

31 gain was greater in the fine sand than in the coarse sand, as the void size in the latter was
32 significantly larger compared to the calcium carbonate crystals' size, resulting in precipitation
33 on less effective locations, away from contacts between particles. The strengths and porosities
34 obtained for the two sands in this work fall within ranges reported in the literature for natural
35 soft rocks, demonstrating the MICP technique is able to achieve realistic properties and may
36 be used to produce a full range of properties by varying the grain sizes, and possibly the width
37 of the particle size distribution.

38 **KEYWORDS**

39 Granular rocks, biocementation, MICP, grain size, uniformity, efficiency, artificial rock

40 **LIST OF SYMBOLS**

41 UCS Unconfined compressive strength
42 MICP Microbially induced carbonate precipitation
43 OD Optical density
44 CS Cementation solution
45 BS Bacteria solution
46 D_{50} Mean particle size
47 LNB Liquid nutrient broth
48 n Porosity
49 I_s Point load index
50 PSD Particle size distribution

51 **1. INTRODUCTION**

52 The term soft sandstone is used in reference to poorly consolidated weakly cemented
53 sandstones, representing a transitional material between soils and fully aggregated rocks, and

54 sharing characteristics and behavior of both (Sitar et al. 1980; Collins and Sitar 2009,
55 Nakagawa and Myer 2001). Sandstones represent the host rock for a large portion of active
56 aquifers and oil and gas reservoirs because their high porosity both enhances storage and
57 facilitates extraction. The transitional nature of sandstones, in particular, presents some
58 challenges to the safety of extraction operations and the mechanical response of these materials
59 under a variety of conditions is still poorly understood. Unfortunately, coring of soft sandstones
60 tends to destroy cementation resulting in poor recoveries, so that sufficient quantities of high-
61 quality samples for laboratory testing are both difficult to obtain and expensive. As an
62 alternative, synthetic rock specimens can provide virtually limitless quantities and
63 customisable characteristics, allowing relevant structural parameters to be varied
64 independently, and hence isolating their effects (Saidi et al. 2005). Rock specimen reproduction
65 has received great attention in the literature (Wygall 1963; Maccarini 1987; Nakagawa and
66 Myer 2001; Ismail et al. 2002; Saidi et al. 2003; Vogler et al. 2017) due to the increasing need
67 for understanding the mechanical behavior of various rocks.

68 Soft sandstones are characterized by low unconfined compressive strength, poor core integrity,
69 core wash-out during laboratory tests, and stress-dependent porosity and permeability. Studies
70 report unconfined compression strength (UCS) values ranging from 100-3500 kPa (Sitar et al.
71 1980; Shafii Rad and Clough 1982; Dobereiner 1984; Ispas et al. 2012; Kanji 2014; Pradhan
72 et al. 2014; Sattler and Paraskevopoulou 2019). Another critical property dominating the
73 behaviour of these materials is porosity, generally ranging from 0.2 to 0.4, much higher than
74 in competent rocks (Heath 1965; Sitar et al. 1980; Krishnan et al. 1998; Suarez-Rivera et al.
75 2002; Collins and Sitar 2009). As the value of porosity is determined by simple tests, it is often
76 used to derive strength or permeability of the material from empirical relationships (Fjar et al.
77 2008). Any method that aims at reproducing salient properties of soft sandstones needs to
78 reproduce the correct combination of strength and porosity.

79 Collins and Sitar (2009) demonstrated that the behaviour of most cemented sandstones appears
80 to be similar regardless of the particular cementing agent, but the degree of cementation is
81 closely linked to the mechanical properties. This study focuses on carbonate cemented
82 sandstones.

83 Microbially induced carbonate precipitation (MICP) can be applied to produce a range of weak
84 carbonate sandstone-like materials from a base sand through a bio-process that builds up
85 calcium carbonate cementation around the particles. MICP is potentially an excellent tool to
86 develop artificially carbonate cemented sandstone with consistent characteristics that can be
87 customized by changing the amount of carbonate cementing agent. The main objectives of this
88 study were: (1) to assess reliability and repeatability of the MICP process used to generate
89 synthetic specimens with varying controllable properties from materials with different particle
90 size distributions and (2) to determine whether the resulting properties, primarily strength and
91 porosity, would sufficiently resemble weakly carbonate cemented sandstones to be used as a
92 substitute in a subsequent laboratory investigation of mechanical response under more complex
93 loading conditions.

94 **2. BACKGROUND**

95 MICP has been extensively studied for a number of geotechnical applications generally aimed
96 at improving soil properties and reducing hazards such as: liquefaction control (Montoya et al.
97 2013; Montoya and DeJong, 2015), mitigation of internal and surface erosion (Jiang et al. 2017;
98 Cheng et al. 2014; van Paassen et al. 2010), slope stabilisation (DeJong et al. 2010; DeJong et
99 al. 2013), structural stability (Umar et al. 2016; Bella et al. 2017; Konstantinou and Biscontin
100 2020; DeJong et al. 2011), bio-remediation (Torres-Aravena et al. 2018; Li et al., 2013;
101 Mugwar and Harbottle 2016) and even in self-healing of soils, bioconcrete or cracks (Harbottle
102 et al. 2014; Montoya and Dejong 2013; Castro-Alonso et al. 2019; Ersan et al. 2016).

103 The advantage of the method over the conventional techniques is the mitigation of geotechnical

104 engineering problems in a non-disruptive manner. It can be easily applied at ambient
105 temperatures over a large area, even under buildings, without disturbing them. MICP offers a
106 substantial increase in strength, stiffness, and dilative behaviour, while retaining soil's
107 permeability to some extent.

108 In MICP, bacteria are first introduced to the medium and then a cementation solution consisting
109 of urea and a calcium source is supplied in the form of injections (Whiffin 2004; DeJong et al.
110 2006). The properties of the treated products, in particular strength and stiffness, depend on
111 both the grain characteristics of the base material (particle roughness, shape, size) and the
112 cement distribution and morphology within the medium (amount, crystal shape and size, and
113 location of calcium carbonate) (DeJong et al. 2010; Mortensen et al. 2011; Al Qabany et al.
114 2012; Al Qabany and Soga 2013; Zhao et al. 2014; Cheng et al. 2017; Mujah et al. 2017).
115 Although numerous studies have been conducted to derive protocols for effective bio-
116 cementation by altering components of the MICP recipe (Whiffin et al. 2007; Al Qabany et al.
117 2012; Martinez et al. 2013; Cheng and Cord-Ruwisch 2014; Dawoud et al. 2014; Dawoud
118 2015; Feng and Montoya 2015; Cui et al. 2017; Jiang et al. 2017; Mujah et al. 2017; Cheng et
119 al. 2019), cementation in the specimens has not always been uniform. This is an important
120 consideration when using the method for artificial specimens' preparation as non-uniform
121 samples invalidate any further testing results.

122 The focus of the majority of previous studies was the identification of the optimum protocol
123 parameters. The granular material used was typically a single type of poorly graded fine sand
124 with mean particle diameters of 0.15-0.7 mm (Zhao et al. 2014; Dawoud 2015; Feng and
125 Montoya 2015; Lin et al. 2015; Cheng et al. 2017; Cui et al. 2017; Dadda et al. 2017, 2019).
126 Coarse sand was very rarely selected for bio-cementation (Mahawish et al. 2018) due to size
127 incompatibility between the microbes and the grain sizes according to the criterion proposed

128 by Mitchell and Santamarina (2005) (Fig. 1).

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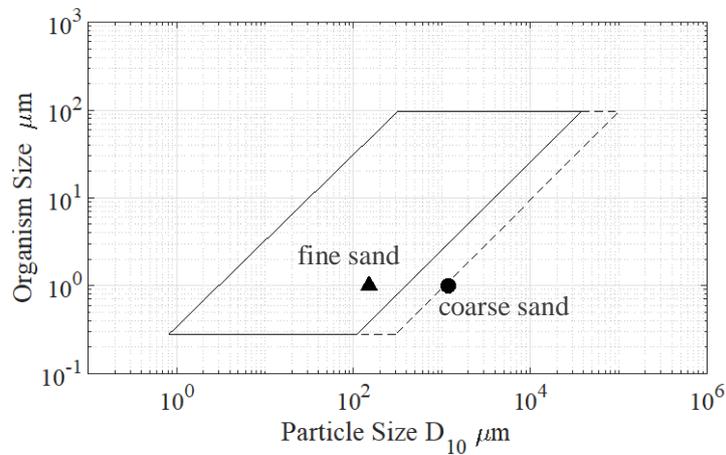
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136 **Fig. 1.** The bounded region indicates the range of soil sizes that can be treated with
137 bioclogging (after Mitchell and Santamarina, 2005)

138 Although it is generally recognised that the medium's intrinsic properties (grain size,
139 roughness, particle's shape) affect the effectiveness of the process, the understanding of these
140 effects remains limited. Rebata-Landa (2007) investigated the efficiency of MICP using
141 different soils with varying grain sizes and porosity. In very fine soils, the bacterial activity
142 (ability to metabolise and generate biofilms) was restricted by the small space available in the
143 pores resulting in low calcium carbonate concentration. In coarse soils, the low cementation
144 was attributed to the formation of a thin distributed layer of calcium carbonate, which was not
145 sufficient to increase the strength of the specimens (Rebata-Landa 2007).

146 3. MATERIALS AND METHODS

147 The MICP procedure (bacterial density, urease activity, chemical concentration, injection times
148 etc.) was identical for all specimens and all types of sand in order to minimise variability from
149 bio-chemical processes, while the amount of cementation was varied by changing the amount
150 of cementation solution injected into the medium. The key to obtaining uniform specimens of
151 repeatable quality is to ensure that the bacteria and cementation solution are permeating the
152 base material uniformly and the reactions occur at a rate that is compatible with the velocity of

153 the flow. Therefore, the effectiveness of the MICP process is controlled by chemical efficiency,
154 which in turn depends on the retention times, the injecting method, the chemical concentration,
155 and the optical density of the bacteria solution.

