicoid homeodomain's function in fly development. *eLife* 7, e34594.
- Ludwig, M.Z., Patel, N.H., Kreitman, M., 1998. Functional analysis of eve stripe 2 enhancer evolution in *Drosophila*: rules governing conservation and change. *Development* 125, 949–958.
- Lynch, J.A., Brent, A.E., Leaf, D.S., Pultz, M.A., Desplan, C., 2006. Localized maternal orthodenticle patterns anterior and posterior in the long germ wasp *Nasonia*. *Nature* 439, 728–732.
- Marques-Souza, H., Aranda, M., Tautz, D., 2008. Delimiting the conserved features of hunchback function for the trunk organization of insects. *Development* 135, 881–888.
- Martin, A., Serano, J.M., Jarvis, E., Bruce, H.S., Wang, J., Ray, S., Barker, C.A., O'Connell, L.C., Patel, N.H., 2016. CRISPR/Cas9 Mutagenesis Reveals Versatile Roles of Hox Genes in Crustacean Limb Specification and Evolution. *Curr. Biol.* 26, 14–26.
- Martinez-Arias, A., Lawrence, P.A., 1985. Parasegments and compartments in the *Drosophila* embryo. *Nature* 313, 639–642.
- McGregor, A.P., 2005. How to get ahead: the origin, evolution and function of bicoid. *BioEssays* 27, 904–913.
- McGregor, A.P., Pechmann, M., Schwager, E.E., Feitosa, N.M., Kruck, S., Aranda, M., Damen, W.G.M., 2008. Wnt8 is required for growth-zone establishment and development of opisthosomal segments in a spider. *Curr. Biol. CB* 18, 1619–1623.
- Meinhardt, H., 1982. *Models of Biological Pattern Formation*. Academic Press.
- Misof, B., Liu, S., Meusemann, K., Peters, R.S., Donath, A., Mayer, C., Frandsen, P.B., Ware, J., Flouri, T., Beutel, R.G., Niehuis, O., Petersen, M., Izquierdo-Carrasco, F., Wappler, T., Rust, J., Aberer, A.J., Aspöck, U., Aspöck, H., Bartel, D., Blanke, A., Berger, S., Böhm, A., Buckley, T.R., Calcott, B., Chen, J., Friedrich, F., Fukui, M., Fujita, M., Greve, C., Grobe, P., Gu, S., Huang, Y., Jermiin, L.S., Kawahara, A.Y., Krogmann, L., Kubiak, M., Lanfear, R., Letsch, H., Li, Yiyuan, Li, Z., Li, J., Lu, H., Machida, R., Mashimo, Y., Kapli, P., McKenna, D.D., Meng, G., Nakagaki, Y., Navarrete-Heredia, J.L., Ott, M., Ou, Y., Pass, G., Podsiadlowski, L., Pohl, H., Reumont, B.M. von, Schütte, K., Sekiya, K., Shimizu, S., Slipinski, A., Stamatakis, A., Song, W., Su, X., Szucsich, N.U., Tan, M., Tan, X., Tang, M., Tang, J., Timelthaler, G., Tomizuka, S., Trautwein, M., Tong, X., Uchifune, T., Walz, M.G., Wiegmann, B.M., Wilbrandt, J., Wipfler, B., Wong, T.K.F., Wu, Q., Wu, G., Xie, Y., Yang, S., Yang, Q., Yeates, D.K., Yoshizawa, K., Zhang, Q., Zhang, R., Zhang, W., Zhang, Yunhui, Zhao, J., Zhou, C., Zhou, L., Ziesmann, T., Zou, S., Li, Yingrui, Xu, X., Zhang, Yong, Yang, H., Wang, Jian, Wang, Jun, Kjer, K.M., Zhou, X., 2014. Phylogenomics resolves the timing and pattern of insect evolution. *Science* 346, 763–767.
- Mito, T., Kobayashi, C., Sarashina, I., Zhang, H., Shinahara, W., Miyawaki, K., Shinmyo, Y., Ohuchi, H., Noji, S., 2007. even-skipped has gap-like, pair-rule-like, and segmental functions in the cricket *Gryllus bimaculatus*, a basal, intermediate germ insect (Orthoptera). *Dev. Biol.* 303, 202–213.

