

Avalanche criticality during ferroelectric/ferroelastic switching

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Abstract

Field induced domain wall displacements define ferroelectric/ferroelastic hysteresis loops, which are at the core of piezoelectric, magnetoelectric and memristive devices. These collective displacements are scale invariant jumps with avalanche characteristics. Here, we analyse the spatial distribution of avalanches in ferroelectrics with different domain and transformation patterns: $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3\text{--PbTiO}_3$ contains complex domains with needles and junction patterns, while BaTiO_3 has parallel straight domains. Nevertheless, their avalanche characteristics are indistinguishable. The energies, areas and perimeters of the switched regions are power law distributed with exponents close to predicted mean field values. At the coercive field, the area exponent decreases, while the fractal dimension increases. This fine structure of the switching process has not been detected before and suggests that switching occurs via criticality at the coercive field with fundamentally different switching geometries at and near this critical point. We conjecture that domain switching process in ferroelectrics is universal at the coercive field.

In ferroelectric materials, domain walls separate regions with different polarization directions. Their dynamical behaviour is subject to intense fundamental and applied research as it is at the core of ferroelectric switching¹⁻⁴, which is the key design parameter e.g. in piezoelectric^{5,6}, magnetoelectric⁷⁻⁹ and memristive¹⁰⁻¹² devices, as well as in devices operating above GHz frequencies¹³. Furthermore, the recent research on two dimensional functionalities offered by ferroelectric domain walls¹⁴⁻¹⁷ will find further applications once strategies to dynamically deploy the functionalities, through the motion of domain walls, have been found.

Therefore, understanding the response of domain walls to electric fields is particularly appealing. With this aim, two distinct approaches have been developed. The first one relies on the study of individual domain wall movement on long-time scales. It describes the nucleation and growth of domains and their interaction with defects, interfaces and existing domain walls¹⁸⁻²⁰. The second one aims to understand collective movements during short-time scales^{21,22}. It considers discrete impulsive jumps, or ‘jerks’, occurring during the motion of domain walls, as indicators of avalanches on a broad range of scales. In such ferroelectric avalanches, any switching event is likely to trigger subsequent switching, and anisotropic long-range interactions between local events are essential, in contrast with classic microscopic ferroelectric models^{23,24}. This approach is particularly relevant for the development of neuromorphic computing architectures²⁵ where maximal computational performances are achieved through scale-invariant avalanches that develop at a critical point^{26,27}, similar to neuronal avalanches observed in the brain²⁸. The key question is whether this switching dynamics is a universal process in ferroelectrics with little or no influence from symmetry or structural features of domain walls.

Mean-field (MF) theory applied to ferroelectrics predicts the power-law distribution of jerks²⁹, which is one of the signatures of scale-free processes, and atomistic simulations show that avalanches are induced by kinks and domain walls junctions³⁰⁻³², as well as defects acting as

pinning centres³³. Ultraslow processes have been modelled³⁴ and reveal that many of the relevant ferroelectric parameters, e.g. the size of the switching events, follow power law dependences under switching conditions. In order to confirm the origin of the avalanches, optical visualisation is required and has been successfully applied during the phase transition of martensitic materials^{35–37} and during switching in magnetic thin films³⁸, but not in ferroelectric materials where avalanches are usually studied through indirect methods, e.g. acoustic emission²² or displacement current measurements^{39,40}. Previous to these observations, avalanche studies already revealed the stepwise behaviour of domain wall movements under electric fields but did not lead to a quantitative analysis of avalanche characteristics^{41–43}.

In this work, we combine optical microscopy and statistical analyses to characterize the motion of ferroelastic domain wall during ferroelectric switching in two ferroelectric materials: tetragonal BaTiO₃ (BTO), for which avalanches have already been studied with acoustic emission²², and monoclinic Pb(Mg_{1/3}Nb_{2/3})O₃–PbTiO₃ (PMN–PT) close to the morphotropic boundary⁴⁴. They show very different ferroelastic domain and transformation patterns: BTO is dominated by parallel straight charged domain walls (which we have already characterized in a previous work⁴⁵), while in PMN-PT straight walls intersections lead to complex domain walls, which are often bent, forming needle and junction patterns whose switching differ greatly depending on the starting domain structure⁴⁶. Our optical observations bring the experimental evidence that avalanches are triggered at kinks and domain wall junctions. Furthermore, our ability to image directly the avalanches gives us the possibility to explore the spatiotemporal changes of the ferroelectric domain pattern to identify switched regions. We find that the areas of the switched regions, their energies and perimeters are power law distributed with power law exponents close to the predicted MF values. We also show that during ferroelectric switching, the fractal dimension of the switched regions increases and reaches a maximum at the coercive field. This fine structure of the switching process has not