156 **3.1. MICP Procedure**

157 The bacterium *Sporosarcina pasteurii* was used, as its urease-synthesis behaviour is well-
158 defined, and its activity has been proven to be higher than other species (Whiffin 2004). Batch
159 experiments were conducted under aerobic conditions and in a sterile environment. The
160 growing medium consisted of 20 g/L yeast extract, 10 g/L ammonium sulphate, 20 g/L agar,
161 and 0.13 M tris buffer (base). After 24 h of incubation at 30 °C, the culture was harvested and
162 stored at 4 °C. Bacterial colonies were introduced into liquid nutrient broth without agar (LNB),
163 placed in a shaking incubator for additional 24 h to form the bacterial solution (BS), which was
164 then stored at 4 °C. The optical density of the BS measured at a wavelength of 600 nm, OD₆₀₀,
165 was between 1.5 and 2.0.

166 The bacterial urease activity for each specimen was measured with a conductivity assay
167 (Whiffin, 2004) on a bacteria solution diluted to an optical density of 1.0 for the purpose of
168 comparison with other works. The measured urease activity averaged across all tests, 0.8 (mM
169 urea/h)/OD, was lower compared to most previous research (Whiffin et al. 2007; Cheng et al.
170 2013, 2017). However, it was sufficient to induce reactions in previous works (Jiang and Soga
171 2017) and was found to be a key factor in obtaining uniform specimens (Konstantinou, 2020).

172 The cementation solution (CS) used in this study comprised 0.375 M urea, 0.25 M calcium
173 chloride (CaCl₂), and 3 g/L nutrient broth. This recipe was in the low range of concentrations
174 among those reported in literature and applied longer retention times than most previous works,
175 although it was consistent with several studies showing effective MICP treatment (DeJong et
176 al. 2006).

177 **3.2. Sample preparation**

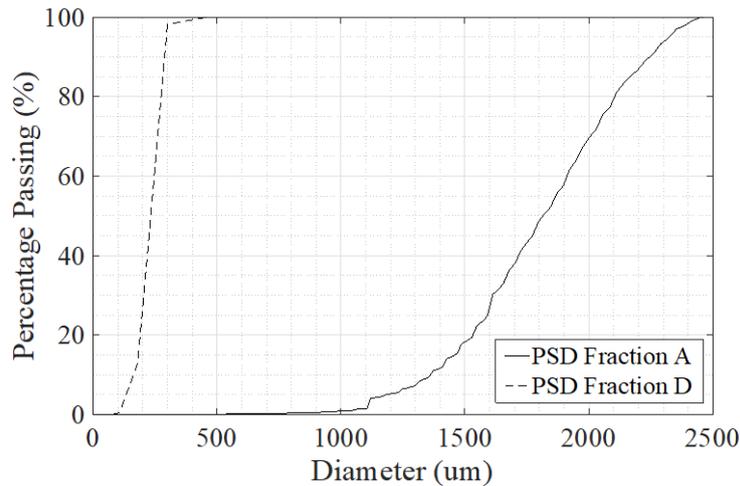
178 Two silica sands differing by a factor of 10 in mean particle size (D_{50}) were used as the base
 179 material matrix for the specimens. This selection was driven by a desire to assess the suitability
 180 of MICP for creating synthetic rock specimens across a wide range of particle sizes, possibly
 181 beyond natural rock characteristics as this would allow the use of bespoke materials with
 182 exaggerated features in further testing programs.

183 The characteristics of both sands are reported in Table 1. The fine sand had a D_{50} of 0.18 mm,
 184 while the coarse sand D_{50} was 1.82 mm. The particle size distribution curves are shown in Fig.
 185 2. The mineralogy and other characteristics of the sands were similar: both sands were uniform
 186 and had sub-rounded grains with medium sphericity. The coefficient of uniformity was 1.38
 187 and 1.33 for the fine and coarse sands, respectively. The average grain size of the fine sand
 188 falls in the optimum range of grain sizes for bio-cementing and has been used widely (DeJong
 189 et al. 2006; Al Qabany et al. 2012) whilst according to Mitchell and Santamarina (2005), the
 190 coarse sand used in this study is not recommended for bio-cementation due to the large size of
 191 its pores (see Fig. 1).

Sand	Mineralogy	Grain Angularity	Average particle diameter (mm)	Coefficient of uniformity Cu	Coefficient of curvature Cc	Initial porosity
Fine	Quartz	Sub-rounded	0.18	1.38	0.89	0.38-0.42
Coarse	Quartz	Sub-rounded	1.82	1.33	1.05	0.33-0.37

192 **Table 1.** The characteristics of the two sands used in this study

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194

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Fig. 2. Particle size distribution curves for fine and coarse sands

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To create test specimens, the sand was placed in cylindrical molds of 70 mm diameter and 220 mm height and vibrated until the porosity of the fine sand was in the range of 0.38-0.42 and the porosity of the coarse sand was between 0.33-0.37.

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The treatment was carried out in two phases: (1) 330 ml of bacteria solution (BS), equivalent to 1.1 the specimen pore volume, was injected only once at the beginning of the process and allowed to saturate the specimen for 24 hrs; (2) multiple injections of 330 ml of cementation solution (CS), each equivalent to 1.1 times the pore volume of the specimen, were then delivered at regular 24 hr intervals.

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The number of injections of cementation solution depended on the desired final cementation level, defined as weight of calcium carbonate over the total weight of the sample, and the efficiency of the process in transforming available reactants into calcium carbonate, i.e. the ratio of calcium carbonate precipitating over calcium chloride introduced to the sand columns.

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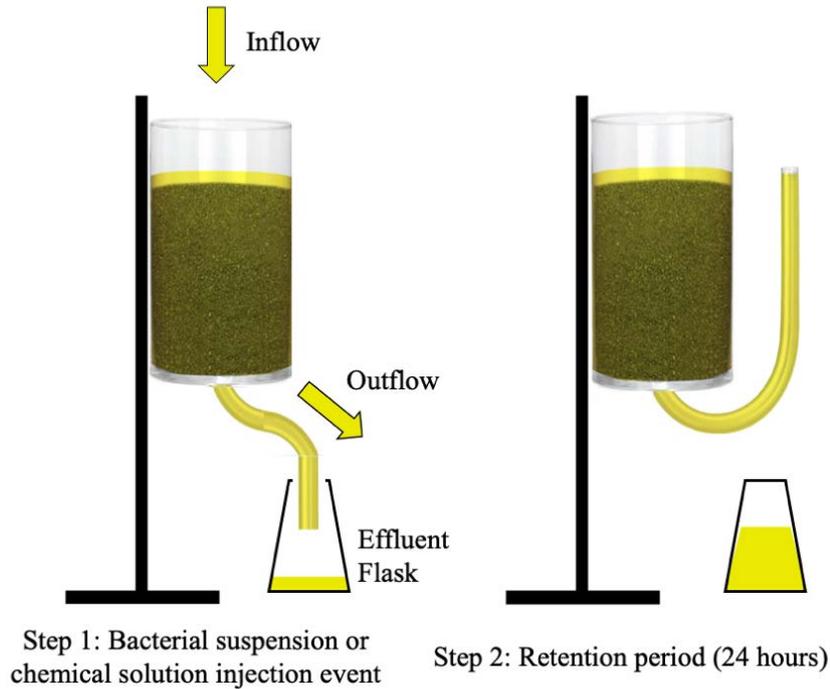
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The theoretical number of injections was calculated as the total volume of cementation solution required for precipitation of the specified amount of desired cementation level (carbonate content) divided by the volume of one injection (330 ml), assuming that all reactants were converted into products. A preliminary testing program determined that the efficiency of the

203

212 process was around 80% and 60% in the fine and coarse sands, respectively. The number of
213 injections needed to achieve a targeted cementation level was calculated based on these values:
214 for example, if the theoretical number of injections to achieve a specific cementation level was
215 10, then the actual number of injections required to achieve the target would be 12 for the fine
216 sand and 16 for the coarse sand.

217 Injection via gravity was selected, since it has been shown to result in uniform samples when
218 compared to other methods (Mujah et al. 2017) and the grain size of the fine sand used in this
219 study falls in the optimum range to inject with this technique. Filters were placed at the top and
220 bottom boundaries to diffuse the flow evenly. A similar protocol was applied by Al Qabany et
221 al. (2012) for smaller samples with 35.4 mm diameter. The experimental setup is illustrated in
222 Fig. 3. With each new injection, the previous solution was allowed to drain out and at the same
223 time, new solution was introduced to the specimen. Outward flow was stopped when 1.1 pore
224 volume of solution had been collected at the outflow. The saturated specimen was allowed to
225 rest for a 24 hr retention period for both bacteria and cementation solution injections. The
226 overall MICP treatment process was completed once the pre-defined number of injections of
227 chemical solution had been administered.



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Fig. 3. Experimental setup - Stepwise injection via gravity: Step 1 – Injection; Step 2 - retention period.

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At the end of the last retention period, specimens were extracted from the molds with care to minimise disturbance. About 10 mm were trimmed from the ends of the sand columns to eliminate potentially disturbed or uneven zones. The remaining portion was divided in two parts, one to provide a specimen with a final height of 150 mm to conform to the ASTM standard for unconfined compression testing, the other to be used for point load tests.

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The only parameter allowed to vary across specimens was the number of injections, resulting in different cementation levels.

237

238 **3.3. Experimental characterisation**

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The effectiveness of the proposed approach in producing consistent and controlled characteristics was evaluated through a series of tests. Uniformity, repeatability and efficiency were assessed for varying calcium carbonate contents. These metrics define how easy it is to produce specimens of a desired cementation level and, most importantly, the quality of those

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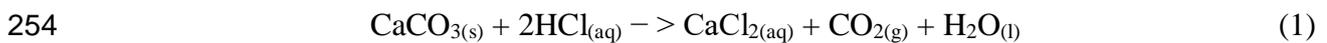
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243 specimens for the purpose of laboratory testing. Chemical efficiency, defined as the amount of
244 reactants converted into products, was often used in previous studies to assess the effectiveness
245 of the MICP process and is included in this study to compare the findings. The strength of the
246 specimens at various cementation levels and porosities was measured with unconfined
247 compressive strength and point load tests. Microscopy images were taken to understand the
248 morphological differences in the bio-cemented material, which may explain strength
249 variations.