- Mito, T., Shinmyo, Y., Kurita, K., Nakamura, T., Ohuchi, H., Noji, S., 2011. Ancestral functions of Delta/Notch signaling in the formation of body and leg segments in the cricket *Gryllus bimaculatus*. *Development* 138, 3823–3833.
- Miyawaki, K., Mito, T., Sarashina, I., Zhang, H., Shinmyo, Y., Ohuchi, H., Noji, S., 2004. Involvement of Wingless/Armadillo signaling in the posterior sequential segmentation in the cricket, *Gryllus bimaculatus* (Orthoptera), as revealed by RNAi analysis. *Mech. Dev.* 121, 119–130.
- Morelli, L.G., Ares, S., Herrgen, L., Schröter, C., Jülicher, F., Oates, A.C., 2009. Delayed coupling theory of vertebrate segmentation. *HFSP J.* 3, 55–66.
- Murgan, S., Kari, W., Rothbacher, U., Iché-Torres, M., Méléneç, P., Hobert, O., Bertrand, V., 2015. Atypical Transcriptional Activation by TCF via a Zic Transcription Factor in *C. elegans* Neuronal Precursors. *Dev. Cell* 33, 737–745.
- Nakamoto, A., Hester, S.D., Constantinou, S.J., Blaine, W.G., Tewksbury, A.B., Matei, M.T., Nagy, L.M., Williams, T.A., 2015. Changing cell behaviours during beetle embryogenesis correlates with slowing of segmentation. *Nat. Commun.* 6, 6635.
- Nakao, H., 2018. A *Bombyx* homolog of *ovo* is a segmentation gene that acts downstream of *Bm-wnt1* (*Bombyx wnt1* homolog). *Gene Expr. Patterns* 27, 1–7.
- Nakao, H., 2015. Analyses of interactions among pair-rule genes and the gap gene *Krüppel* in *Bombyx* segmentation. *Dev. Biol.* 405, 149–157.
- Nakao, H., 2010. Characterization of *Bombyx* embryo segmentation process: expression profiles of engrailed, even-skipped, caudal, and *wnt1*/wingless homologues. *J. Exp. Zool. B Mol. Dev. Evol.* 314B, 224–231.
- Nasiadka, A., Dietrich, B.H., Krause, H.M., 2002. Anterior-posterior patterning in the *Drosophila* embryo, in: *Advances in Developmental Biology and Biochemistry, Gene Expression at the Beginning of Animal Development*. Elsevier, pp. 155–204.
- Nüsslein-Volhard, C., Wieschaus, E., 1980. Mutations affecting segment number and polarity in *Drosophila*. *Nature* 287, 795.
- Oates, A.C., Morelli, L.G., Ares, S., 2012. Patterning embryos with oscillations: structure, function and dynamics of the vertebrate segmentation clock. *Development* 139, 625–639.
- Oberhofer, G., Grossmann, D., Siemanowski, J.L., Beissbarth, T., Bucher, G., 2014. Wnt/ β -catenin signaling integrates patterning and metabolism of the insect growth zone. *Development* 141, 4740–4750.
- Oda, H., Nishimura, O., Hirao, Y., Tarui, H., Agata, K., Akiyama-Oda, Y., 2007. Progressive activation of Delta-Notch signaling from around the blastopore is required to set up a functional caudal lobe in the spider *Achaearanea tepidariorum*. *Dev. Camb. Engl.* 134, 2195–2205.
- Paese, C.L.B., Schoenauer, A., Leite, D.J., Russell, S., McGregor, A.P., 2018. A *SoxB* gene acts as an anterior gap gene and regulates posterior segment addition in a spider. *eLife* 7, e37567.
- Paré, A.C., Vichas, A., Fincher, C.T., Mirman, Z., Farrell, D.L., Mainieri, A., Zallen, J.A., 2014. A positional Toll receptor code directs convergent extension in *Drosophila*. *Nature* 515, 523–527.
- Patel, N.H., Condrón, B.G., Zinn, K., 1994. Pair-rule expression patterns of even-skipped are found in both short- and long-germ beetles. *Nature* 367, 429.
- Pechmann, M., Khadjeh, S., Turetzek, N., McGregor, A.P., Damen, W.G.M., Prpic, N.-M., 2011. Novel Function of *Distal-less* as a Gap Gene during Spider Segmentation. *PLOS Genet.* 7, e1002342.
- Peel, A., Akam, M., 2003. Evolution of segmentation: rolling back the clock. *Curr. Biol. CB* 13, R708–710.
- Peel, A.D., Chipman, A.D., Akam, M., 2005. Arthropod segmentation: beyond the *Drosophila* paradigm. *Nat. Rev. Genet.* 6, 905–916.
- Pick, L., 2016. Hox genes, evo-devo, and the case of the *ftz* gene. *Chromosoma* 125, 535–551.
- Posnien, N., Schinko, J.B., Kittelmann, S., Bucher, G., 2010. Genetics, development and composition of the insect head – A beetle’s view. *Arthropod Struct. Dev., Evolution of Patterning Mechanisms* 39, 399–410.

- Pourebahim, R., Houtmeyers, R., Ghogomu, S., Janssens, S., Thelie, A., Tran, H.T., Langenberg, T., Vleminckx, K., Bellefroid, E., Cassiman, J.-J., Tejpar, S., 2011. Transcription Factor Zic2 Inhibits Wnt/ β -Catenin Protein Signaling. *J. Biol. Chem.* 286, 37732–37740.
- Pueyo, J.I., Lanfear, R., Couso, J.P., 2008. Ancestral Notch-mediated segmentation revealed in the cockroach *Periplaneta americana*. *Proc. Natl. Acad. Sci.* 105, 16614–16619.
- Rohr, K.B., Tautz, D., Sander, K., 1999. Segmentation gene expression in the mothmidge *Clogmia albipunctata* (Diptera, psychodidae) and other primitive dipterans. *Dev. Genes Evol.* 209, 145–154.
- Rosenberg, M.I., Brent, A.E., Payre, F., Desplan, C., 2014. Dual mode of embryonic development is highlighted by expression and function of *Nasonia* pair-rule genes. *eLife* 3.
- Rothschild, J.B., Tsimiklis, P., Siggia, E.D., François, P., 2016. Predicting Ancestral Segmentation Phenotypes from *Drosophila* to *Anopheles* Using In Silico Evolution. *PLOS Genet.* 12, e1006052.
- Salazar-Ciudad, I., Newman, S.A., Solé, R.V., 2001. Phenotypic and dynamical transitions in model genetic networks I. Emergence of patterns and genotype-phenotype relationships. *Evol. Dev.* 3, 84–94.
- Samee, Md.A.H., Lydiard-Martin, T., Biette, K.M., Vincent, B.J., Bragdon, M.D., Eckenrode, K.B., Wunderlich, Z., Estrada, J., Sinha, S., DePace, A.H., 2017. Quantitative Measurement and Thermodynamic Modeling of Fused Enhancers Support a Two-Tiered Mechanism for Interpreting Regulatory DNA. *Cell Rep.* 21, 236–245.
- Sander, K., 1976. Specification of the basic body pattern in insect embryogenesis. *Adv Insect Physiol* 12, 125–238.
- Sarrazin, A.F., Peel, A.D., Averof, M., 2012. A segmentation clock with two-segment periodicity in insects. *Science* 336, 338–341.
- Scholtz, G., 1992. Cell lineage studies in the crayfish *Cherax destructor* (Crustacea, Decapoda): germ band formation, segmentation and early neurogenesis. *Roux Arch. Dev Biol* 202, 36–48.
- Schönauer, A., Paese, C.L.B., Hilbrant, M., Leite, D.J., Schwager, E.E., Feitosa, N.M., Eibner, C., Damen, W.G.M., McGregor, A.P., 2016. The Wnt and Delta-Notch signalling pathways interact to direct pair-rule gene expression via caudal during segment addition in the spider *Parasteatoda tepidariorum*. *Dev. Camb. Engl.* 143, 2455–2463.
- Schoppmeier, M., Damen, W.G.M., 2005a. Expression of Pax group III genes suggests a single-segmental periodicity for opisthosomal segment patterning in the spider *Cupiennius salei*. *Evol. Dev.* 7, 160–169.
- Schoppmeier, M., Damen, W.G.M., 2005b. Suppressor of Hairless and Presenilin phenotypes imply involvement of canonical Notch-signalling in segmentation of the spider *Cupiennius salei*. *Dev. Biol.* 280, 211–224.
- Schroeder, M.D., Greer, C., Gaul, U., 2011. How to make stripes: deciphering the transition from non-periodic to periodic patterns in *Drosophila* segmentation. *Dev. Camb. Engl.* 138, 3067–3078.
- Schröter, C., Ares, S., Morelli, L.G., Isakova, A., Hens, K., Soroldoni, D., Gajewski, M., Jülicher, F., Maerkl, S.J., Deplancke, B., Oates, A.C., 2012. Topology and Dynamics of the Zebrafish Segmentation Clock Core Circuit. *PLOS Biol.* 10, e1001364.
- Schulz, C., Schröder, R., Hausdorf, B., Wolff, C., Tautz, D., 1998. A caudal homologue in the short germ band beetle *Tribolium* shows similarities to both, the *Drosophila* and the vertebrate caudal expression patterns. *Dev. Genes Evol.* 208, 283–289.
- Schwager, E., 2008. Segmentation of the spider *Achaearanea tepidariorum* investigated by gene expression and functional analysis of the gap gene hunchback (text.thesis.doctoral). Universität zu Köln.
- Schwager, E.E., Pechmann, M., Feitosa, N.M., McGregor, A.P., Damen, W.G.M., 2009. hunchback functions as a segmentation gene in the spider *Achaearanea tepidariorum*. *Curr. Biol. CB* 19, 1333–1340.