been detected before. Our results suggest that the change of the fractal dimension is the key observable to understand ferroelectric domain motion under electric field and that switching occurs via criticality at the coercive field with fundamentally different switching geometries at and near this critical point. This behaviour is seen in PMN-PT and BTO so that we conjecture that the overall domain switching process in ferroelectrics may be universal and show little dependence on the details of the actual domain patterns.

Figs. 1a,d show two domain patterns of PMN-PT and BTO, visualised with an optical microscope in transmission mode, as representative examples. The regions switching during the application of a positive voltage, i.e. the ferroelectric avalanches, are shown in Figs. 1b,e. For low voltages (< 200 V for PMN-PT and < 120 V for BTO), switched regions, defined as topological connected entities where pixels intensity change, form patches of small areas, around the domain walls. On approaching the coercive field (250 V for PMN-PT and 170 V for BTO), the number of switched regions increases and their area distribution becomes broader. At even higher fields (~ 350 V for PMN-PT and ~ 250 V for BTO), virtually no switching occurs and the number of switched regions decreases accordingly. After a full hysteresis loop, the accumulation maps (Figs. 1c,f) show the location of the avalanches through the number of times each pixel has been changed, i.e. the activity. These maps show that almost the entire field of view has been switched and that most changes occur around domain walls. The low activity far from the coercive field indicates that most of the intensity variations induced by the linear electrooptic are too small to be detected and remain within noise level. The accumulated activity is higher in PMN-PT with its high concentration of bent domain walls, junctions, kinks and intersections (Note 1 in the Supplementary Information), confirming that avalanches are triggered at kinks and domain wall junctions^{30–32}. These patterns differ greatly from the domain patterns in BTO (Figs. 1d,f) where domain walls are much straighter and form few intersections. Nevertheless, small domain patches also form in BTO in

front of advancing domain boundaries, which are topologically very similar to the domain patches in PMN-PT (an example for a single domain in BTO is shown in the Note 5 of the Supplementary Information).

In Fig. 2, spatiotemporal avalanche maps of PMN-PT (Figs. 2a-g) and BTO (Figs. 2h-j) are shown. In Figs. 2b,c and Figs. 2i,j we observe that most avalanches occur at the coercive field (250 V for PMN-PT and 170 V for BTO) and that they are located in the vicinity of domain walls. We established a data set of the areas A of all switched regions and the corresponding energies as the square of the areas ($E = A^2$). We also determine the perimeter P of the switched regions. Scaling P as a function of A yields the Hausdorff dimension H_D with $P \sim A^{H_D/2}$ (ref. 47, Notes 2 and 3 in Supplementary Information), shown in Figs. 2f,g. We calculate the area exponent τ assuming a power-law distribution of the area with the probability distribution per area interval $\text{PDF}(A) \sim A^{-\tau}$, as shown in Figs. 2d,e. At the coercive field we find $\tau = 1.7$ while the overall exponent is above 2. By comparing Figs. 2d,e and Figs. 2f,g, the anticorrelation between τ and H_D is seen when the number of switched regions is high. In the creep regime, at high voltages, we observe few small changes of the domain patterns. The same behaviour, including the anticorrelation between τ and H_D , holds independently of the domain pattern in any of the analysed regions. In particular, in PMN-PT, the upper part of the sample – dominated by straight walls – and the lower part of the sample – dominated by needle and junction patterns – behave similarly (Figs. 2b,d,f).