250 **3.3.1. Calcium carbonate Content**

251 Calcium carbonate content was measured according to the procedure in ASTM D4373-14
252 (ASTM 2014). A 30 g dried and ground sample was treated with 30 mL of hydrochloric acid
253 (HCl) of 2.5 M. Calcium carbonate (CaCO_3) is dissolved according to the reaction:



255 Carbon dioxide is released into a chamber (calimeter) equipped with a pressure gauge. The
256 pressure reading is translated into amount of carbon dioxide, allowing the amount of calcium
257 carbonate to be calculated with the aid of the stoichiometry of the reaction. The degree of
258 cementation (C_w) is expressed in this study as weight of calcium carbonate over the total
259 weight of the sample tested (in percent).

260 **3.3.2. Unconfined Compressive Strength and Point load tests**

261 Unconfined compressive strength (UCS) and point load tests (I_s) were performed on oven dried
262 specimens with varying levels of cementation. For the UCS tests, the samples were prepared
263 and tested according to ASTM D7012-14e1 (ASTM 2004) and ASTM D2938:390-391 (ASTM
264 1995). The specimens in the axial compression tests had a 70 mm diameter and a 150 mm
265 height. The loading of the samples was displacement-controlled with a rate of 1.14 mm/min.

266 Point load tests were conducted on core and lump specimens to assess the rock strength index

267 following ASTM D5731-16 (ASTM 1985). Care was taken in order to induce failure between
268 the tenth and the sixtieth second of the test. The smallest dimension of the specimens in the
269 lump tests was no less than 30 mm.

270 3.3.3. Final porosity

271 Porosity (n) is defined as:

$$272 \quad n = 1 - \frac{\rho}{G_s} \quad (2)$$

273 where ρ is the bulk dry density and G_s is the specific gravity of the porous material. The final
274 porosity was calculated using an equivalent specific gravity that takes into account the
275 specific gravities of the individual minerals present based on the relative volume fraction. For
276 a rock that consists of two minerals (Sharwood 1912):

$$277 \quad G_s = \frac{W_{total}}{\frac{w_1}{G_{s1}} + \frac{w_2}{G_{s2}}} \quad (3)$$

278 where W_{total} is the total dry weight of the artificial material, w_1 and w_2 are the weight of
279 quartz and calcium carbonate within the rock, respectively. G_{s1} and G_{s2} are the specific
280 gravities the of quartz and calcium carbonate, equal to 2.65 and 2.71 respectively.

281 3.3.4. Microstructural Observations

282 Environmental scanning electron microscope (ESEM) images of MICP treated samples were
283 taken to investigate the morphology and distribution of calcium carbonate crystals and their
284 bonding network. The microscopy investigation was carried out with a PHILIPS XL30
285 scanning electron microscope. All MICP treated samples were dried at 100°C for 24h before
286 conducting the microscopy analysis.

287 4. RESULTS & DISCUSSION

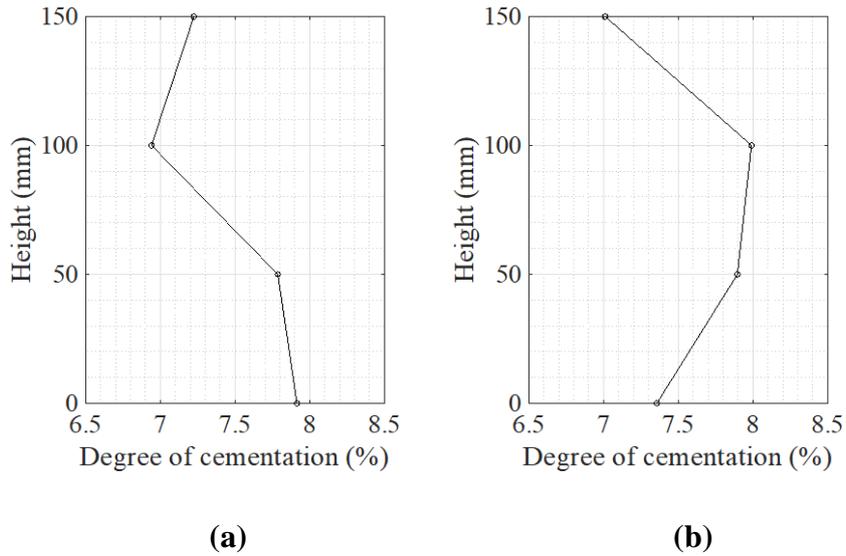
288 The effectiveness of the MICP process and the resulting mechanical properties were
289 significantly affected by the particle size distribution of the matrix material. The same number

290 of injections resulted in different calcium carbonate concentration levels due to variations in
291 chemical efficiency. Even when the concentration levels were similar, the resulting cemented
292 material properties varied for different particle size distributions (PSDs). These effects are
293 examined separately in this study since a single recipe was followed for both types of sands in
294 order to eliminate any influence from bio-chemical factors.

295 **4.1. Effectiveness of MICP in the fine and coarse sands**

296 Three metrics were used to assess the ability of MICP to produce suitable specimens: chemical
297 efficiency, repeatability, and uniformity. Chemical efficiency is defined as the amount of
298 calcium carbonate in the final specimen (in mol/litre) relative to calcium chloride injected in
299 mol/litre expressed in percentage. Calcium chloride was chosen over urea as it is the limiting
300 factor in the reactions (the ratio of urea to calcium chloride is 1.5:1, therefore if all calcium
301 chloride is consumed there is an additional 0.125 M urea left). Although the chemical
302 efficiency is not directly related to the quality of the specimens, it is generally used to assess
303 the effectiveness of the process in other works, which will be used for comparison with the
304 results presented here. Repeatability, which is derived from chemical efficiency, accounts for
305 the ability to produce similar outcomes starting from the same components and quantities
306 through the same process and it is a more appropriate figure for the purposes of this research.
307 Repeatability is assessed with plots of actual vs targeted cementation levels. Uniformity
308 measures the spatial distribution of the cementing agent across the height of the specimens.

309 The three metrics were assessed against measurements of carbonate content at four to five
310 points along the height of each specimen. Examples of cementation level profiles are reported
311 in Fig. 4 for the fine and coarse sand specimens at a medium cementation level within the range
312 targeted in this study. The calculations for chemical efficiency and repeatability were based on
313 the average cementation level of the specimen, while the degree of uniformity was assessed
314 based on the variance of the cementation level for each profile.

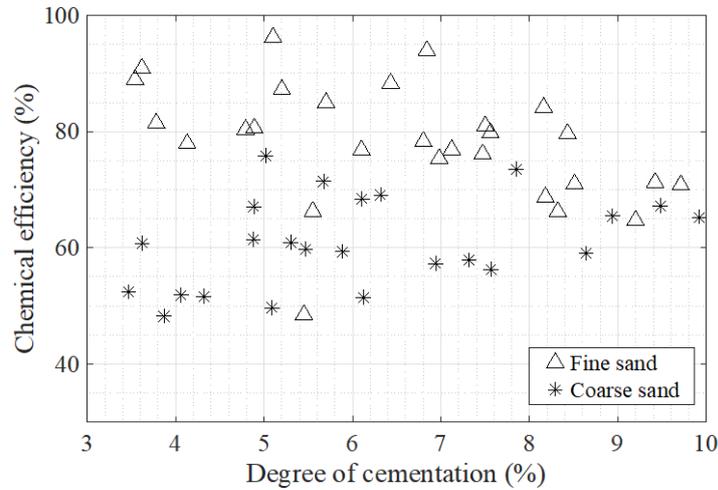


317 **Fig. 4.** (a) Cementation level profile of fine sand and (b) Cementation level profile of coarse
 318 sand at an average cementation level of 7.5%

319 **4.1.1. Chemical efficiency**

320 The measured chemical efficiency is plotted against the degree of cementation for the fine and
 321 coarse sands in Fig. 5. The results include all samples developed for this study. The
 322 precipitation efficiencies of calcium carbonate of the coarse sand specimens are around 60%
 323 and almost constant at all cementation levels, although with some scatter. In contrast, the
 324 efficiencies of the MICP process in the fine sand specimens are about 80% at a cementation
 325 level of 4%, falling to 70% at higher degrees of cementation.

326 The lower chemical efficiency at high cementation levels can be explained by the heavy
 327 precipitation of calcium carbonate at the injection point, leading to clogging of the pores. This
 328 in turn, hindered further penetration of the cementation liquid into the sample. Although the
 329 system had low reaction rates due to lower urease activities, as the cementation level increased,
 330 the flow rate decreased, allowing more of the chemical solution to be consumed around the
 331 injection point. This portion of the specimens was eliminated and only the central 180-200 mm
 332 were used in the following studies.



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Fig. 5. Chemical efficiency at various cementation levels

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Injections in the fine sand specimens showed lower chemical efficiency values compared to Al Qabany et al. (2012) who found that the chemical efficiency remained approximately constant with the degree of cementation at around 90% or above (for calcium chloride concentrations of 0.25 M). While the chemical recipe and the experimental protocol in the two works are similar, lower urease activity in this study, in conjunction with much longer retention times or even different surface conditions (chemical characteristics etc.) on host grains, may explain a reduction in the chemical efficiency. Achieving high cementation levels required a large number of injections of chemical solution, increasing the overall duration of the bio-treatment to 16 or even 20 days, and leading to substantial reduction in bacterial activity towards the end of the process (van Paassen 2009; Konstantinou 2020).

