

## S1 Appendix: Explanation of selected ordinal prediction models for CPM and eCPM

### Multinomial logistic regression (MNLr)

CPM<sub>MNLr</sub> and eCPM<sub>MNLr</sub> were implemented using the 'MNLogit' class from the 'statsmodels' module (dev. v0.14.0) [1] in Python (v3.7.6). The GOSE score of 1 (death) was designated as the reference label, and, for each other GOSE score, a separate logistic model was trained to regress the logit of the ratio of the probability of that score to the reference score from a linear combination of the predictors. The logit outputs of each model feed into a softmax function, after which cumulative sums would determine the probability at each threshold. Model weights for MNLr were optimised using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm [2] to maximize conditional likelihood.

### Proportional odds (i.e., ordinal) logistic regression (POLr)

CPM<sub>POLr</sub> and eCPM<sub>POLr</sub> were implemented using the 'OrderedModel' class from the 'statsmodels' module in Python. The model maps GOSE scores to a latent, logit space where consecutive GOSE scores are separated by thresholds. Thus, the model trains only one set of linear predictor weights, but a separate intercept for each threshold. Model weights for POLr were optimised using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm [2] to maximize conditional likelihood.

### Class-weighted feedforward neural network with a multinomial output layer (DeepMN)

CPM<sub>DeepMN</sub> and eCPM<sub>DeepMN</sub> were implemented using the 'PyTorch' (v1.10.0) [3] module in Python. The network architecture of DeepMN included a hyperparametric number of dense hidden layers (either 1, 2, 3, 4, 5, or 6), each containing a hyperparametric number of nodes (either 128, 256, or 512) with a rectified linear unit (ReLU) activation function and a hyperparametric percentage (either 0% or 20%) dropout during training. The output layer of DeepMN was a softmax layer of 7 nodes, from which probabilities at each GOSE are calculated with cumulative sums (**Fig 1A**). DeepMN was optimised using the Adam algorithm ( $\gamma$  [learning rate] = 0.001,  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ ) [4] with categorical cross-entropy loss. In the loss function, classes were weighted inversely proportional to the frequency of each GOSE score in the training set to counter class imbalance.

### Class-weighted feedforward neural network with an ordinal output layer (DeepOR)

CPM<sub>DeepOR</sub> and eCPM<sub>DeepOR</sub> were implemented using the 'PyTorch' (v1.10.0) [3] module in Python. The network architecture of DeepMN included a hyperparametric number of

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dense hidden layers (either 1, 2, 3, 4, 5, or 6), each containing a hyperparametric number of nodes (either 128, 256, or 512) with a rectified linear unit (ReLU) activation function and a hyperparametric percentage (either 0% or 20%) dropout during training. The output layer of DeepOR was a sigmoid layer of 6 nodes, where each node represented the binomial probability of the outcome being greater than a certain threshold, and each node is constrained to be less than or equal to lower-threshold nodes with a negative ReLU transformation (**Fig 1A**). DeepOR was optimised using the Adam algorithm ( $\gamma$  [learning rate] = 0.001,  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ ) with binary cross-entropy loss. In the loss function, classes were weighted inversely proportional to the frequency of each GOSE score in the training set to counter class imbalance.

| CPM or eCPM | Description  | Hyperparameters     |                    |           | Total number of configurations |
|-------------|--|---------------------|--------------------|-----------|--------------------------------|
|             |  | Hidden layers       | Neurons per layer* | Dropout   |                                |
| MNLR        | Multinomial logistic regression  |                     |                    |           | 1                              |
| POLR        | Proportional odds (i.e., ordinal) logistic regression  |                     |                    |           | 1                              |
| DeepMN      | Class-weighted feedforward neural network with a multinomial (i.e., softmax) output layer                | 1, 2, 3, 4, 5, or 6 | 128, 256, or 512   | 0% or 20% | 2184                           |
| DeepOR      | Class-weighted feedforward neural network with an ordinal (i.e., sigmoid at each threshold) output layer | 1, 2, 3, 4, 5, or 6 | 128, 256, or 512   | 0% or 20% | 2184                           |

\*Different hidden layers may have distinct numbers of neurons.

## References

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