In Figs. 3 and 4 we plot the log-log dependences of the area, energy and perimeter for both materials together with their Hausdorff dimensions, as integrated over the full field of view. The anticorrelation between the area exponent τ and the Hausdorff dimension H_D becomes obvious in Figs. 3a and 4a. The distribution of area, energy and perimeter at selected representative points (numbers 1, 2 and 3) in the different regimes are shown in Figs. 3c and 4c. At the coercive field, the switching operates with the lowest τ (regime 1), while τ increases

in the vicinity, but away from the coercive field value (regime 2). The τ -values in the creep regime (regime 3), where the jerks are uncorrelated and do not represent power laws, are approximated by the asymptotic behaviour of the slope near the upper value of the areas (respectively energies or perimeters) in the PDF curves. These values have no direct physical meaning besides showing that in this regime no significant switching occurs. The Hausdorff dimension in this regime is $H_D=1$.

The anticorrelations are quantitatively shown in Figs. 3b and 4b. At the minima of τ we find the maxima of H_d . The minimum value of τ is 1.7 (energy exponent $\varepsilon=1.3$) in both materials, the corresponding Hausdorff dimension is ~ 1.8 . The changes of the domain patterns are highly fractal and contain a multitude of large regions with rough surfaces, which contribute greatly to the increase of the number of avalanches at minima in τ (Figs. 3e,4e). With increasing τ -value we find that H_D decreases until the switching interval has passed and H_D approaches unity (Figs. 3a and 4a). Comparing these fine structures of the switching process with the total switching behaviour as seen in Figs. 3d and 4d, the value of $\tau \sim 2-2.2$ is obtained, in accordance with results of previous acoustic emission measurements in BTO²². The closeness of this exponent to that of regime 2 is understood by the larger duration of regime 2 compared with regime 1 and the high number of switching events over a broader interval (Fig. 3e,4e). The field dependence of this activity (Figs. 3e,4e) reproduces the ferroelectric hysteresis very well, indicating the predominant role of ferroelastic domain walls in mixed ferroelectric/ferroelastic systems.

Strain fields, which are long ranging and anisotropic, induce correlations that are a key element in avalanches²². Such correlations had already been inferred from studies of switching dynamics in polycrystalline materials, where depolarization fields are screened by adapting local bound charges and elastic interactions dominate. In these systems, ferroelastic domain walls are highly mobile compared to 180° domain walls and their synchronized movements

within grains is shown to reproduce well the ferroelectric hysteresis loop⁴⁸⁻⁵⁰. Even in uniaxial ferroelectrics (e.g. LiNbO₃ and LiTaO₃), where avalanche behaviour related to the movement of non-ferroelastic 180° domain walls have been observed (but not quantified)^{51,52}, it is possible that secondary local strain⁵³ accompanying the movement of domain walls plays a role. In fact, in magnetic systems, it has been shown that even magnetic Barkhausen noise depends explicitly and strongly on strain coupling^{54,55}.

We note that our observations for ferroelectrics are also consistent with results obtained in other critical systems, e.g. during the failure of materials where the energy exponent ε decreases before failure⁵⁶⁻⁵⁸, sometimes down to the MF value $\varepsilon = 1.3$, when the system reaches the critical point⁵⁸ while the rate of energy release diverges⁵⁹⁻⁶¹.

We have shown that ferroelectric/ferroelastic switching progresses via avalanches in two typical ferroelectric materials. We are able to correlate the visible domain switching with predictions of avalanche theory and show the close agreement with the results of previous measurements of acoustic emission in BTO²². The closeness of the avalanche characteristics with those predicted by MF theory⁶² is remarkable. Surprising and somewhat counterintuitive is the observation that fine structures appear during the switching process. The presumed critical point of the switching process is the coercive field. At the coercive field, the area and energy exponents correspond to an unrelaxed MF value ($\varepsilon = 1.3$, $\tau = 1.7$), while the fractality is maximum with $H_D = 1.8$. In the creep regime, far away from the main switching, the areas are exponentially distributed which indicates uncorrelated noise and $H_D=1$. In between these two regimes, the switching progresses with exponents near the field integrated MF model with $\varepsilon = 1.6$ and $\tau \sim 2.2$. The switching activity in this regime is reduced but spreads over a longer time so that the overall switching follows $\varepsilon = 1.6$ and $\tau = 2.2$. We don't observe exponent mixing as could be expected⁶³ but our experimental resolution is probably insufficient for the investigation of mixing. Furthermore, the mixing proceeds not simply via two fix points with