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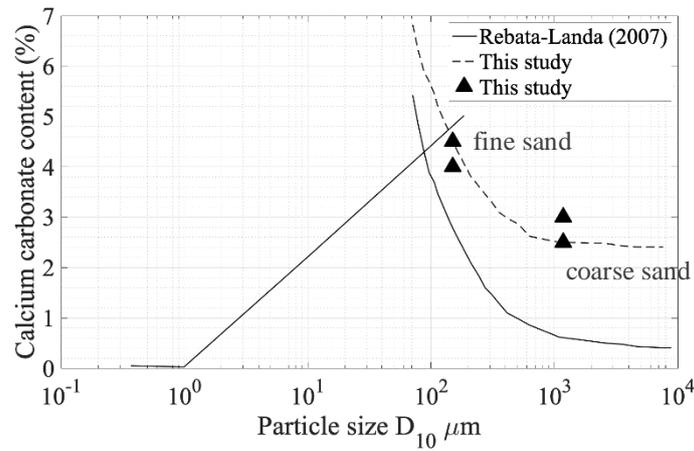
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Although it was expected that the MICP process would have lower efficiency in sands with larger particle size, resulting in very lightly cemented samples, this was not the case in this study. The high density of the bacteria (optical density of 1.5- 2.0) increased the probability of microbes attaching to the particles and the long retention time between the bacteria injection and the first cementation solution injection improved the settlement of bacteria, therefore

351 increasing efficiency. The efficiency of injection in the coarse sand specimens was still lower
352 compared to that of the fine sand specimens as, inevitably, more bacteria were flushed out of
353 the specimens due to the higher flow rate (20-30 ml/min) during the first cementation solution
354 injection when the suspension liquid was removed (Liu et al. 2019; Wang et al. 2019a).
355 Measurements of the optical density were taken in approximately every 60 mL of effluent after
356 the first injection. For coarse sand, the OD₆₀₀ of the first 60 mL was around 0.9 and increased
357 to 1.3 in later stages, before finally decreasing again towards the end. The OD₆₀₀ of the effluent
358 for fine sands was lower throughout the process at 0.7-1.

359 Fig. 6 shows results of this study against the findings by Rebata-Landa (2007) for a target
360 cementation of approximately 5% for varying particle sizes. The solid line and curve represent
361 the findings of Rebata-Landa (2007). The author injected the same amount of chemical solution
362 in soils with varying grain sizes and showed that no cementation takes place for particle size
363 less than 1 μm and then the precipitation level increases linearly up to 100 μm . Above the
364 threshold of 100 μm , the cementation level decreases substantially. The figure includes the
365 range of average cementation level for fine and coarse sand specimens with targeted
366 cementation of 5% (triangles). The fit provided by Rebata-Landa (2007), was shifted upwards
367 to match the experimental data of this work (dashed curve). While the fine sand specimens in
368 this study showed similar results, the coarse sand specimens performed better than predicted
369 in Rebata-Landa's study demonstrating good chemical efficiency, and thus good repeatability.
370 Recent experiments on microfluidic chips (Wang et al. 2019a, 2019b) have proven that bacteria
371 form aggregates as soon as the cementation solution is injected, with aggregates increasing in
372 size with larger optical density. The MICP procedure in this study adopted optical densities in
373 the upper range studied by Wang et al. (2019a) possibly resulting in larger aggregates which
374 are more likely to settle within the porous medium instead of being flushed out of the specimen,
375 leading to overall higher chemical efficiency. The higher efficiency found in this study extends

376 the micro-fluidics findings by Wang et al. (2019a) to actual soils.

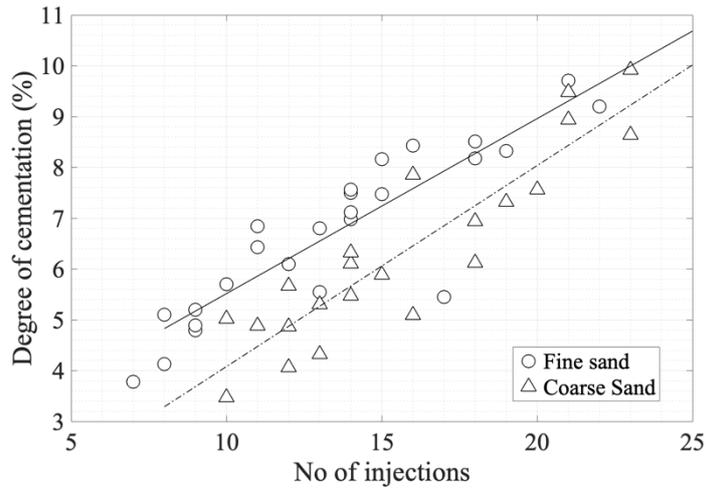


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378 **Fig. 6.** CaCO_3 content and models as a function of grain size (after Rebata-Landa (2007))

379 4.1.2. Repeatability

380 One of the objectives of this work was to generate artificially cemented sands with similar
381 carbonate characteristics but with varying cementation levels in a repeatable manner. Fig. 7
382 presents the averaged degree of cementation of both fine and coarse sand specimens with
383 respect to the number of injections. In both cases, the relationship is linear, demonstrating the
384 success of the design of the MICP procedure as the number of injections largely controls the
385 amount of cementation. Clearly, for the same number of injections, larger amounts of carbonate
386 precipitate in fine sands than in coarse sands. However, at higher injection numbers the
387 difference between the precipitating cement in fine and coarse sands becomes smaller.



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Fig. 7. Number of injections and the degree of cementation

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Fig. 8 shows the average degree of cementation of each specimen, derived by averaging the

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measurements of calcium carbonate across the height of each sample. In the fine sand with 5-

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7% target cementation, the achievable values are similar to the targeted ones, as the data points

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are concentrated around the 1:1 line, while over 7% the achievable values are lower. In the

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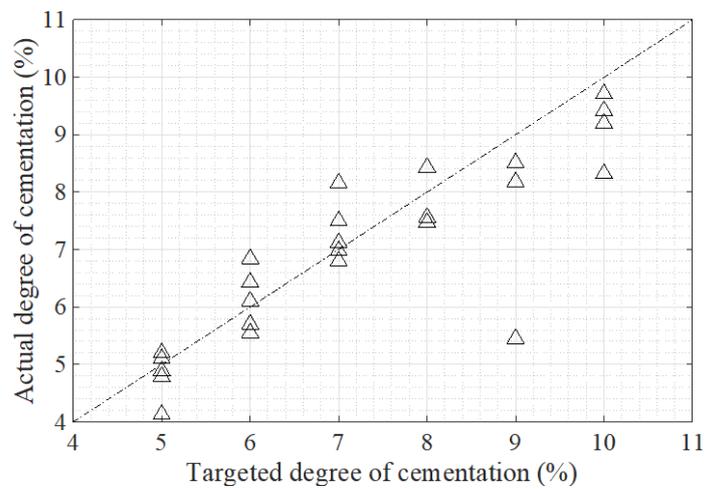
coarse sand, the achievable cementation levels are more scattered and the averages for each

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cementation level are lower than the targeted ones. The results confirm generally good

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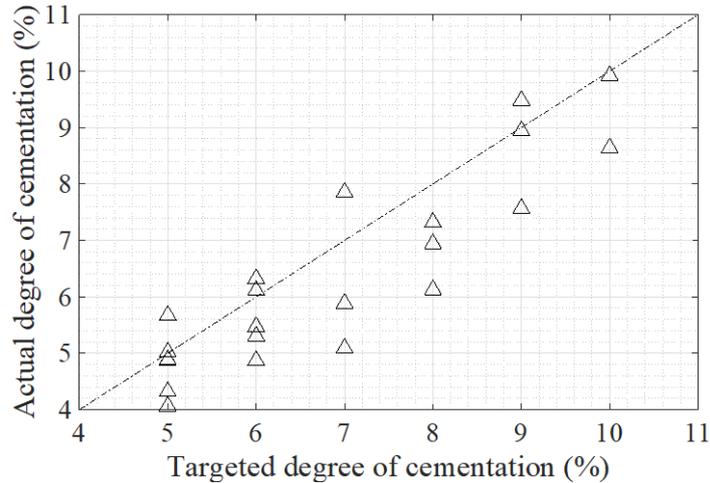
repeatability for the fine sand and a lower degree for the coarse sand.



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(a)



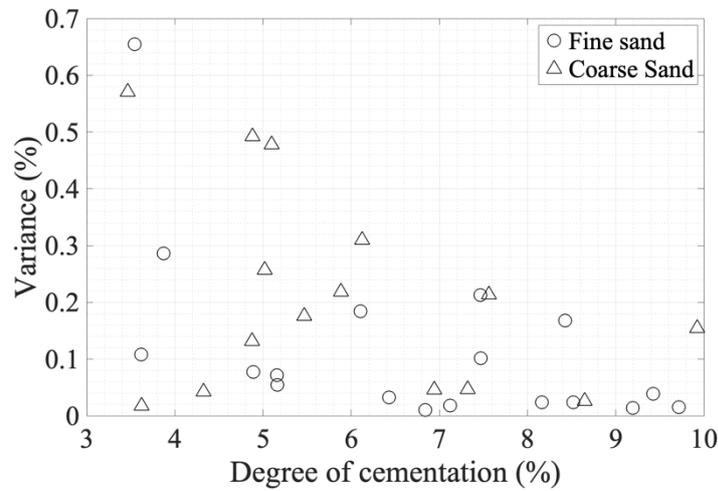
(b)

Fig. 8. Actual vs targeted degree of cementation for (a) fine and (b) coarse sands.

4.1.3. Uniformity

As shown in Fig. 9, the variance in uniformity of cementation measurements declines as the cementation level increases, indicating more uniform samples at the highest range of about 10% (g of calcium carbonate/ g of specimen). The carbonate precipitation in the fine sand specimens is relatively uniform above 5% cementation, while similar variability is observed for the coarse sand at slightly higher cementation levels (6%-10%). No particular trend was observed in the precipitation profiles across the height of each sample. A possible explanation for observed trends in variance when the cement content increases is that, once the easily accessible pores are filled with cement, the cementation solution in a subsequent injection is forced to flow in what were originally less permeable parts of the sand. The coarse sand samples were uniformly cemented along the height because the high injection rates, and the longer retention times (24 hours is towards the longer intervals being used previously) in conjunction with the low bacteria activity, allowed the reaction to take place almost at the same time along the height of the sample. For the fine sand specimens, although the injection rate was lower, this was compensated by the low bacterial activity, which resulted in low urease

417 conversion rates.



