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Note on fundamental physics tests from black hole imaging: Comment on "Hunting for extra dimensions in the shadow of Sagittarius A*"

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ABSTRACT

Several recent works have tested fundamental physics with horizon-scale black hole (BH) images, using the size $r_{\rm sh}$ and deviation from circularity ΔC of the BH shadow. For the Event Horizon Telescope image of Sgr A^{*}, limits on ΔC are not available due to the sparse interferometric coverage of the 2017 observations, alongside the short variability timescale of Sgr A^{*} compared to M87^{*}. We comment on the results of a recent preprint which purports to have derived new limits on extra dimensions using the deviation from circularity of Sgr A^{*}'s shadow. The latter is quoted to be $\leq 10\%$ as with M87^{*}, based on the "similarity" of the two shadows, which however is an incorrect assumption. In the immediate future, the simplest tests of fundamental physics from Sgr A^{*}'s image will mostly have to rely on $r_{\rm sh}$.

Keywords: High energy astrophysics — Astrophysical black holes — Black hole physics

1. INTRODUCTION

Millimeter-scale Very Long Baseline Interferometry (VLBI) has provided us the first horizon-scale images of supermassive black holes (BHs): these feature a central brightness depression, related to the underlying BH shadow (Luminet 1979; Falcke et al. 2000), surrounded by a bright ring of emission. In most scenarios, the BH shadow corresponds to the apparent image of the photon region, the region of space-time where photons are forced to travel along orbits (Perlick & Tsupko 2022). Various fundamental physics scenarios leave imprints on the BH shadow: conversely, horizon-scale BH images can thus be used to test fundamental physics, provided the size of the bright ring can serve as a proxy for the shadow size $r_{\rm sh}$, with little dependence on the accretion flow details, as is the case for the radiatively inefficient accretion flows surrounding both Sagittarius A* (Sgr A*) and M87* (see Narayan et al. 2019; Bronzwaer & Falcke 2021).

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2. BLACK HOLE SHADOW CIRCULARITY AND FUNDAMENTAL PHYSICS TESTS

Over the past years, considerable work has been devoted to tests of fundamental physics from the Event Horizon Telescope (EHT) images of M87^{*} (Akiyama et al. 2019; Kocherlakota et al. 2021). These have been based both on the size of the bright ring of emission (as a proxy for $r_{\rm sh}$), and the deviation from circularity of the shadow ΔC (Bambi et al. 2019), which quantifies the shadow's oblateness (Johannsen & Psaltis 2010). In Akiyama et al. (2019), the limit $\Delta C \leq 10\%$ has been quoted and translated into a deviation from the Kerr quadrupole moment of order 4.

In Vagnozzi & Visinelli (2019) (VV19 hereafter), we have shown how this limit can be used to test extra dimension scenarios such as the Randall-Sundrum model (Randall & Sundrum 1999a,b), and in particular constrain the AdS₅ curvature radius ℓ (see also Banerjee et al. 2020; Neves 2020; Hou et al. 2021). We found that the limit $\Delta C \leq 10\%$ translates to a limit of $\ell \leq 170$ AU.

Recently, Wu (2022) purported to have derived a new constraint on ℓ based on the new EHT image of Sgr A^{*} (Akiyama et al. 2022a). This preprint, almost entirely based on VV19 and following a similar analysis, quotes a deviation from circularity $\Delta C \leq 10\%$ for Sgr A^{*}, analogously to M87^{*}. We disagree with these findings, as the procedure used to derive the results are not correct. The author quotes the limit $\Delta C \leq 10\%$ on the basis of "Sgr A^{*} and M87^{*} [being] very similar and [...] accurately described by the Kerr metric" (see Footnote 1 of Wu 2022). However, limits on ΔC have not been quoted for Sgr A^{*}'s image, as explicitly discussed by the EHT collaboration on page 19 of Akiyama et al. (2022b), due to the sparse interferometric coverage of the observations taken in 2017 when Sgr A^{*} had been imaged (at the time of the observations the EHT network did not have enough telescopes online to robustly obtain circularity measurements). Moreover, the variability timescales $t_g \sim GM/c^3$ change considerably between Sgr A^{*} and M87^{*} due to the sheer difference in mass, with the short timescale of Sgr A^{*} leading to an extensive overnight variability. Therefore, it is not yet possible to perform an analysis similar to VV19 to obtain analogous results from Sgr A^{*}. In fact, some of the latest results based on the new image of Sgr A^{*} do not make use of ΔC (Chen et al. 2022; Jusufi et al. 2022; Chen 2022; Vagnozzi et al. 2022).

3. CONCLUSIONS

Horizon-scale BH images can be used to test fundamental physics, using the BH shadow's size $r_{\rm sh}$ and deviation from circularity ΔC . However, while for M87^{*} information on both $r_{\rm sh}$ and ΔC is available, for the 2017 EHT observations of Sgr A^{*} only the former one is available: therefore, in the near future, the simplest tests of fundamental physics from Sgr A^{*}'s shadow will inevitably have to be based on its size and not its oblateness, until the EHT collaboration or its successor will explicitly constrain the latter (Raymond et al. 2021). We have commented on erroneous results obtained in Wu (2022) in the context of extra dimensions, based on incorrect premises relating the circularity of Sgr A^{*}'s shadow. Besides $r_{\rm sh}$ and ΔC , complementary observables and techniques to explore new physics are being developed, including polarimetric measurements, the photon ring, and shadow drift (Chen et al. 2020; Hadar et al. 2021; Chen et al. 2022), all of which will soon be accessible to VLBI arrays.

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