two exponents but via a continuous distribution of exponents which increase continuously from $\varepsilon = 1.3$ and $\tau = 1.7$ to greater values. Simultaneously H_D decreases, which implies that the switched regions become more compact, with interfaces that are much smoother than those at the critical point. At these late stages of the switching process, smooth domain walls progress without much change to their shape. The universal framework presented here suggests operating ferroelectrics close to the coercive field, where criticality and scale-invariant avalanches develop, maximizing their properties.

Methods

Samples. The PMN-PT (001) sample, with composition $(1-x)[\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3]-x[\text{PbTiO}_3]$, $x=0.32$, is a commercial sample from Atom Optics Co., LTD. (Shanghai, China), with dimensions $5 \times 1 \times 0.5 \text{ mm}$. The BTO (111) sample is from MTI corporation (USA), with dimensions $6 \times 1 \times 1 \text{ mm}$.

Optical microscopy and displacement current measurements. We visualized the ferroelectric domain structure with an optical microscope in transmission mode (Leica), using an objective with magnification 20X and numerical aperture 0.4. The experimental setup is described in ref. ⁴⁵, polarized white light is transmitted through the sample and an analyser is used to select the polarization state before the CCD camera. The optical contrast between ferroelastic domains arises from the unique symmetric polar tensor of second rank determining the optical indicatrix of each ferroelastic domain state. In order to move domain walls, we applied an electric field along the $[100]_{\text{pc}}$ direction for PMN-PT (1-mm thick) and the $[-110]_{\text{pc}}$ direction for BTO (1-mm thick) with two silver-paint electrodes on the sides of the samples. We used a picoammeter (Keithley 6487) to measure the displacement current of the sample while cycling the applied electric field (Note 6 in the Supplementary Information) to ensure that full switching loops are measured. We cycled the voltage (electric field) between 0 and

$\pm 500\text{V}$ for PMN-PT at 10 V s^{-1} and from 0 to $\pm 300\text{ V}$ for BTO at 7 V s^{-1} with a triangular function while recording optical images at 30 frames per seconds (noted as $\delta t = 1/30\text{ s}$). The results presented are obtained after more than 10 cycles to avoid ‘virgin’ effects.

Statistical analysis of optical images. In order to identify the avalanches, we perform a pixel by pixel analysis of the optical images during switching. Jerks J_{ij} in intensity as a function of time are defined as:

$$J_{ij} = \left(\frac{dB_{ij}}{dt} \right)^2$$

where B_{ij} is the intensity at each pixel (i and j are indices used for the spatial coordinates). The areas A of the switched regions are defined as topological connected entities where the values of J_{ij} are greater than a threshold. Detailed analysis shows that these regions contain an almost constant intensity (Notes 2 and 3 in the Supplementary Information). We use as threshold a value that is twice the mean value of the pixel’s noise under the absence of electric field. The exact value of the threshold proved irrelevant for our observations.

For exponents, we use τ for areas, ε for energies, and δ for perimeters. They are derived from the probability distribution function (PDF) as slopes of the log-log PDF curves and, independently by the maximum likelihood method⁶⁴ (Note 5 in Supplementary Information).

We compute the entropy of the avalanche images as $-\sum p \log_2(p)$, where p contains the normalized histogram counts of switched pixels and we fit its evolution with the avalanche occupancy with a parabolic function, following percolation theory⁶⁵ (Notes 2 and 3 in Supplementary Information).

Data availability

Optical microscopy videos showing the evolution of the domain structure during ferroelectric switching are available from the corresponding author on request.

Code availability

The code used for the statistical analysis of optical images is available upon request.

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Author Contributions

All authors contributed to writing the manuscript and discussing the results. E.K.H.S. supervised the project. B.C. and G.F.N. performed the experiments. Data analysis and code development was done by B.C.

Competing Interests

The authors declare that they have no conflict of interest.