418

419

Fig. 9. Variance of uniformity profiles

420 Since the coarse sand specimens had higher flow rates, a more uniform cementation
421 distribution would be expected. This trend was indeed observed by Cheng and Cord-Ruwisch
422 (2014), on sands falling in the optimum compatibility region (Mitchell and Santamarina 2005).
423 However, it is not the case for the coarse sand used in this study. The literature review has
424 shown conflicting results between different authors on uniformity versus cementation level.
425 Previous studies including uniformity measurements (Feng and Montoya 2015; Lin et al. 2015)
426 did not use injection via gravity for delivering the solutions. Therefore, at least some of the
427 difference in trends between the results of this study and those of previous works may be
428 attributed to the injection method.

429 The highest variation in calcium carbonate content within a specimen was in the range between
430 1.5 and 2.0 % by weight, whilst the most uniform specimens had cementation level varying by
431 only 0.1 to 0.2 % by weight. Most of the previous studies in fine sands have shown differences
432 larger than 1.5% in calcium carbonate content within each sample (Dawoud 2015; Feng and
433 Montoya 2015; Cui et al. 2017). Very few studies provide uniformity profiles of different bio-
434 sands with particle sizes produced through the same MICP procedure. Limited results presented

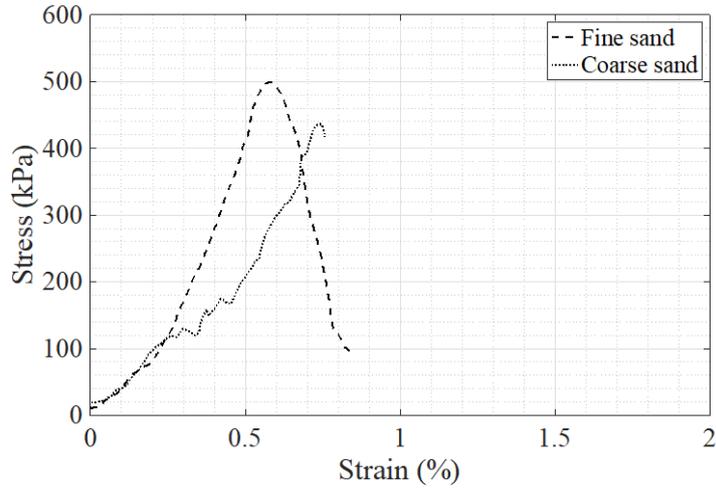
435 by Lin et al. (2015) suggest that medium-fine sands (average particle diameter of 0.71 mm)
436 tend to produce less uniformly cemented products compared to the fine ones. The very coarse
437 bio-cemented sands (average particle diameter of 1.6 mm) obtained by Mahawish et al. (2018)
438 also show limited success in controlling the MICP process when large particles are used, since
439 the average variation between the measurements of calcium carbonate content within each
440 sample are about 3 % by weight. The conflicting observations can be explained by the very
441 different MICP procedure followed by Mahawish et al. (2018) compared to the one in the
442 present study. The review of these previous studies highlights the challenge of comparing
443 outcomes of different MICP processes.

444 **4.1.4. Relation between the three metrics**

445 There is a trade-off between chemical efficiency and the degree of uniformity as the chemical
446 efficiency and variance in carbonate content decline with the increase of cementation. This
447 means that, for specimens generated with the bio-chemical and injection methods selected in
448 this study, a more cemented specimen is more uniform, but more difficult to obtain because
449 the efficiency decreases when cementation is higher. The long injection intervals of 24 hours
450 extended the overall duration of the injection phase. When a higher cement content was
451 targeted, a decline in bacterial activity was observed towards the end of the injection phase due
452 to the larger number of injections and, therefore, the extended amount of time was needed to
453 achieve the targeted cementation (van Paassen, 2009).

454 **4.2. Effects of degree of cementation and porosity on strength**

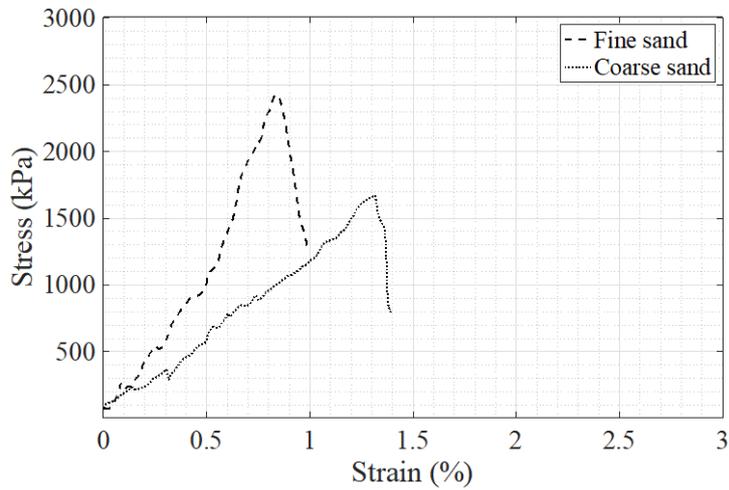
455 UCS and point load index tests were performed to examine the correlation between the degree
456 of cementation and the strength of the samples. Examples of the stress strain curves obtained
457 for the fine and coarse MICP-treated sands at low (5.5%) and high (10%) cementation levels
458 are presented in Fig. 10 (a) and (b), respectively.



459

460

(a)



461

462

(b)

463 **Fig. 10.** Stress strain curves for both fine and coarse MICP-treated sands at (a) low and (b)

464

high degrees of cementation

465 The strength increases substantially as the cementation level changes from 5% to 10%, from

466 500 kPa to about 2500 kPa and from 450 kPa to 1600 kPa for the fine and coarse sands,

467 respectively. These values fall within the range of measured strengths of natural soft sandstones

468 reported in the literature. The sharp peak, immediately followed by a dramatic decrease in the

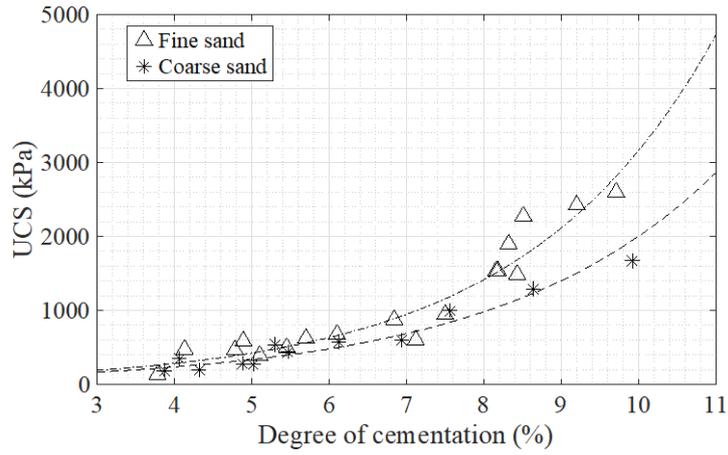
469 strength, indicates brittle failure, which occurred at less than 2% strain. The stress-strain curve

470 of MICP-treated coarse sand specimens shows fluctuations due to the appreciable dislocation

471 when crushing of the bonds causes closure of the voids. Between 5% and 10% cementation,
472 the specimens show a characteristic axial splitting mode. These observations are also consistent
473 with previous MICP work by Cheng et al. (2013) and van Paassen et al. (2010). Visual
474 inspection revealed that the weakest specimens tended to disaggregate at grain scale with the
475 particles of the coarse sand, especially, detaching from the failure surface.

476 Five coarse sand specimens with low to medium cementation levels failed as soon as the initial
477 load was applied as they were weaker at one of the two ends, adjacent to the top or bottom
478 pedestal. They were treated as having null strength and were removed from the subsequent
479 plots. The samples' uniformity could not be assessed as the original location of the grains
480 could not be identified.

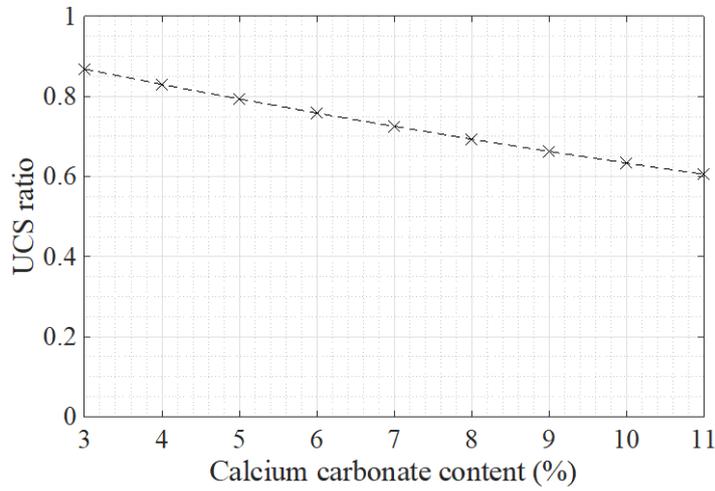
481 Both sands show a substantial increase in strength when the cementation increases (Fig. 11
482 (a)), as found by many authors (Al Qabany and Soga 2013; Feng and Montoya 2015; Lin et al.
483 2015). The sand matrix is originally cohesionless and unstable structures are formed at lower
484 calcium carbonate contents. The gain in strength is relatively small at lower cementations, but
485 it becomes more pronounced at higher cementation levels and especially in the fine sand above
486 7% cementation. At a cementation level of 3%, the ratio of the UCS of the coarse sand to the
487 UCS of the fine sand is at about 90%, as shown in Fig. 11 (b). The ratio decreases to about
488 60% at a cementation level of 10%. An exponential curve provided the best fit for both fine
489 and coarse sands, as shown in Table 2.