- Schwentner, M., Combosch, D.J., Nelson, J.P., Giribet, G., 2017. A Phylogenomic Solution to the Origin of Insects by Resolving Crustacean-Hexapod Relationships. *Curr. Biol.* 27, 1818-1824.e5.
- Sharpe, J., 2017. Computer modeling in developmental biology: growing today, essential tomorrow. *Development* 144, 4214–4225.
- Shinmyo, Y., Mito, T., Matsushita, T., Sarashina, I., Miyawaki, K., Ohuchi, H., Noji, S., 2005. caudal is required for gnathal and thoracic patterning and for posterior elongation in the intermediate-germband cricket *Gryllus bimaculatus*. *Mech. Dev.* 122, 231–239.
- Soroldoni, D., Jörg, D.J., Morelli, L.G., Richmond, D.L., Schindelin, J., Jülicher, F., Oates, A.C., 2014. Genetic oscillations. A Doppler effect in embryonic pattern formation. *Science* 345, 222–225.
- Stahi, R., Chipman, A.D., 2016. Blastoderm segmentation in *Oncopeltus fasciatus* and the evolution of insect segmentation mechanisms. *Proc. R. Soc. B Biol. Sci.* 283, 20161745.
- Steventon, B., Duarte, F., Lagadec, R., Mazan, S., Nicolas, J.-F., Hirsinger, E., 2016. Species-specific contribution of volumetric growth and tissue convergence to posterior body elongation in vertebrates. *Dev. Camb. Engl.* 143, 1732–1741.
- Stollewerk, A., Schoppmeier, M., Damen, W.G.M., 2003. Involvement of Notch and Delta genes in spider segmentation. *Nature* 423, 863–865.
- Sucena, É., Vanderberghe, K., Zhurov, V., Grbić, M., 2014. Reversion of developmental mode in insects: evolution from long germband to short germband in the polyembryonic wasp *Macrocentrus cingulum* Brischke. *Evol. Dev.* 16, 233–246.
- Surkova, S., Kosman, D., Kozlov, K., Manu, Myasnikova, E., Samsonova, A.A., Spirov, A., Vanario-Alonso, C.E., Samsonova, M., Reinitz, J., 2008. Characterization of the *Drosophila* segment determination morphome. *Dev. Biol.* 313, 844–862.
- Verd, B., Clark, E., Wotton, K.R., Janssens, H., Jiménez-Guri, E., Crombach, A., Jaeger, J., 2018. A damped oscillator imposes temporal order on posterior gap gene expression in *Drosophila*. *PLOS Biol.* 16, e2003174.
- Verd, B., Crombach, A., Jaeger, J., 2014. Classification of transient behaviours in a time-dependent toggle switch model. *BMC Syst. Biol.* 8, 43.
- Vroomans, R.M.A., Hogeweg, P., ten Tusscher, K.H.W.J., 2018. Around the clock: gradient shape and noise impact the evolution of oscillatory segmentation dynamics. *EvoDevo* 9, 24.
- Vroomans, R.M.A., Hogeweg, P., Ten Tusscher, K.H.W.J., 2016. In silico evo-devo: reconstructing stages in the evolution of animal segmentation. *EvoDevo* 7, 14.
- Williams, T., Blachuta, B., Hegna, T.A., Nagy, L.M., 2012. Decoupling elongation and segmentation: notch involvement in anostracan crustacean segmentation. *Evol. Dev.* 14, 372–382.
- Williams, T.A., Nagy, L.M., 2017. Linking gene regulation to cell behaviors in the posterior growth zone of sequentially segmenting arthropods. *Arthropod Struct. Dev.* 46, 380–394.
- Wilson, M.J., McKelvey, B.H., van der Heide, S., Dearden, P.K., 2010. Notch signaling does not regulate segmentation in the honeybee, *Apis mellifera*. *Dev. Genes Evol.* 220, 179–190.
- Wolff, C., Tinevez, J.-Y., Pietzsch, T., Stamatakis, E., Harich, B., Guignard, L., Preibisch, S., Shorte, S., Keller, P.J., Tomancak, P., Pavlopoulos, A., 2018. Multi-view light-sheet imaging and tracking with the MaMuT software reveals the cell lineage of a direct developing arthropod limb. *eLife* 7, e34410.
- Xiang, J., Reding, K., Heffer, A., Pick, L., 2017. Conservation and variation in pair-rule gene expression and function in the intermediate-germ beetle *Dermestes maculatus*. *Dev. Camb. Engl.* 144, 4625–4636.
- Xu, J., Gridley, T., 2012. Notch signalling during oogenesis in *Drosophila*. *Genet. Res. Int.* 2012, Article ID 648207.
- Zheng, L., Michelson, Y., Freger, V., Avraham, Z., Venken, K.J.T., Bellen, H.J., Justice, M.J., Wides, R., 2011. *Drosophila* Ten-m and filamin affect motor neuron growth cone guidance. *PLoS One* 6, e22956.