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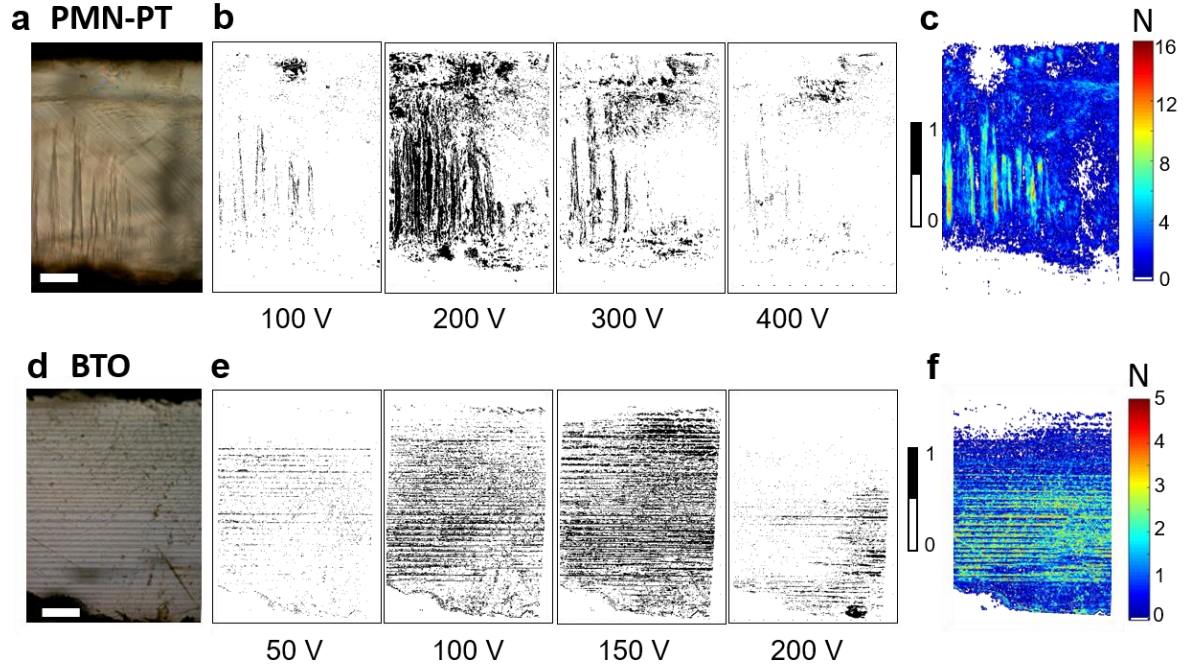


Figure 1. **Localisation of avalanches for PMN-PT and BTO.** Optical image of the initial state of the sample for (a) PMN-PT and (d) BTO. The scale bar indicates 200 μm . Switched regions for (b) PMN-PT and (e) BTO, at representative applied voltages. The black regions (assigned to 1) are regions that switched between t and $t+\delta t$, with $\delta t = 1/30$ s, while the white regions (assigned to 0) remained unchanged. Accumulated activity maps after a full hysteresis loop for (c) PMN-PT and (f) BTO. The colour scale indicates the number of times each pixel ($\sim 1 \mu\text{m}^2$ in size) has been changed.