490

491

(a)



492

493

(b)

494

Fig. 11. (a) UCS results with various degrees of cementation for MICP-treated fine and
 495 coarse sand specimens (b) UCS of coarse sands over the UCS of fine sands with respect to
 496 cementation level

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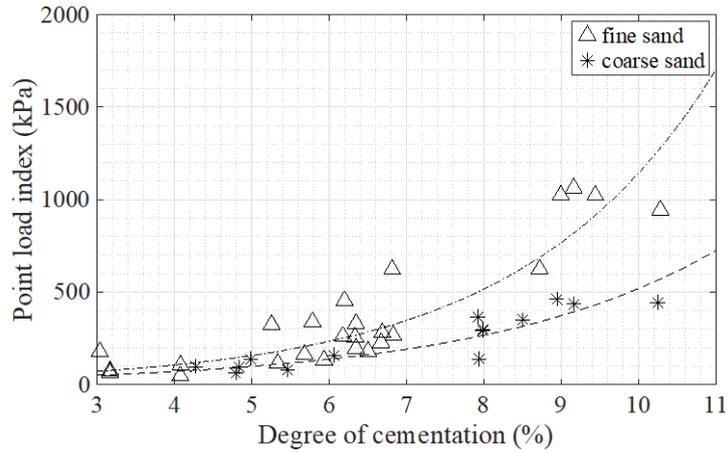
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Type of correlation	Type of sand	Expression	R ²
UCS = f(cementation level)	Fine	$UCS = 56.911 * \exp(0.4018 * C_w)$	$R^2 = 0.87901$
	Coarse	$UCS = 56.544 * \exp(0.3568 * C_w)$	$R^2 = 0.90103$
Is = f(cementation level)	Fine	$Is = 21.385 * \exp(0.3979 * C_w)$	$R^2 = 0.7709$
	Coarse	$Is = 18.44 * \exp(0.3337 * C_w)$	$R^2 = 0.8231$
UCS = f(porosity)	Fine	$UCS = 0.0888 * n^{-8.715}$	$R^2 = 0.6866$
	Coarse	$UCS = 0.0053 * n^{-9.526}$	$R^2 = 0.8353$

502 **Table 2.** Curve fitting for UCS with respect to cementation level and porosity and Is with
503 respect to cementation level

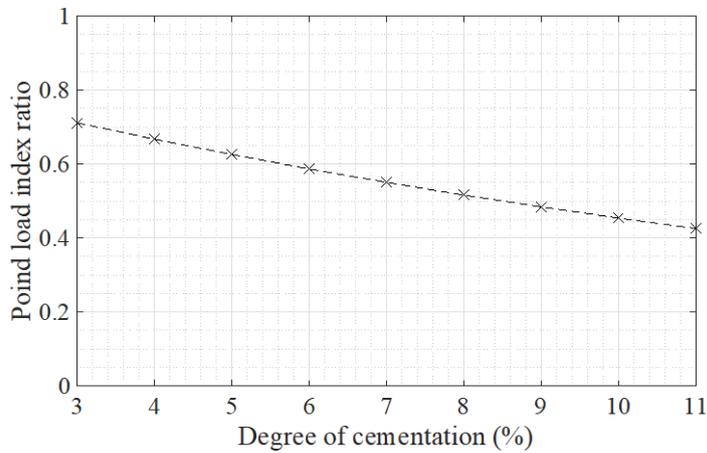
504 The strength was also assessed by point load index tests. The measurements are plotted with
505 respect to the degree of cementation in Fig. 12 (a). The coarse sand samples with less than 4%
506 degree of cementation were very weak, making this test unsuitable. Although the results are
507 more scattered compared to the UCS results, an exponential regression curve provided a best
508 fit for both types of sands (Table 2). The exponent values are 0.3979 and 0.3337 for the fine
509 and coarse sands, respectively, which are similar to those obtained in the UCS tests. At lower
510 cementations the ratio of the point load strengths of the coarse sand over that of the fine sand
511 is about 71% and it reduces to 50% at higher concentration levels, as shown in Fig. 12 (b).



512

513

(a)



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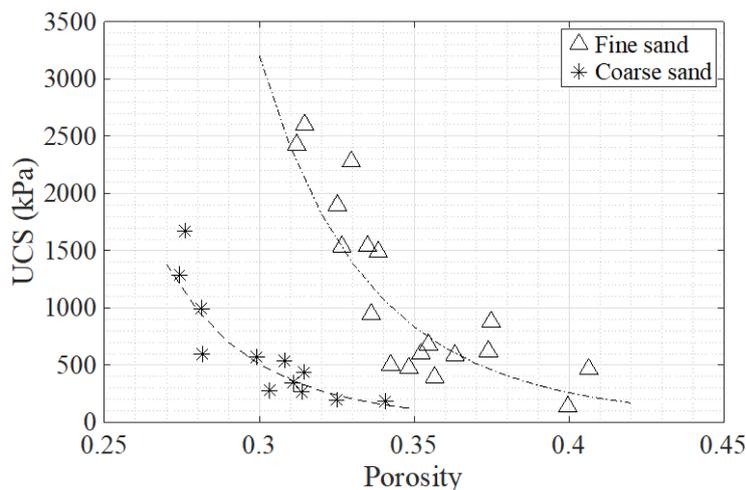
(b)

516 **Fig. 12.** (a) Point load index results with respect to various degrees of cementation for fine
 517 sands and coarse sands (b) Point load index of coarse sands over the point load index of fine
 518 sands with respect to cementation level

519 Coarser particles form fabrics with larger pores, but overall smaller porosity, because they
 520 cannot achieve stable and very open arrangements. If particles are spaced too far apart the
 521 structure quickly collapses under small solicitations. Finer particles are able to form more open
 522 stable arrangements with higher porosity, but smaller void sizes. The larger number of particles
 523 in the same volume also results in larger surface area and more contact points available for
 524 calcium carbonate deposition. Fig. 13 shows that the final porosity of the MICP treated fine

525 sand specimens falls in the range of 0.3-0.4 and the final porosity of the MICP treated coarse
526 sand specimens falls in the range of 0.25-0.35. A power function provided best fits for both
527 types of sands (highest R-squared values). As seen in Table 2, unconfined compressive strength
528 is higher when the final porosity is lower; as porosity decreases, a higher proportion of the
529 voids is filled with calcium carbonate and a further reduction of porosity causes higher gain in
530 strength. This trend is more evident in the fine sand where the initial void sizes are smaller and
531 more readily occluded.

532 In the common porosity range (0.3-0.35), the UCS of fine sand is four to five times that of the
533 coarse sands, bracketing the range of achievable strengths and porosities. By varying the grain
534 size, and possibly the width of the particle size distribution, it is possible to achieve different
535 combinations within the boundaries shown. Plumb (1994) reported an empirical relationship
536 to correlate soft sandstones' strength with porosity in a power form and specified an upper
537 boundary. As shown later, both the fine and coarse sand specimens' data points fall below the
538 upper strength limit, in the region of the plot towards the higher porosity range measured for
539 natural materials.



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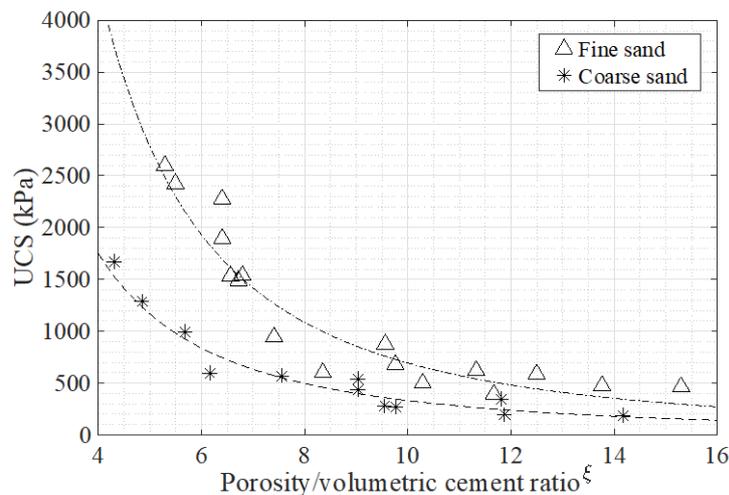
Fig. 13. UCS results with respect to porosity

542 The increase in strength is a function of both the final porosity and cementation level, as seen

543 in Figs. 12 and 13. Consoli et al. (2010) utilised a power function to express UCS as a function
 544 of the ratio of the volumetric cement content, defined as volume of calcium carbonate over the
 545 total volume of the sample (C), and porosity of the specimen, which accounts for the conjugate
 546 effects of these variables on the strength of the samples (Consoli et al. 2007, 2011). The
 547 porosity over the volumetric cement ratio is often adjusted by an exponent ξ which is selected
 548 across a range of possible values to provide the best fit.

$$549 \quad UCS = f\left(\frac{\text{porosity}}{\text{volumetric cement ratio}^\xi}\right) = f\left(\frac{n}{C^\xi}\right) \quad (4)$$

550 The UCS values obtained from the tests are plotted against this ratio (Fig. 14). The coefficient
 551 ξ giving the best fit for the fine sand is 0.97 and that for the coarse sand is 1. Both coefficients
 552 are very close to 1, which, according to Rios et al. (2013), indicate that the two sands have the
 553 same mineralogy and similar particle shape, as well as being uniform.



554
 555 **Fig. 14.** UCS Vs. **porosity/ (volumetric cement ratio) $^\xi$** ratio: Power fit for coarse and
 556 fine MICP-treated sand specimens

557 The successful use of MICP to generate specimens using base materials with two very different
 558 grain sizes established specific combinations of strength and porosity. This initial work
 559 indicates that a similar approach can be used to treat materials with intermediate grain sizes or
 560 wider PSD.

561 **4.3. Comparison of the properties of artificial specimens with natural weak sandstones**

562 UCS is the most typical property measured when assessing the behaviour of rock, however,
563 point load index tests are easier to conduct. The values for the ratio of UCS over I_s in this study
564 were around 2.8 for fine sands and 3.3-3.9 for coarse sands, below the range of 6.6 to 30
565 reported in the literature for sedimentary and soft rocks (Rabat et al. 2020).

566 The strength of the artificial specimens in this study varied between 200 and 3000 kPa, falling
567 in the range for very weak and extremely weak sandstones (ISRM 1981). UCS reported in the
568 literature for a number of sandstones is collected in Table 3, demonstrating the great variability
569 in natural materials from the same formations. Wide ranges of porosity (0.2-0.4) are also
570 reported for this group of soft rocks, characterized by values that are generally higher than the
571 ones reported for stronger sandstones associated with porosity of less than 0.1. In this study
572 porosity fell in the interval 0.26 to 0.42 within the same wide range exhibited by the very weak
573 natural carbonate cemented sandstones. Fig.15 presents pairs of UCS and porosities values
574 found in literature, along with the trends identified for fine and coarse sands in Fig. 13,
575 bracketing the grey area highlighting achievable strengths and porosities. A large portion of
576 pairs reported in literature fall in the region of achievable strengths.