Zhu, X., Rudolf, H., Healey, L., François, P., Brown, S.J., Klingler, M., El-Sherif, E., 2017. Speed regulation of genetic cascades allows for evolvability in the body plan specification of insects. *Proc. Natl. Acad. Sci.* 201702478.

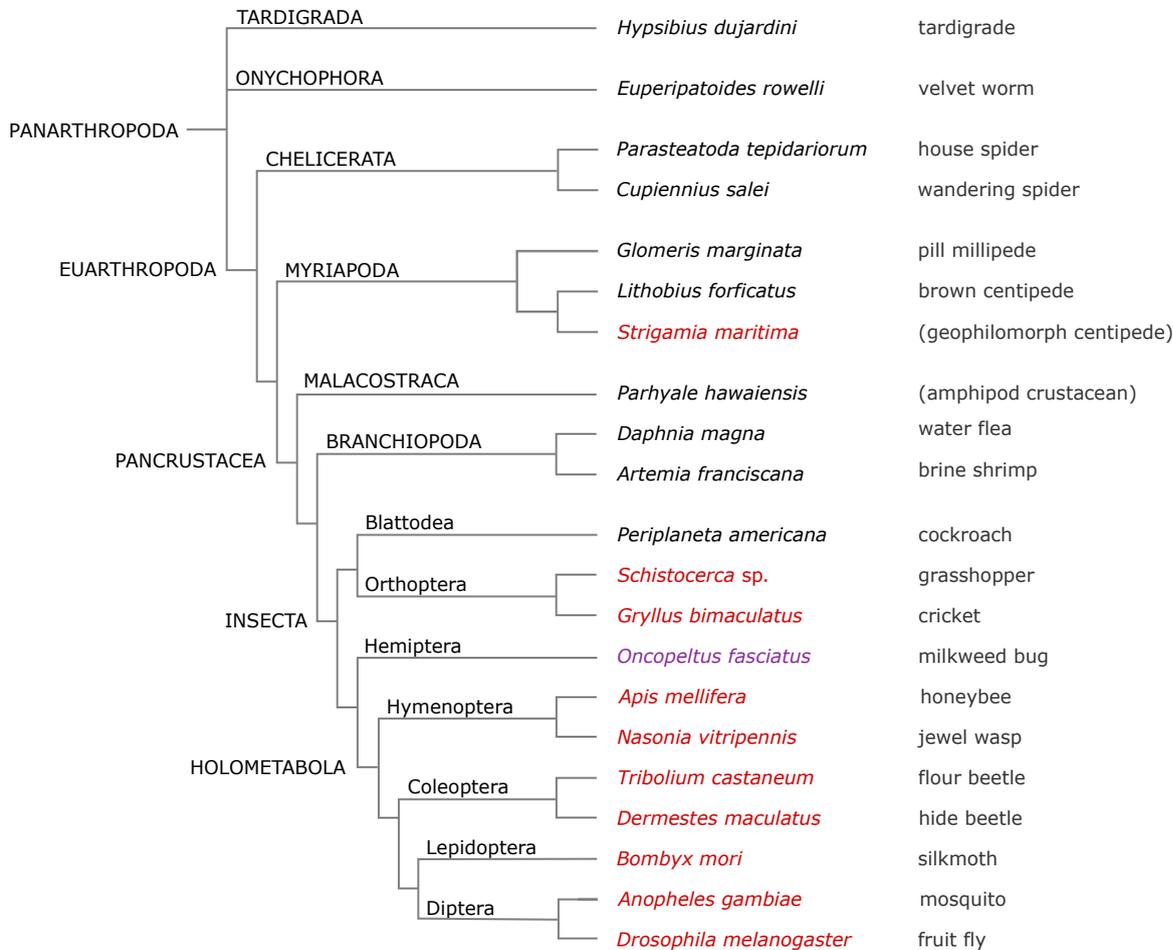
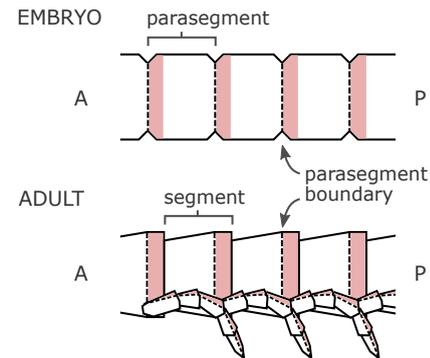
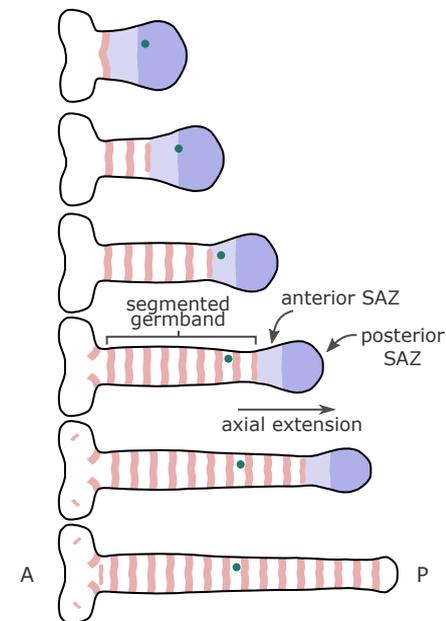
Fig. 1. Overview of arthropod segmentation. (A) Phylogenetic tree of notable arthropod model species (based on Misof et al., 2014; Schwentner et al., 2017). Red text indicates species known to use pair-rule patterning; the status of *Oncopeltus* is currently unclear. Branch lengths not to scale. (B) Diagram showing the relationship between parasegments and segments. Pink=*engrailed* expression; 'A'=anterior; 'P'=posterior. (C) Schematic time series of an arthropod embryo undergoing sequential segmentation. *engrailed* stripes (pink) emerge sequentially from a retracting segment addition zone (SAZ, blue) as the germband extends posteriorly. Green dots mark the progress of a specific individual cell that starts in the posterior SAZ (dark blue), passes through the anterior SAZ (light blue), and ends up in the segmented germband.