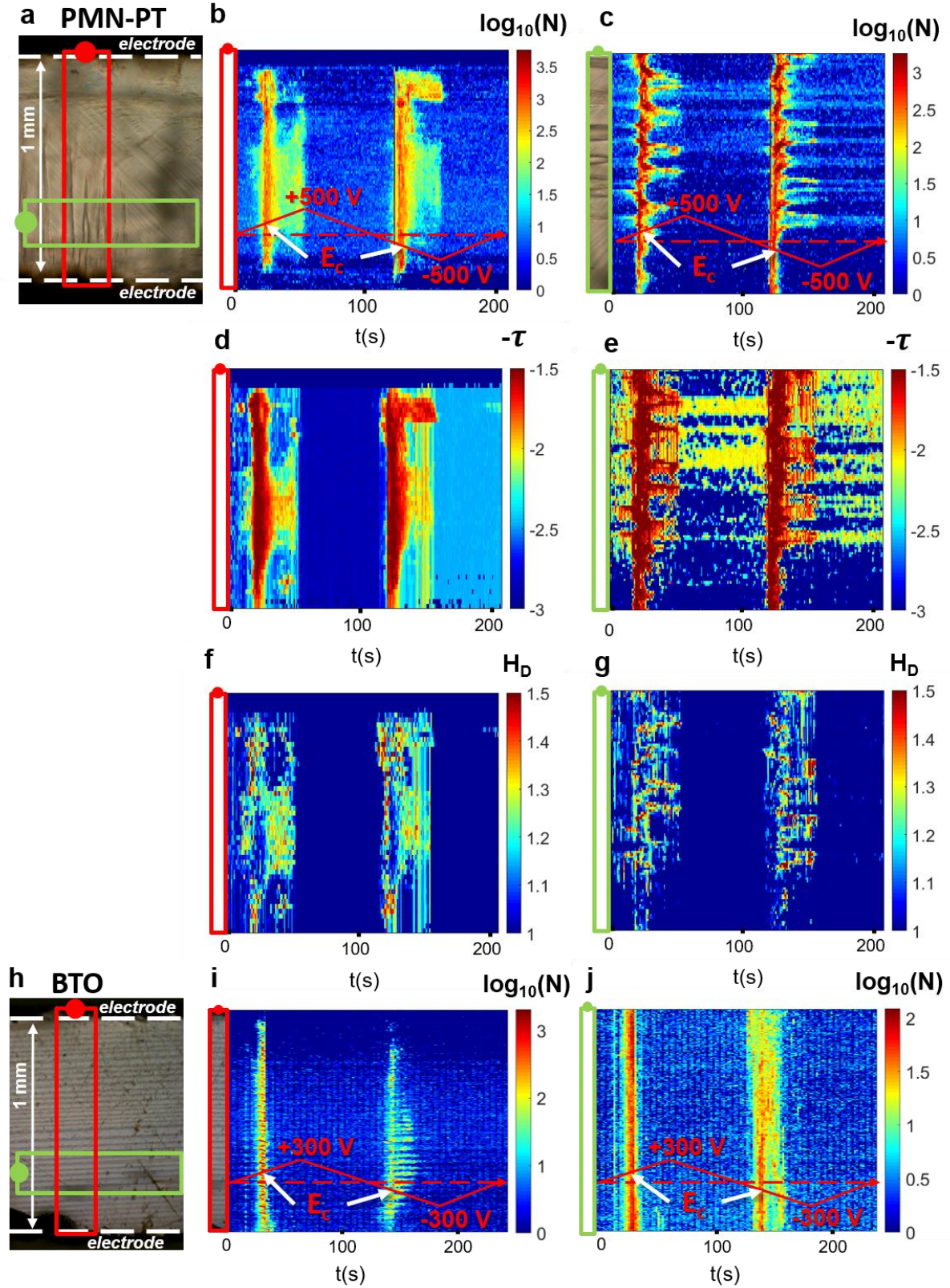


Figure 2. **Spatiotemporal avalanche maps for (a-g) PMN-PT and (h-j) BTO samples.** The red and green rectangles in the optical images a and h are analysed further in b, d, f, i (red) and c, e, g, j (green). Accumulated avalanche activities integrated over space N for (b, c) PMN-PT and (i, j) BTO. (d, e) The avalanche exponent τ and (f, g) the Hausdorff dimension H_D are shown for PMN-PT. Similar graphs for BTO are shown in the Note 4 of the Supplementary Information.