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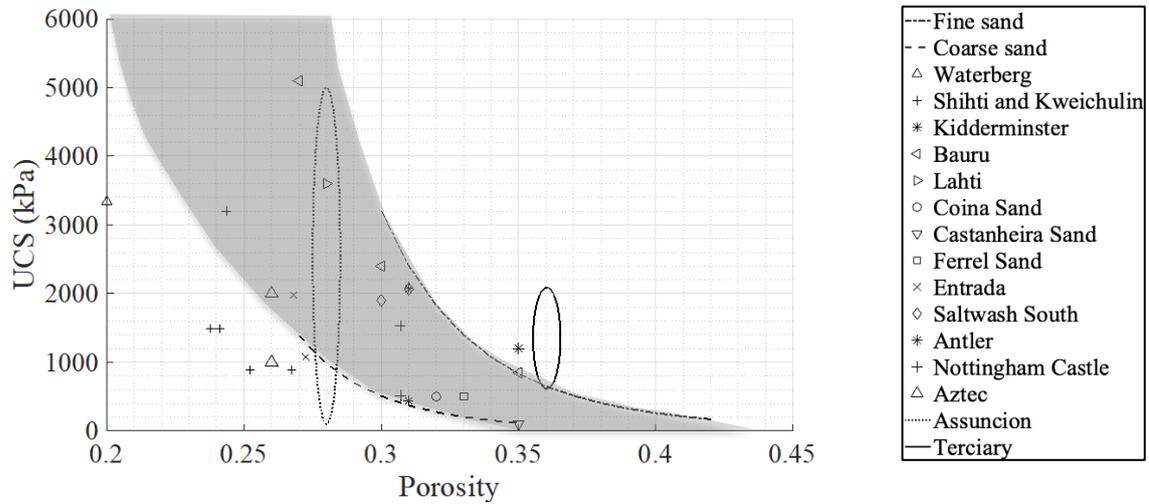
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Name/Type of sandstone	UCS (kPa)	Porosity	Reference(s)
Waterberg	3338	0.2	Mohlala (2016)
Shihti and Kweichulin Formations	880- 3200	0.24-0.27	Chen and Hu (2003)
Kidderminster	440-2070	0.31	Dobereiner (1984); Freitas and Dobereiner (1986)
Bauru	850-5100	0.27-0.35	Dobereiner (1984); Freitas and Dobereiner (1986)
Lahti	3600	0.28	Dobereiner (1984); Freitas and Dobereiner (1986)
Coina Sand	500	0.32	Freitas and Dobereiner (1986)
Castanheira sand	100	0.35	Freitas and Dobereiner (1986)
Ferrel sand	500	0.33	Dobereiner (1984)
Entrada sandstone in Utah, USA	1080-1980	0.27	Larsen (2015)
DV sandstone	1640-3720		D. S. Agustawijaya (2007)
Saltwash South	1900-2070	0.3-0.31	Ispas et al. (2012); Pradhan et al. (2014)
Pleistocene sandstone, shale	200-1200		Huang and Pan (1999)
Pleistocene Toukoshan Formation	100-1300		Ku et al. (2008)
Antler sandstone	1200	0.35	Krishnan et al. (1998)
Nottingham Castle Sandstone Formation	516-1530	0.307	Sattler and Paraskevopoulou (2019)
Dubai weak calcareous sandstones	500-5000		Elhakim (2015)
Calcareenite from the site of the off-shore gas platform of North Rankin in Western Australia	500-2000		Cuccovillo and Coop (1997)
Silica sandstone from the Lower Greensand series of Kent in England.	600		Cuccovillo and Coop (1997)
Cemented sands from Asunción	100-5000	0.27	Kanji (2014)
Terciary	800-2000	0.36-0.37	Kanji (2014)
Aztec sandstone	1000-2000	0.26	Haimson and Lee (2004)

584 **Table 3.** Unconfined compressive strength (UCS) and porosities for soft rocks reported in
585 previous studies.

586



587

588 **Fig. 15.** UCS with respect to porosity with values reported in literature (Table 3) and the
 589 results of this study

590 **4.4. Microstructural analysis**

591 The microstructure of natural sandstones is also a key to their characterisation. The
 592 predominant matrix mineral of weakly cemented sandstones is quartz and the cement is often
 593 carbonate (siliceous cement, calcium carbonate, or calcareous cement) or clay minerals
 594 (Krynine and Judd 1957; Fjar et al. 2008). The degree of binding action depends on the amount
 595 and type of cementing agent (Sitar et al. 1980) whilst the behaviour of most cemented
 596 sandstones appears to be quite similar, regardless of the particular cementing agent (Collins
 597 and Sitar 2009).

598 The data from the MICP specimens show that the cementation level cannot fully describe the
 599 variation in strength across the two types of sands; the fine sands have higher strengths
 600 compared to the coarse sands for a given degree of cementation and porosity (Fig. 12). Strength
 601 is not only affected by the amount of cementation, but also depends on the initial spatial
 602 configuration of the grains and the microstructural characteristics of the cementation material
 603 within the original sand structure.

604 The MICP procedure (bacterial optical density, activity, concentration of chemicals, flow rate)

605 largely controls the delivery and distribution of bacteria within the soil, as well as the speed of
606 the reactions. The calcite distribution within the granular network, in turn, depends on the
607 position of the microbes relative to the grains (at pore throats or against grain surface asperities)
608 and the matrix configuration. These parameters, therefore, define the cement precipitation
609 patterns relative to the porous medium.

610 Given that the MICP procedure is identical for both types of sand, it is reasonable to expect
611 similar calcite crystal characteristics (shapes and sizes) at a given cementation level. However,
612 the location and amount of calcite crystals are expected to be highly affected by the initial
613 configuration of the granular fabric and the voids sizes. The larger the voids are, the lower the
614 probability of a cement crystal forming at a pore throat. In the case of coarse sands, the voids'
615 size is significantly larger than the expected calcite crystals' size due to the low chemical
616 solution concentration, whilst in fine sands the voids are smaller and comparable to the calcite
617 crystals' size.

618 The particle size also defines the total number of interparticle contacts in a given volume:

619
$$N_c \sim \left(\frac{1}{R^3}\right) \quad (5)$$

620 where N_c is the particle contact points number and R is the particle radius (Ismail et al. 2002,
621 Gray, 1968).

622 The fine sand used in the present paper has 1000 times more contact points between the
623 particles compared to the coarse sand, when all the other factors (grain shape and surface
624 characteristics, sorting etc.) are assumed to be equal or negligible. It is therefore likely that
625 carbonate crystals will land at contact points in the fine sand since these interparticle contact
626 points are much higher in number compared to the coarse sand for a given volume.

627 Fine sand have an advantage in strength gain since cementation at particle-to-particle contacts
628 acts as 'bridge' for the transmission of stresses acting on the granular skeleton, whereas

629 deposition of calcite on the faces of grains has a much smaller effect on strength.

630 The precipitation patterns (size and distribution of calcite crystals within the granular matrix)

631 were evaluated with the aid of ESEM images of materials at low and high cementation levels

632 (Fig. 16). The images were all taken with a magnification of 315X at a spatial resolution of 100

633 μm to allow a clear view of the relative position of the calcium carbonate crystals with respect

634 to the grains and for comparisons of the absolute sizes of the crystals between the two sands.

635 The first image from each category (cementation level and type of sand) uses arrows to indicate

636 grains and circles to indicate calcite crystals. In the fine sand with low concentrations of

637 calcium carbonate, crystals are observed mainly at particle-to-particle contacts with limited

638 deposition at non-effective locations (Fig. 16 (a)-(b)). However, only a small portion of the

639 intergranular contacts are filled with cement, resulting in low strength gain (Fig 17(a)). Failure

640 occurs through the path of uncemented contact points, representing the weakest points. As more

641 calcite crystals are deposited, they also bond a larger portion of effective locations, resulting in

642 the faster strength increase. For very high concentrations (Fig. 16 (c)-(d) and Fig. 17 (b)) the

643 crystals fill the available voids, such that the sand grains act as rigid inclusions in a soft matrix

644 of cement and macropores (Saidi et al. 2003).