Fig. 2. Within cell, between-cell, and tissue-level aspects of the arthropod segmentation clock. (A) Pair-rule gene oscillations may be driven by a cross-regulatory feedback loop within cells. The two hypothetical topologies shown (left) would be capable of driving similar, although not identical, cycles of *eve*, *runt*, and *odd* expression within cells (right). In *Tribolium*, the relative expression patterns of Eve protein, *runt* transcript and *odd* transcript resemble the predicted expression of model 2, rather than model 1 (see Supporting Information from Choe et al., 2006). Expression predictions assume Boolean regulatory logic and equal time delays for protein synthesis and protein decay (Clark, 2017). (B) Notch signalling might indirectly synchronise intracellular oscillations of *eve*, *runt*, and *odd* across cells, by acting through *hairy*. This figure shows a hypothetical regulatory network, which synthesises genetic interactions documented from various different arthropod species (Clark, 2017; Eriksson et al., 2013; Nakao, 2015; Pueyo et al., 2008; Stollewerk et al., 2003). The left half of the network ("oscillator 1") would synchronise oscillations of *hairy* across neighbouring cells, by coupling *hairy* expression to Notch signalling. The oscillations of *hairy* would then influence the phase of the genetic ring oscillator that forms the right hand of the network ("oscillator 2"), by repressing some of its component genes. (C) Genes such as *Wnt*, *caudal*, *Dichaete*, and *opa* have distinct expression patterns within the SAZ, which correlate with different phases of segment patterning. 'A'=anterior; 'P'=posterior. (Based on *Tribolium* data from Clark and Peel, 2018.) Note that *Wnt* and *opa* have segment-polarity patterns in the segmented germband. *caudal* and/or *Dichaete* stripes (not shown) are seen in the anterior SAZ of some species, indicating that the clock feeds back on their expression (Chipman et al., 2004; Clark and Peel, 2018).

Fig 3. Resolving the segment pattern: from oscillations to stable stripes. (A) Comparison of patterning using a single-gene oscillator versus patterning using a three-gene oscillator. With a single-gene oscillator, different cell fates are determined by different expression levels of the oscillator. The output is sensitive to noise in the amplitude of, or measuring of, the signal, and must be palindromic, because the input signal is symmetrical. With a three-gene oscillator, different cell fates can be determined by different combinations of input factors. The output is more robust to noise, and has an inherent polarity. (B) Comparison of the segment-polarity fate readout for clocks with single-segment or double-segment periodicity. Parasegment boundaries (red lines) form wherever a cell with an anterior segment-polarity fate ('A'; i.e. expressing *engrailed*) abuts a cell with a posterior segment-polarity fate ('P'; i.e. expressing *slp* and *wg*). A third cell fate (light grey; e.g. *odd* in *Drosophila*) prevents ectopic boundaries. Note that species with double-segment periodicity have a different, more complex mapping between the input pattern (pair-rule gene expression) and the output pattern (segment-polarity gene expression). (C) Dynamic model for the patterning of *prd* and *slp* in *Drosophila*: the staggered expression boundaries of *prd* and *slp* are caused by the Eve stripes shifting anteriorly across the tissue over time. The posterior border of the *prd* stripe is patterned at timepoint t_1 (Eve expression shown by dotted line), while the posterior border of the *slp* stripe is patterned a short while later, at timepoint t_2 (Eve expression shown by solid line). (Based on Clark, 2017). (D) The staggered pattern of pair-rule gene expression comprises a positional code, which specifies narrow stripes of segment-polarity gene expression. The regulatory logic (top) and resulting expression pattern (bottom) of *Drosophila engrailed* (*en*) is shown as an example. Note that odd-numbered and even-numbered *en* stripes are regulated differently. (Based on Jaynes and Fujioka, 2004).