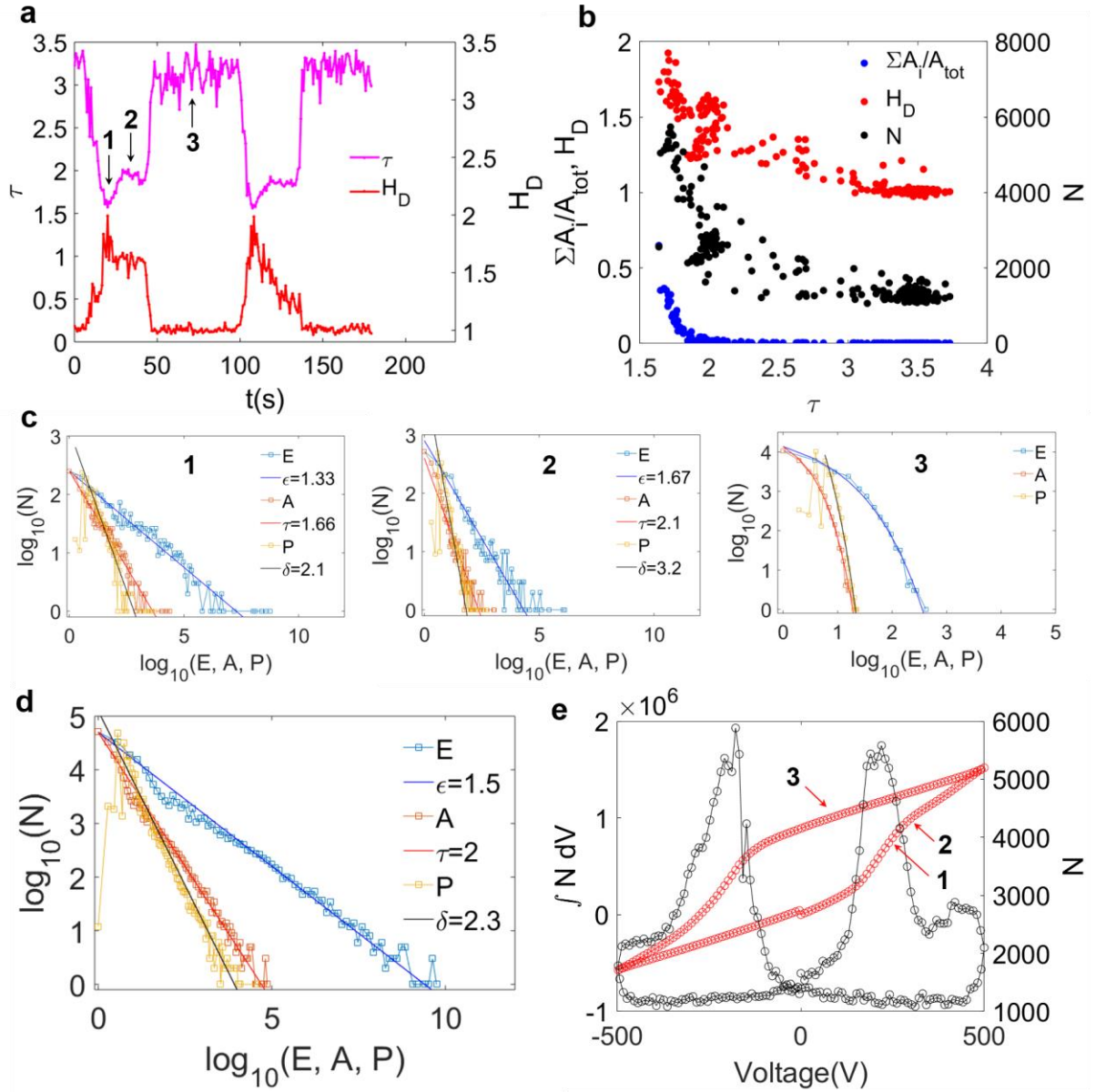


Figure 3. **Scale-invariant avalanches in PMN-PT.** (a) H_D and τ as a function of time. (b) H_D , $\Sigma(A_i)/A_{tot}$ (proportion of switched regions with respect to the total area) and N (avalanche activity, defined as the number of switched regions between t and $t+\delta t$) as a function of τ . (c) E (energy), A (area), P (perimeter) distribution at the time steps marked as 1, 2 and 3 by arrows in (a). (d) E , A , P distribution from all the time steps. (e) N as a function of the applied voltage (right axis) and its integration over the voltage applied (left axis).