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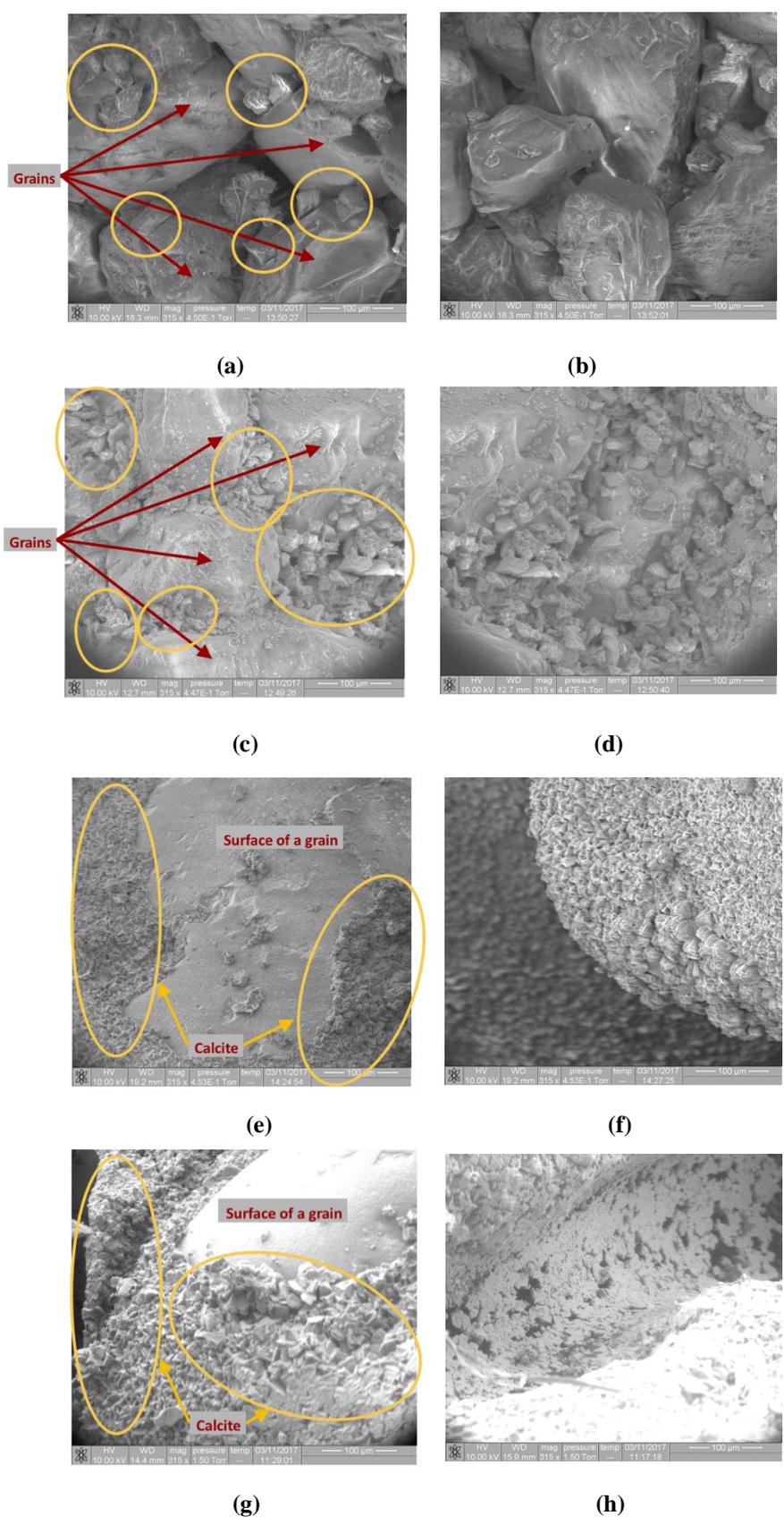
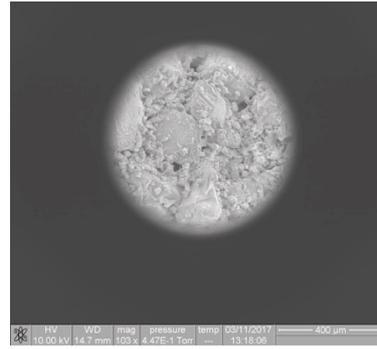
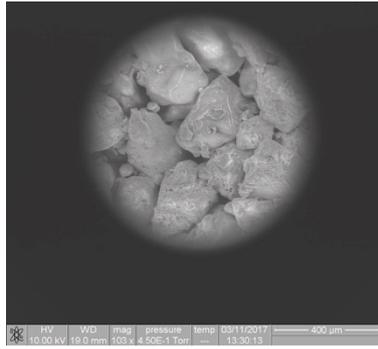
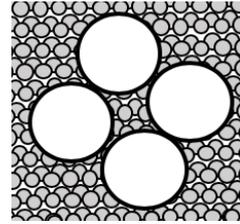
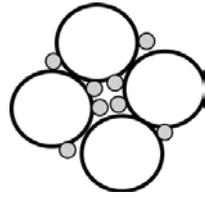


Fig. 16 . SEM images for (a)-(b) lightly and (c)-(d) heavily cemented fine sands (e)-(f) lightly and (g)-(h) heavily cemented coarse sands

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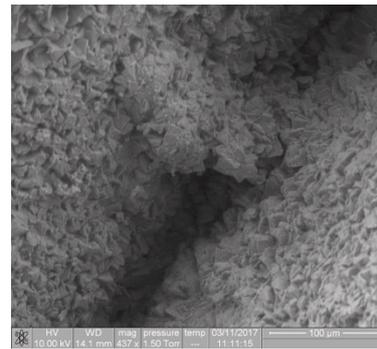
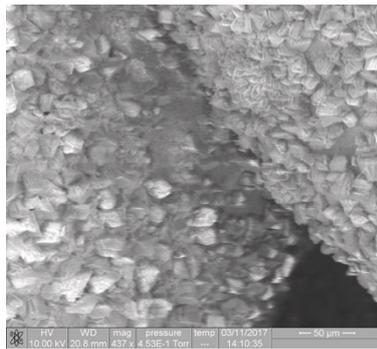


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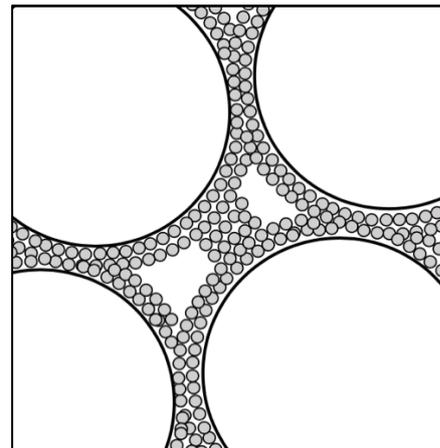
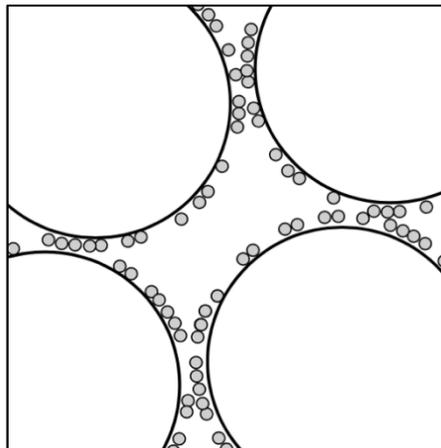
(a)

(b)

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676



677

(c)

(d)

678 **Fig. 17.** SEM images for (a) lightly cemented fine sand, (c) lightly cemented coarse sand, (b)

679

heavily cemented fine sand (d) heavily cemented coarse sand

680 The microstructure of the coarse sand differs from that of the fine sand. Calcite accumulates
681 on the surface of the grains (surface coating), as well as on the effective locations (Fig. 16 (e)-
682 (h)). The calcite crystals have similar shape and size to the ones observed in the case of the fine
683 sand; however, they form clusters indicating that calcite gradually precipitates within the
684 matrix (Terzis and Laloui 2019).

685 The particle contacts enhanced by MICP-cementation account for a smaller percentage of the
686 deposited calcite resulting in lower strength gain (Fig 16 (a)). At higher cementation levels, the
687 strength increases because more cement accumulates on the surface of particles and on particle-
688 to-particle contacts. Given that the chemical efficiency is low in the coarse sand, it is not clear
689 whether the MICP method adopted here would allow for the coarse sand to reach a state similar
690 to the heavily cemented fine sands (all pores filled with calcite) and higher concentrations of
691 calcite may have to be used to produce larger calcium carbonate crystals.

692 The cemented fine sands can develop higher strength because of the higher number of contact
693 points and the more effective calcite distribution relative to the grains. Initial porosity is,
694 therefore, critical in the coarse sands, as higher relative density provides more interparticle
695 contacts and thus more effective locations for cementation, resulting in higher strengths.
696 Results by Al Qabany and Soga (2013), suggest that higher concentrations of calcium chloride
697 in the chemical solution during the injection phase could result in larger calcite crystals, which
698 could potentially provide more effective bonding in coarse sands. The controlled and targeted
699 cementation offered by the MICP procedure makes it a possible tool to develop artificial
700 sandstone with consistent characteristics that can be customized by changing the formation
701 process. The results also provide a potential approach to address the issue of uniform
702 cementation in field applications of MICP, especially with coarser materials, by carefully
703 calibrating bacterial urease activity, in conjunction with chemical concentrations in the
704 cementing solution, and injection rates to balance speed of the reaction with flow rates.

705 5. CONCLUSIONS

706 The proposed MICP strategy reliably delivered artificial carbonate cemented sand specimens
707 for laboratory testing purposes with consistent and controlled mechanical properties. Although
708 the coarse sand with mean particle size of 1.82 mm is not considered an ideal candidate for
709 MICP, the process presented in this paper was able to successfully produce cemented
710 specimens with a good degree of uniformity and repeatability, especially at higher cementation
711 levels. This outcome, in particular, provides a promising approach for other applications of
712 MICP, including field ones, involving coarser materials. The key to obtaining uniform and
713 repeatable products, especially in the coarser sand, was slow MICP reactions, due to lower
714 concentration of the cementation solution, which allowed full permeation through the
715 specimens. Long retention times, then, were required to ensure a high percentage of the
716 cementation solution was transformed into calcium carbonate.

717 The strength increase of both sands could be controlled by targeting the appropriate degree of
718 cementation through the number of injections. The identical treatment ensured consistency in
719 size and shape of calcium carbonate crystals for all specimens, with only the amount of
720 cementation changing between specimens. Strength increased exponentially with degree of
721 cementation for both types of sands, with a more pronounced gain in the fine sand than in the
722 coarse sand. This difference in strength cannot be explained solely by the cementation level,
723 as the size of the host grains and void spaces significantly affect the distribution, and therefore
724 the effectiveness, of the calcium carbonate. The microstructural images of the fine sand
725 specimens show that a few small calcium carbonate crystals are sufficient to cement particle-
726 to-particle contacts, whereas images of the coarse sand specimens show calcium carbonate
727 deposition on both the surface of the grain and the contact points between the particles,
728 requiring a larger amount of cementation to produce a comparable increase in strength.

729 The successful use of MICP to generate specimens using base materials with two very different

730 grain sizes established that more combinations of strength and porosity could be obtained using
731 intermediate grain sizes, or PSDs, to meet the requirement of laboratory testing programs
732 The findings of this study can be extended to other potential applications of MICP, especially
733 when coarser materials are involved.

734 **6. ACKNOWLEDGEMENTS**

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736 Cambridge. We thank Chris Knight and the Department of Engineering technical staff for their
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742 **8. REFERENCES**

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