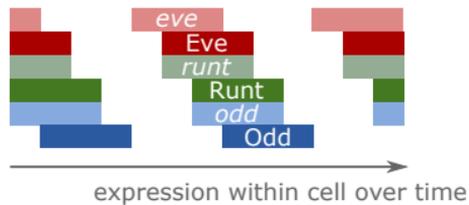
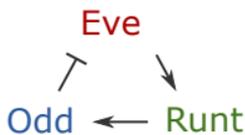
Fig. 4. Reconciling sequential and simultaneous segmentation. (A) Structural overview of arthropod segmentation gene networks. The core of the system (yellow box) is relatively conserved across species. In sequential segmentation, spatial information is provided by the timing factor network, which generates a wavefront. Gap genes do not play a major role in segment patterning, although late gap gene expression may be important for “shutting down” the SAZ, by repressing timing factors that maintain it (dashed blue arrow). In simultaneous segmentation, timing factors only provide temporal information. Spatial information is usually provided by a novel anterior patterning centre (i.e. a morphogen gradient such as Bicoid (Liu et al., 2018; McGregor, 2005)), which regulates gap gene expression. Gap genes pass this information to the primary pair-rule genes, through newly-evolved regulatory elements (SSEs). (B) Spatial patterning in *Drosophila* is inherently dynamic. (1) Regulatory interactions between gap genes cause gap domains to shift anteriorly across the blastoderm over time. (2) Stripes of pair-rule gene expression regulated by gap inputs also shift anteriorly. (3) Regulatory interactions between the pair-rule genes convert these shifts into a staggered pattern of expression overlaps across the pair-rule repeat. Note that each panel zooms in on a smaller region of the AP axis. (C) Schematic kymographs (i.e., plots of how gene expression along the AP axis changes over time) comparing the key spatiotemporal features of sequential and simultaneous segmentation. In sequential segmentation, timing factor expression (blue) matures from anterior to posterior across the tissue, producing a wavefront (diagonal line). Periodicity is generated by sustained oscillations (note how *even-skipped* turns on and off over time within the blue zone). The wavefront converts the oscillations into a stable segment-polarity pattern. In simultaneous segmentation, there is little spatial regulation of timing factor expression across the tissue, and pair-rule stripes are present from the start. Embryo diagrams depict the specific timepoints they line up with on the kymographs (*eve* expression is not shown). Patterning has double-segment periodicity. Note the different scales of the two time axes.

Fig 5. The evolution of simultaneous segmentation involves a gradual replacement of the segmentation clock by SSEs. (A) Clock enhancers (potentially homologous to zebra elements) and SSEs both drive stripes that shift anteriorly over time. SSEs can therefore gradually assume regulatory control over particular clock-driven stripes, without disrupting downstream patterning. (B) (1) Simultaneous patterning is likely to evolve stepwise along the AP axis, via the acquisition over evolutionary time of new SSEs that control expression in increasingly posterior stripes. Embryo diagrams assume a segmentation clock with double-segment periodicity. (2) Simultaneous patterning is likely to evolve stepwise within each pair-rule gene expression repeat, as more of the primary pair-rule genes evolve their own SSEs. Additional SSEs reduce the time required to organise pair-rule gene expression across the repeat. (D) Changes in gap gene expression can be sufficient to generate additional SSE-driven stripes, without accompanying changes in cis-regulatory logic. In *Drosophila* (right panel), SSEs such as *eve 3+7* and *eve 4+6* each drive a pair of stripes. The current situation likely evolved from a simpler scenario (left panel), in which the same enhancers drive expression in only one stripe each. Hb=Hunchback; Kr=Krüppel; Kni=Knirps; Gt=Giant. Note that *eve 3+7* and *eve 4+6* are both repressed by Kni and Hb, but with different relative strengths, represented by different arrow thicknesses (Samee et al., 2017). Diagrams are colour-coded such that transcription factor names (top) have the same colour as their corresponding expression domain(s) (below).

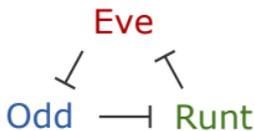
A**B****C**

A *eve*, *runt*, and *odd* might form a genetic ring oscillator

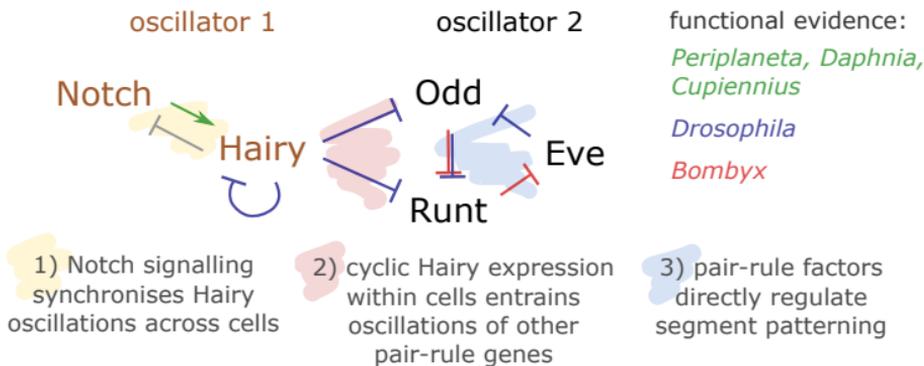
1) activation-based model (Choe et al 2006)