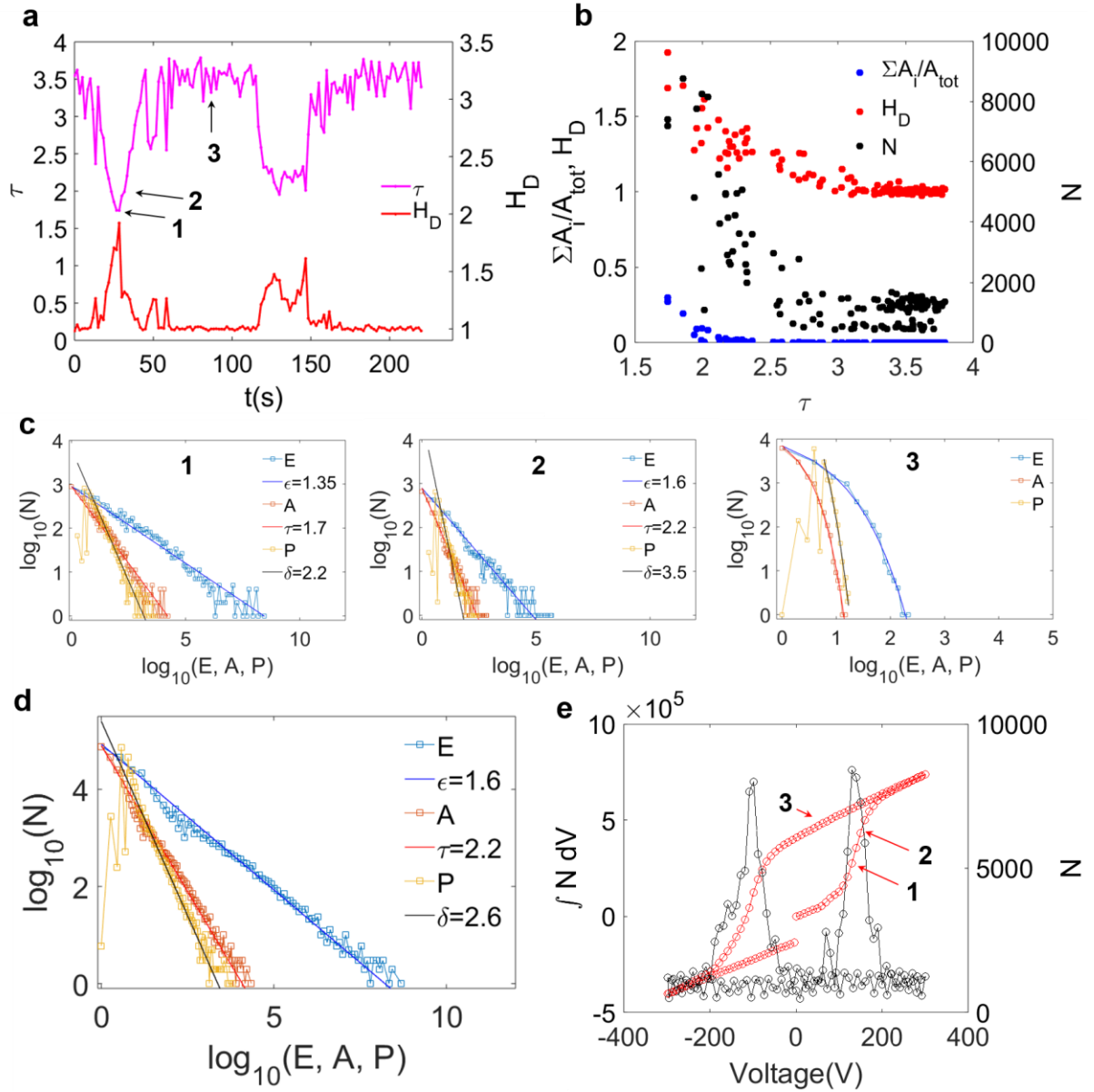


Figure 4. **Scale-invariant avalanches in BTO.** (a) H_D and τ as a function of time. (b) H_D , $\Sigma(A_i)/A_{tot}$ (proportion of switched regions with respect to the total area) and N (avalanche activity, defined as the number of switched regions between t and $t+\delta t$) as a function of τ . (c) E (energy), A (area), P (perimeter) distribution at the time steps marked as 1, 2 and 3 by arrows in (a). (d) E , A , P distribution from all the time steps. (e) N as a function of the applied voltage (right axis) and its integration over the voltage applied (left axis).