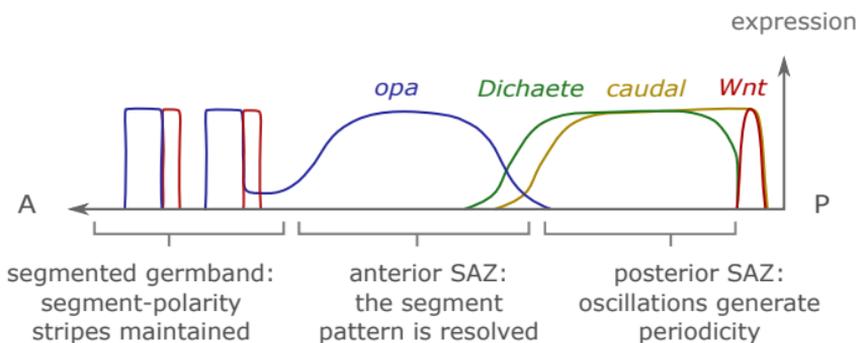
2) repression-based model

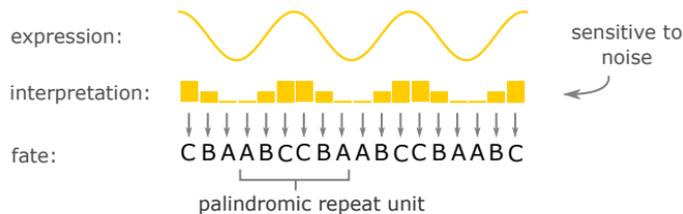
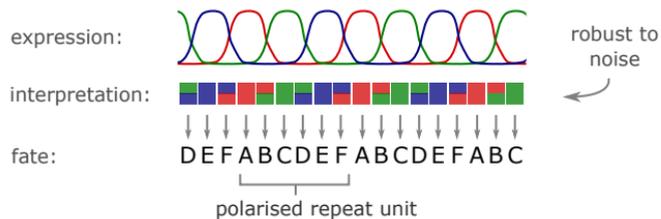
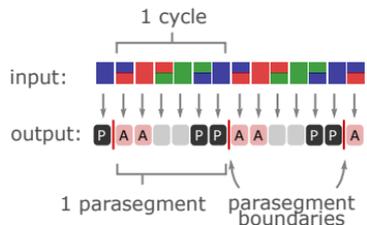


B hypothesis: *hairy* links intercellular and intracellular oscillations

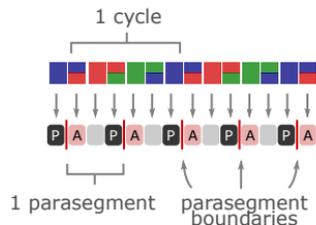
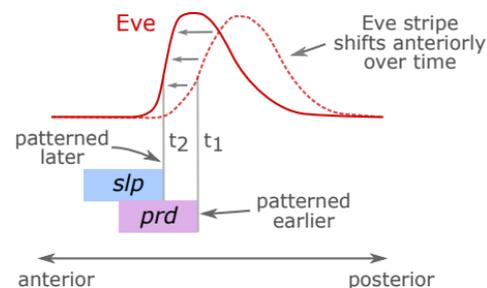


C "timing factors" coordinate segment patterning across the SAZ

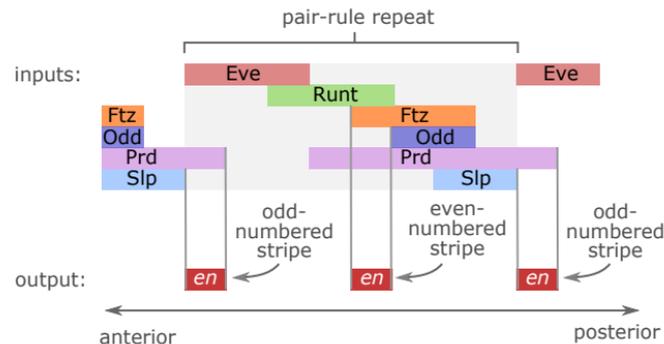
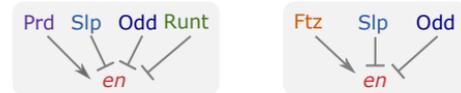


A single-gene oscillator:**three-gene oscillator:****B** single-segment periodicity:

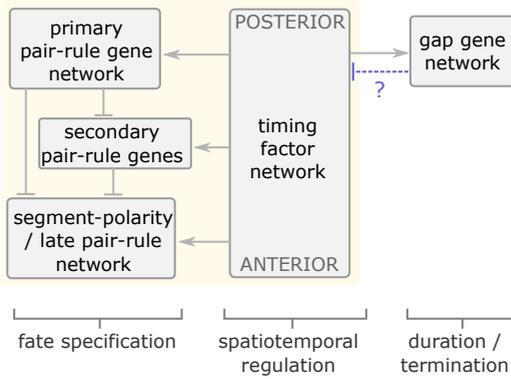
double-segment periodicity:

**C** dynamic model for the patterning of *prd* and *slp***D** segment-polarity genes are patterned by a "combinatorial code" of pair-rule gene expression

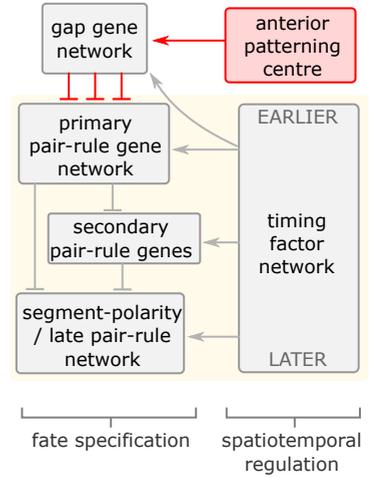
control logic: odd-numbered stripes even-numbered stripes



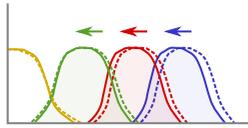
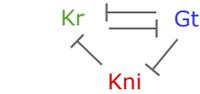
A sequential segmentation



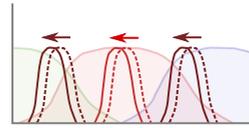
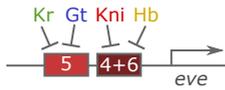
simultaneous segmentation



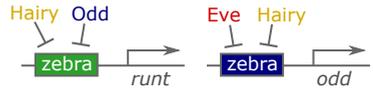
B 1) cross-regulation causes gap expression shifts



2) gap shifts cause SSE-driven stripes to shift

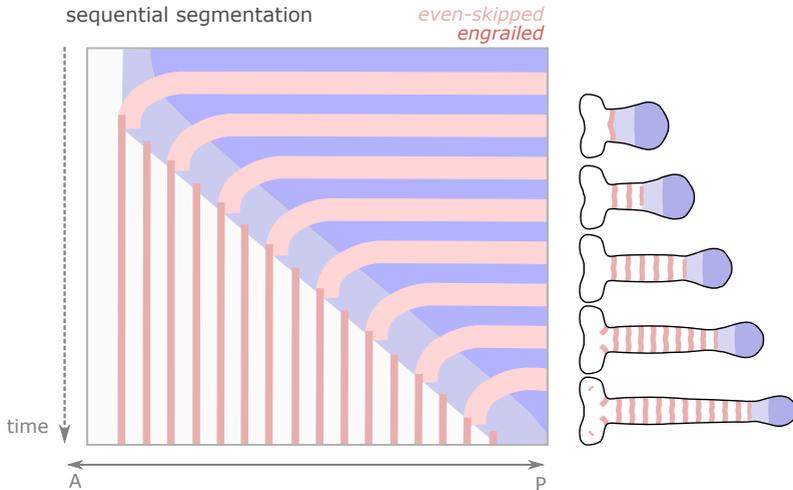


3) shifts plus cross-repression organise pair-rule pattern

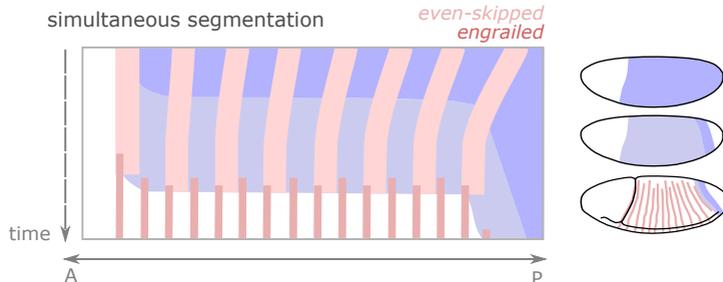


unstable but functionally important overlaps

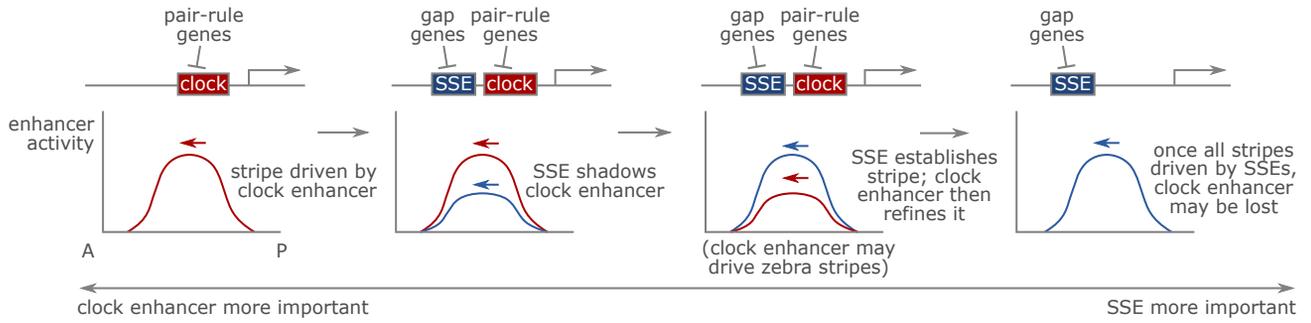
C sequential segmentation



simultaneous segmentation

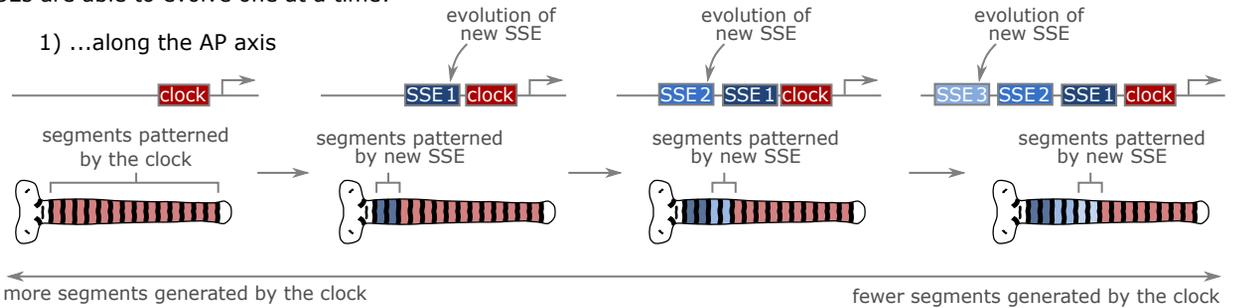


A each SSE can take over from the clock gradually

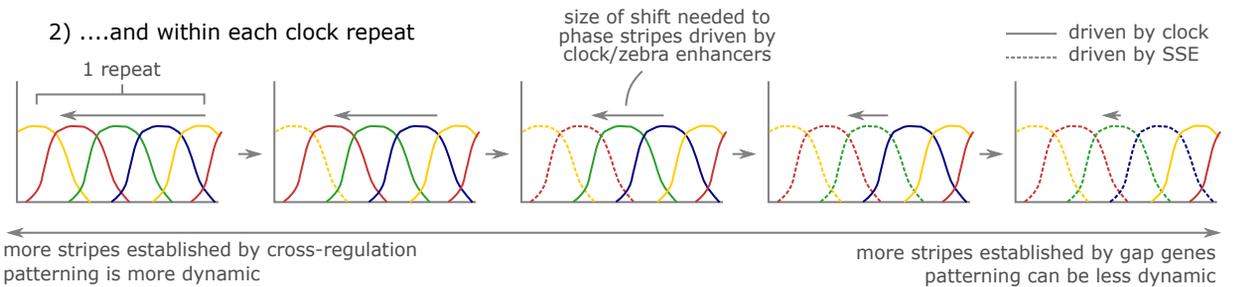


B SSEs are able to evolve one at a time:

1) ...along the AP axis



2)and within each clock repeat



C existing SSEs can be recruited to drive additional stripes

